

Constant head pumping tests
in oxidized glacial till
by
Chin-Ta Tsai

A Thesis Submitted to the
Graduate Faculty in Partial Fulfillment of the
Requirements for the Degree of
MASTER OF SCIENCE

Department: Civil & Construction Engineering
Interdepartment Major: Water Resources

Approved:

Signatures have been redacted for privacy

Iowa State University
Ames, Iowa
1991

TABLE OF CONTENTS

	Page
INTRODUCTION AND OBJECTIVES	1
LITERATURE REVIEW	3
General Description of Glacial Till	3
Hydraulic conductivity and specific yield	4
Mathematical Model	7
Theis solution	7
Super-position method	10
Jacob correction method	12
FIELD SITE AND EXPERIMENT PROCEDURE	16
Test Site	16
Experiment Procedure	22
Field test	22
Data analysis	24
RESULTS AND DISCUSSION	27
Soil Character Test	27
Results	27
Discussion	33
Constant-Head Pumping Test	34
Results of pumping test #1	34
Pumping rate and drawdown response	34
Hydraulic conductivity and specific yield	37
Results of pumping test #2	46
Pumping rate and drawdown response	46
Hydraulic conductivity and specific yield	50
Discussion	58

	Page
CONCLUSION	67
RECOMMENDATION FOR FURTHER RESEARCH	69
BIBLIOGRAPHY	70
ACKNOWLEDGMENTS	73
APPENDIX A. ORIGINAL DATA of PUMPING RATE vs TIME	74
APPENDIX B. SIMPLIFIED DATA of PUMPING RATE vs TIME	89
APPENDIX C. DATA of OBSERVED DRAWDOWN and PREDICTED DRAWDOWN vs TIME	93
APPENDIX D. CURVE FITTING DIAGRAMS in LOG-LOG SCALE	106

LIST OF FIGURES

	Page
Figure 1. Nomenclature for continuously varying pumping rate	11
Figure 2. Location of the study field	17
Figure 3. Location of the test site	18
Figure 4. Plan view of the well layout	20
Figure 5. Vertical cross-section view of a representative well	21
Figure 6. Schematic diagram of the equipment layout	25
Figure 7. Depth of transition zone versus radial distance	29
Figure 8. Textural data for the test site	32
Figure 9. Test #1 & test #2, pumping rate versus time, in normal scale	35
Figure 10. Test #1 & test #2, pumping rate versus time, in log-log scale	36
Figure 11. Test #1, drawdown response curves of wells on line A in the first 2.5 hours of pumping	38
Figure 12. Test #1, drawdown response curves of wells on line B in the first 2.5 hours of pumping	39
Figure 13. Test #1, drawdown response curves of wells on line C in the first 2.5 hours of pumping	40
Figure 14. Test #1, drawdown response curves of wells on line A over the 9.5 hour pumping period	41
Figure 15. Test #1, drawdown response curves of wells on line B over the 9.5 hour pumping period	42
Figure 16. Test #1, drawdown response curves of wells on line C over the 9.5 hour pumping period	43
Figure 17. Test #1, the curves of the drawdown response and the least squares fitting for wells on line A	47

	Page
Figure 18. Test #1, the curves of the drawdown response and the least squares fitting for wells on line B	48
Figure 19. Test #1, the curves of the drawdown response and the least squares fitting for wells on line C	49
Figure 20. Test #2, drawdown response curves of wells on line A in the first 2.5 hours of pumping	51
Figure 21. Test #2, drawdown response curves of wells on line B in the first 2.5 hours of pumping	52
Figure 22. Test #2, drawdown response curves of wells on line C in the first 2.5 hours of pumping	53
Figure 23. Test #1, drawdown response curves of wells on line A over the 24 hour pumping period	54
Figure 24. Test #2, drawdown response curves of wells on line B over the 24 hour pumping period	55
Figure 25. Test #2, drawdown response curves of wells on line C over the 24 hour pumping period	56
Figure 26. Test #2, the curves of the drawdown response and the least squares fitting for wells on line A	59
Figure 27. Test #2, the curves of the drawdown response and the least squares fitting for wells on line B	60
Figure 28. Test #2, the curves of the drawdown response and the least squares fitting for wells on line C	61

LIST OF TABLES

	Page
Table 1. Methods used for investigating hydraulic conductivity of glacial till from 1975 to 1990, based on Lutenegger's literature review (1990)	6
Table 2. The different conditions between the two pumping tests	24
Table 3. The depth of transition zone	28
Table 4. Results of soil character tests (A)	30
Table 5. Results of soil character tests (B)	31
Table 6. Estimations of the flow parameters by test #1	45
Table 7. Estimations of the flow parameters by test #2	57
Table 8. Comparison of flow parameters estimated by both pumping tests and slug tests	62

INTRODUCTION

Accurate determination of flow parameters in porous media, notably, hydraulic conductivity (K), and specific yield (S_y) is necessary for a quantitative understanding of most problems in hydrogeology. In central Iowa it is not uncommon to find a soil profile which consists of an oxidized glacial till deposit underlain by an unoxidized layer. Recently, the fate and transport of water and chemicals in glacial till has become of concern. In the glaciated regions of Iowa, groundwater flow and contaminant transport in glacial till impacts agricultural chemicals, landfills, and underground storage tanks.

Bail tests and laboratory permeameter tests have been widely applied to investigate the hydrogeologic parameters of glacial till. Due to the low permeability, glacial tills are not commonly used for water supply and pumping tests are seldom done in glacial till. There are a wealth of data on flow parameters of glacial tills generated by bail tests or laboratory permeameter tests, but, to the author's knowledge, there are no published results for pumping tests in glacial till.

While many field studies have been done using constant discharge rate pumping tests, there is little literature relating to constant head pumping tests. A constant head

pumping test is a pumping test in which the drawdown is held constant in the pumped well and the discharge varies with time. In a low conductivity medium with a small saturated thickness, selecting a constant pumping rate can be difficult. The constant pumping rate must be high enough to create a sufficient drawdown in the surrounding area for the data analysis, while avoiding pumping the well dry before the desired pumping duration is reached. Under such circumstances, a constant head pumping test may be a better choice.

The objectives of the research are to:

1. Study whether the constant-head pumping test is suitable in glacial till.
2. Determine the hydraulic conductivity and the specific yield of oxidized glacial till in central Iowa using constant-head pumping tests.
3. Compare the results of pumping tests and slug tests.

Two constant-head pumping tests were performed in an oxidized glacial till layer. The super-position of the Theis solution was fit to drawdown data modified by the Jacob correction to estimate the hydraulic conductivity and the specific yield of oxidized till. Also, the hydraulic conductivity estimated by the pumping tests were compared with that estimated by the slug tests performed by Lemar(1990).

LITERATURE REVIEW

General Description of Glacial Till

Glacial till is the most abundant material that was deposited on the land surface during Pleistocene time. In the regions in Northern America, glacial erosion produced till that generally has considerable silt and clay and therefore has low permeability. The glacial environment is one of the most complicated of all geologic environments, having a wide variety of sedimentational processes and resulting deposits. Goldthwait (1971) remarked: "Till has more variations than any other sediment with a single name." Most glacial till deposits can be classified into two general categories: supraglacial till and subglacial till (or basal till) based on the environments of deposition. Due to the effect of weathering, glacial till also can be separated into two kinds of glacial till: weathered (or oxidized) glacial till and unweathered (or unoxidized) glacial till (Lutenegger et al., 1983).

Subglacial till was formed at the glacier base while the supraglacial till was formed on the upper surface of the ice. Generally, subglacial till is more uniform in texture and has higher bulk densities in contrast to supraglacial till. Extensive discussion of glacial deposits can be found in Lutenegger et al., (1983), Kemmis et al., (1981), and Boulton

and Paul, (1976).

Due to the effect of the weathering process, the original deposition properties of glacial till may be significantly changed. The most obvious and recognizable change is the iron oxidation compound in soils producing yellowish brown, or reddish brown color from initially unoxidized, dark gray glacial till. It is not uncommon to find fractures and root penetration in the oxidized zone, particularly at shallow depth. The change of deposition properties can alter hydrogeological properties (Lutenegger et al., 1983). Especially, fractures are recognized as an important factor which dramatically increase the bulk hydraulic conductivity. It has been found that the bulk hydraulic conductivity of fractured glacial till determined by field tests is commonly between 1 to 3 orders of magnitude larger than values of intergranular hydraulic conductivity determined by laboratory tests on unfractured samples. (Freeze and Cherry, 1979)

Hydraulic conductivity and specific yield

A number of studies have investigated the hydraulic conductivity of glacial till. Lutenegger (1990) performed a comprehensive literature review to identify technical papers related to the hydraulic conductivity of glacial materials, in particular, tills. Lutenegger suggested that the results of the hydraulic conductivity investigation appear to be

related to the scale effect of the test technique used and illustrates the wide range of values (10^{-5} cm/s to 10^{-9} cm/s) encountered in these materials. Table 1, which is summarized from Lutenecker's review, shows the type of test methods used since 1975. The review indicates that most researchers tend to investigate the hydraulic conductivity of glacial till by slug tests in situ, or by laboratory methods, including falling head and constant head tests, and consolidation tests. The pumping test method was employed only by Grisak & Cherry (1975). Grisak & Cherry performed the pumping tests in a basal sand confined aquifer and monitored the response in the till confining layer. Since laboratory permeameter methods can only be used to investigate hydraulic conductivity, and the specific yield generated by the slug tests are not reliable (Freeze & Cherry, 1979), information on the specific yield of glacial till is very limited.

Table 1. Methods used for investigating hydraulic conductivity of glacial till from 1975 to 1990, based on Lutenegeger's literature review (1990)

Researchers	Methods		
	Laboratory tests	Slug Tests	Pumping tests
Prudic (1981)	*	*	
Little (1988)	*		
Desauliniers et al. (1981)	*	*	
Goodall & Quigley (1977)	*	*	
Keller et al. (1986)	*	*	
Grisak & Cherry (1975)	*		*
Law & Lee (1981)	*		
Hendry (1982)	*	*	
Craven & Ruedisll (1987)		*	
Starrett and Edil (1982)		*	
Sharp (1984)	*	*	
Bradbury & Muldoon (1990)		*	
Total:	9	9	1

Mathematical Model

To estimate the hydraulic conductivity and specific yield from a pumping test, a mathematical model is required in which the response of the aquifer to pumping is a function of the parameters. In this section, the information about the mathematical models which are relative to the analysis of a constant head pumping test in an unconfined aquifer will be provided.

The Theis solution (Theis, 1935) has been widely applied in analyzing constant rate pumping tests in aquifers. It is recognized that the Theis solution is also applicable to other boundary conditions with adjustment. The Theis solution, after being modified by the super-position method, may be used to analyze the drawdown response of a constant head pumping test which has continuously varying discharge (Stallman, 1962). For a pumping test in a homogeneous, isotropic, infinite unconfined aquifer, the drawdowns can be treated as that which would occur in an equivalent confined aquifer after they are corrected by the Jacob correction method and the early time drawdown data are ignored due to the effect of vertical flow.

Theis solution

In 1935, Theis utilized an analogy to the heat-flow equation given by H.S. Carslaw to arrive at an analytical

solution to the motion of ground water flow in a confined aquifer due to well pumping. The governing equation which describes unsteady radial flow to a well in a confined aquifer due to well pumping is written in terms of drawdown (Bear, 1979)

$$\frac{\partial^2 s}{\partial r^2} + \frac{1}{r} \frac{\partial s}{\partial r} = \frac{S}{T} \frac{\partial s}{\partial t} \quad (1)$$

with boundary conditions,

$$s(r, 0) = 0, r_w \leq r < \infty \quad (2)$$

$$s(\infty, t) = 0, t > 0 \quad (3)$$

$$\lim_{r \rightarrow r_w} 2\pi T \frac{\partial s}{\partial r} = -Q = \text{const.}, t > 0 \quad (4)$$

where $s(r, t)$ = the drawdown, at radial distance r and time t , (L); r_w = the radius of the well, (L); Q = the discharge of the pumping well, (L³/T); T = the coefficient of transmissibility of an aquifer, which is defined as the product of hydraulic conductivity and the thickness of the aquifer, (L²/T); S = the coefficient of storage, (as a decimal, dimensionless). Equation (1) assumes the medium is homogeneous and isotropic, flow is horizontal, and T and S are constant. The solution of (1) to (4) is (Theis, 1935)

$$s(r, t) = (Q/4\pi T) \int_{r^2 S/4Tt}^{\infty} (e^{-u}/u) du \quad (5)$$

The value of the integral in equation (5) is given by the exponential integral

$$\int_u^{\infty} \left(\frac{e^{-u}}{u}\right) du = -0.577216 - \ln u + u - \frac{u^2}{2 \cdot 2!} + \frac{u^3}{3 \cdot 3!} - \frac{u^4}{4 \cdot 4!} + \dots \quad (6)$$

where

$$u = \frac{r^2 S}{4Tt} \quad (7)$$

In the groundwater literature, the integral (6) is known as the well function, $W(u)$. With this notation, equation (5) can be rewritten as

$$s(r, t) = \frac{Q}{4\pi T} W(u) \quad (8)$$

Theis (1935) noted that theoretically, equation (8) applies rigorously only to water-bodies (i) being contained in entirely homogeneous sediments, (ii) of infinite areal extent, (iii) in which the well penetrates the entire thickness of the water-body, (iv) in which the coefficient of transmissibility is constant at all times and in all places, (v) in which the pumping well has an infinitesimal diameter, and (vi), applicable only to unconfined water-bodies in which the water in the volume of sediments through which the water-table has fallen is discharged instantaneously with the fall of the water-table. Also, the pumping rate should be uniform

and continuous. An ideal well pumping system has the boundary conditions: (i) The system is located in a confined aquifer with horizontal impermeable layers on the top and bottom, (ii) The thickness of the aquifer is constant, (iii) The aquifer is homogeneous, isotropic, and infinite, (iv) The diameter of the pumped well is infinitesimal, (v) The pumping well penetrates the whole thickness of the aquifer, (vi) The pumping rate is uniform and continuous. The equation (8) gives the drawdown at any point and time for an ideal well pumping system when the pumping rate and the aquifer constants, coefficients of transmissibility and storage, are known. Inversely, the transmissibility and specific yield can be estimated by fitting equation (8) with data of the measured drawdown, whether at different places or at the same place at different times, and the pumping rate.

Super-position method

The pumping rate of a constant-head pumping test continuously decreases with time because of the decrease in the head gradient with time. If the pumping rate is plotted against time, the smooth curve will be similar to the example shown in Figure 1. This smooth curve may be approximated by a series of discrete pumping rates as shown in Figure 1. Applying the principle of super-position to the Theis solution (8), the drawdown caused by the simulated stepped pumping rates is given by

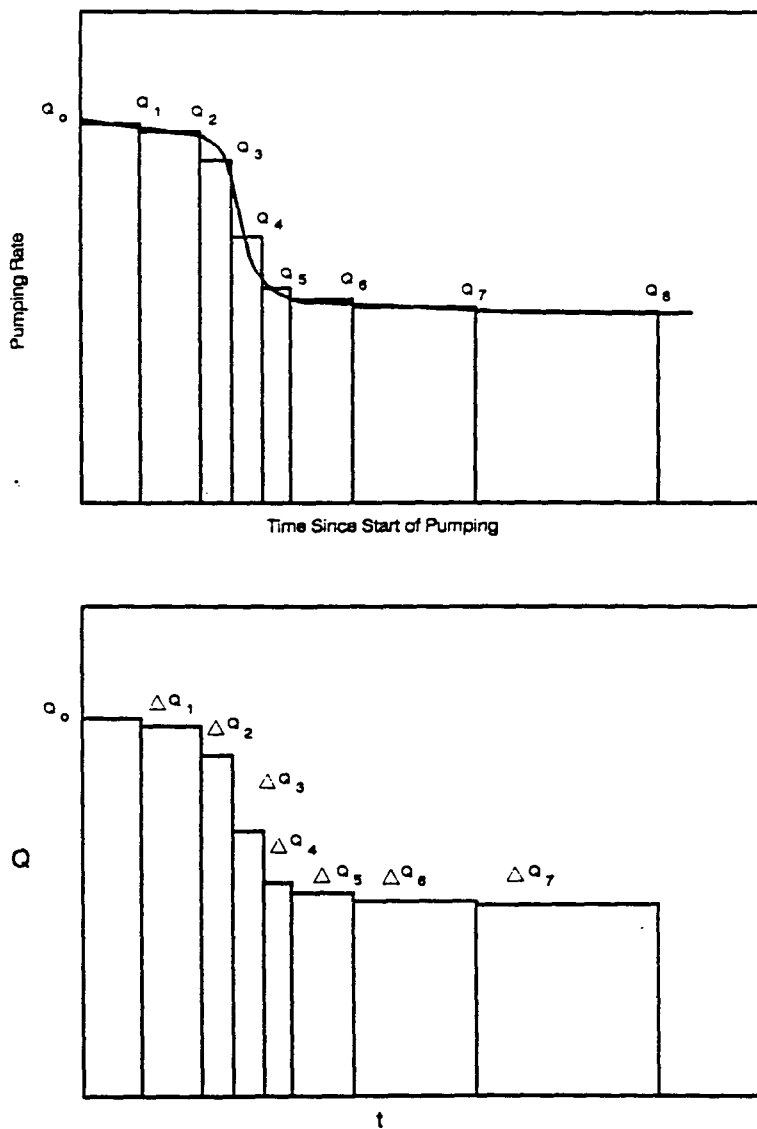


Figure 1. Nomenclature for continuously varying pumping rate

$$s(r, t) = \frac{Q_0}{4\pi T} W(u_0) + \frac{\Delta Q_1}{4\pi T} W(u_1) + \dots + \frac{\Delta Q_m}{4\pi T} W(u_m) \quad (9)$$

where

$$u_j = \frac{r^2 S}{4T(t-t_j)}, \quad (10)$$

$$\Delta Q_i = Q_i - Q_{i-1} \quad (11)$$

and t_j is the time since the start of the pumping rate Q_j , and t is the time since pumping began. This approach is valid because the equation (8) is a linear function of the pumping rate.

Jacob correction method

In an unconfined aquifer, the thickness of the saturated zone diminishes during the process of pumping, therefore This solution can not be directly applied. It was suggested by Jacob (1963) that "If the Theis graphical method is used for determining the hydraulic constants of an aquifer under water-table conditions, the observed drawdown should be corrected for the decrease in saturated thickness. This is especially true if the drawdown is a large fraction of the original saturated thickness, ...". The correction method was developed by Jacob by comparing the Thiem equations (Bear, 1979) for a confined aquifer and an unconfined aquifer.

According to Darcy's law, the equation for the steady radial flow to a well in a confined aquifer is

$$Q_w = -2\pi r T \frac{\partial s}{\partial r} \quad (12)$$

By integrating equation (12) between any two distances r_1 and $r_2 (> r_1)$, we obtain

$$s(r_1) - s(r_2) = \left(\frac{Q_w}{2\pi T} \right) \ln \left(\frac{r_2}{r_1} \right) \quad (13)$$

Equation (13) is called the Thiem equation.

Based on Dupuit's approximation, the Thiem equation for modeling the steady radial flow to a well in an unconfined aquifer is

$$K = \frac{Q_w \ln \left(\frac{r_2}{r_1} \right)}{\pi (h_2^2 - h_1^2)} \quad (14)$$

where h = the height of the water table above an impervious bottom, (L), and K = hydraulic conductivity, (L/T).

Jacob rewrote equation (14) as

$$Km = \frac{2mQ_w \ln \left(\frac{r_2}{r_1} \right)}{2\pi (h_2^2 - h_1^2)} = \frac{Q_w \ln \left(\frac{r_2}{r_1} \right)}{2\pi \left[\left(\frac{h_2^2}{2m} + \frac{m}{2} \right) - \left(\frac{h_1^2}{2m} + \frac{m}{2} \right) \right]} \quad (15)$$

where m = the initial thickness of the saturated zone, (L).

Substituting $s = m - h$ into equation (15) gives

$$Km = \frac{Q_w \ln\left(\frac{r_2}{r_1}\right)}{2\pi \left[\left(s_1 - \frac{s_1^2}{2m}\right) - \left(s_2 - \frac{s_2^2}{2m}\right) \right]} \quad (16)$$

$$Km = \frac{Q_w \ln\left(\frac{r_2}{r_1}\right)}{2\pi (s'_1 - s'_2)} \quad (17)$$

$$s' = s - s^2/2m \quad (18)$$

where s' is called the corrected drawdown, and Km is defined as the initial transmissivity, also denoted as T' . As a result, equation (17) has the same form as equation (13).

By using the concept of the corrected drawdown, Jacob rearranged the governing equation of unsteady flow in an unconfined aquifer into a similar form of the governing equation for the confined aquifer condition. Based on Dupuit's assumptions, the second-order differential equation governing the radial flow of water in an unconfined aquifer is (Bear, 1979)

$$Kh \left[\left(\frac{\partial^2 h}{\partial r^2}\right) + \left(\frac{1}{r}\right) \left(\frac{\partial h}{\partial r}\right) \right] = S_y \left(\frac{\partial h}{\partial t}\right) \quad (19)$$

Substituting $(m-s)$ for h in equation (19), yields

$$Km \left[\left(\frac{\partial^2 s'}{\partial r^2}\right) + \left(\frac{1}{r}\right) \left(\frac{\partial s'}{\partial r}\right) \right] = \left[\frac{m}{(m-s)}\right] S_y \left(\frac{\partial s'}{\partial t}\right) \quad (20)$$

which can be rewritten as

where $T' = Km =$ initial transmissivity and $S'_y = S_y m / (m-s) =$

$$T' \left[\left(\frac{\partial^2 s'}{\partial r^2} \right) + \left(\frac{1}{r} \right) \left(\frac{\partial s'}{\partial r} \right) \right] = S'_y \left(\frac{\partial s'}{\partial t} \right) \quad (21)$$

apparent storativity.

Equation (21) is equivalent to equation (1), the governing equation for radial flow to a well in a confined aquifer. If s is much smaller than m , S'_y can be considered essentially constant, and treated as one approximate solution of S_y . Then by the application of the graphical method of the Theis solution to the corrected drawdown (s'), the value of T' and the approximate value of S_y can be estimated for an unconfined aquifer; the hydraulic conductivity is given by $K = T'/m$.

When applying the Jacob correction method, one should be aware of the following limitations;

(i) This method in effect heavily relies on the Dupuit's assumptions and will fail when vertical gradients become significant.

(ii) Drawdown data collected during the early time of pumping may not conform to this method, since the vertical flow may be significant during the early pumping.

FIELD SITE AND EXPERIMENT PROCEDURE

Field Site

The study field is located about 7.5 miles west of Ames and 0.5 mile south of highway I-30 at the Agricultural Engineering-Agronomy Farm near Boone city, Iowa. A U.S.G.S. topographic map (Boone East, Iowa) of the study field is given in Figure 2. Figure 3 shows the approximate location of the test site. The ground surface of the test site is covered by short grass and has an average gradient of about 3%. The soil profile of the area consists of oxidized glacial till deposit underlain by an unoxidized layer. Wang (1990) performed triaxial permeameter tests to estimate hydraulic conductivity in the vertical direction using soil samples from the same study area. The results suggest that the vertical hydraulic conductivity of the oxidized till is at least 1 order of magnitude higher than that of unoxidized till. Therefore, it is believed that the unoxidized till layer can be treated as an aquitard and the oxidized till layer acts as an unconfined aquifer. According to the result of ground water monitoring, the water table usually is within the depth of 1.5' to 3.5' from the ground surface and the flow gradient and direction is about the same as those of the ground surface.

Sixteen wells were installed in three radial lines

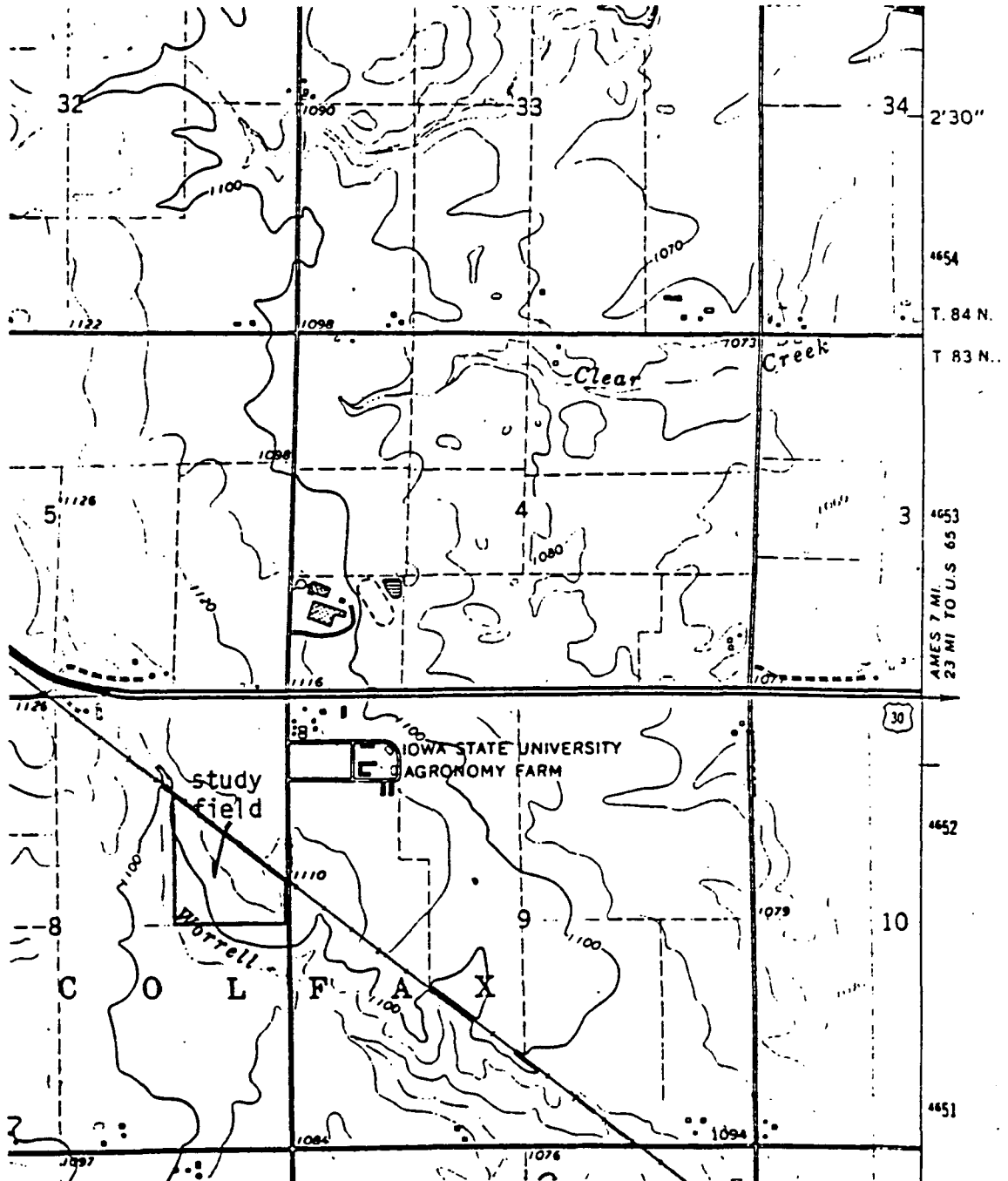


Figure 2. Location of the study field

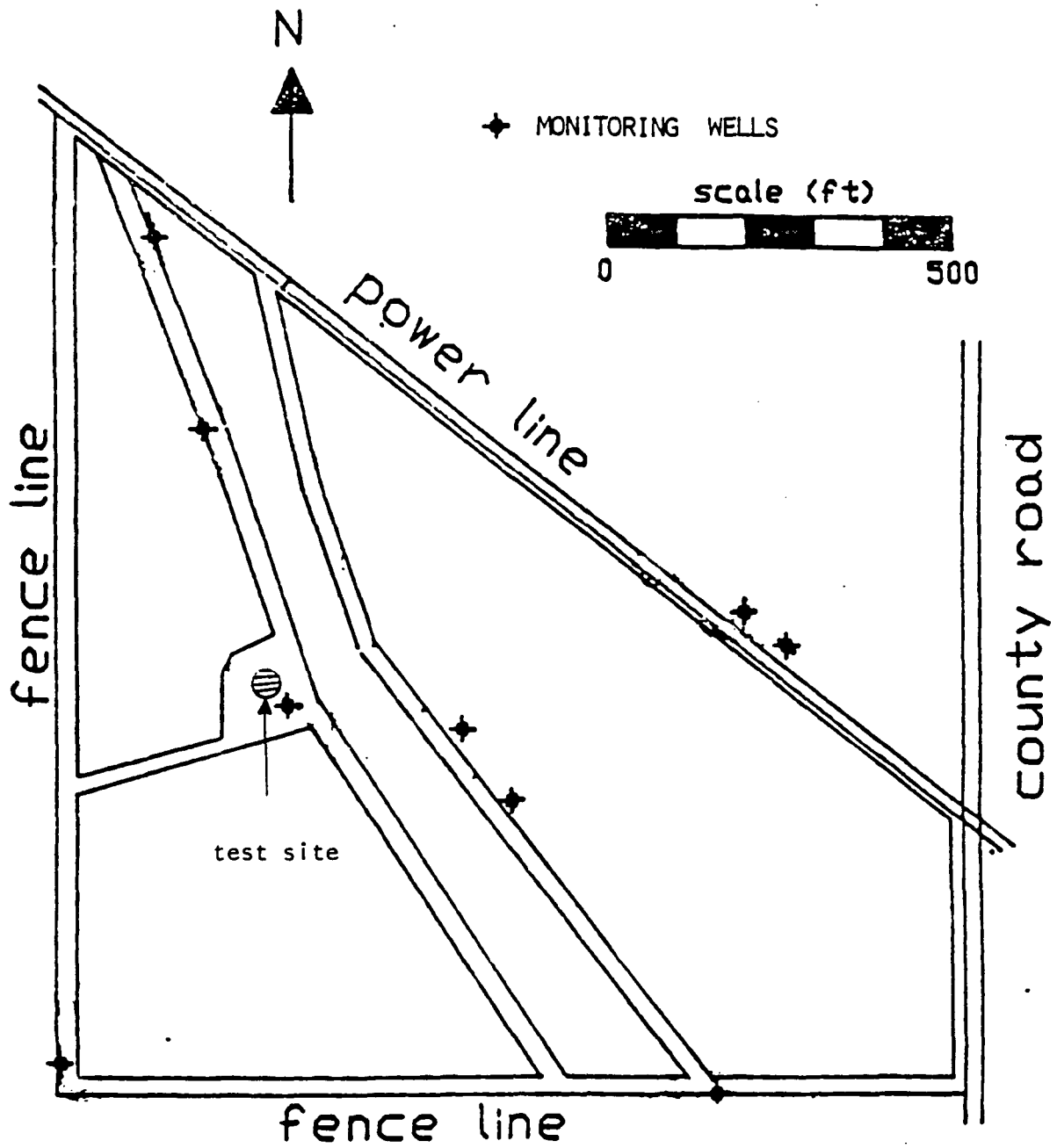


Figure 3. Location of the test site

centered at the pumping well with approximately a 120 degree angle between the radial lines. At approximately 3, 6, 9, 12 and 20 feet from the pumping well, an observation well was installed in each line. A plan view of the well layout is shown in Figure 4, along with the designation used for each well and the gradients and directions of the ground surface and the ground water flow. The well boreholes were installed by a machine drill with a four-inch diameter solid stem auger. All of the wells are about 15' deep. The well material is two-inch diameter schedule 40 PVC pipe connected to a ten-foot long screen with 0.01-inch-wide slots. The ten-foot screens were packed with gravel from the bottom to approximately one foot above the screen. The wells were finished with a bentonite clay pack from top of the gravel pack to about 2 inches below the top of the well. A vertical cross-section view of a representative well is shown in Figure 5.

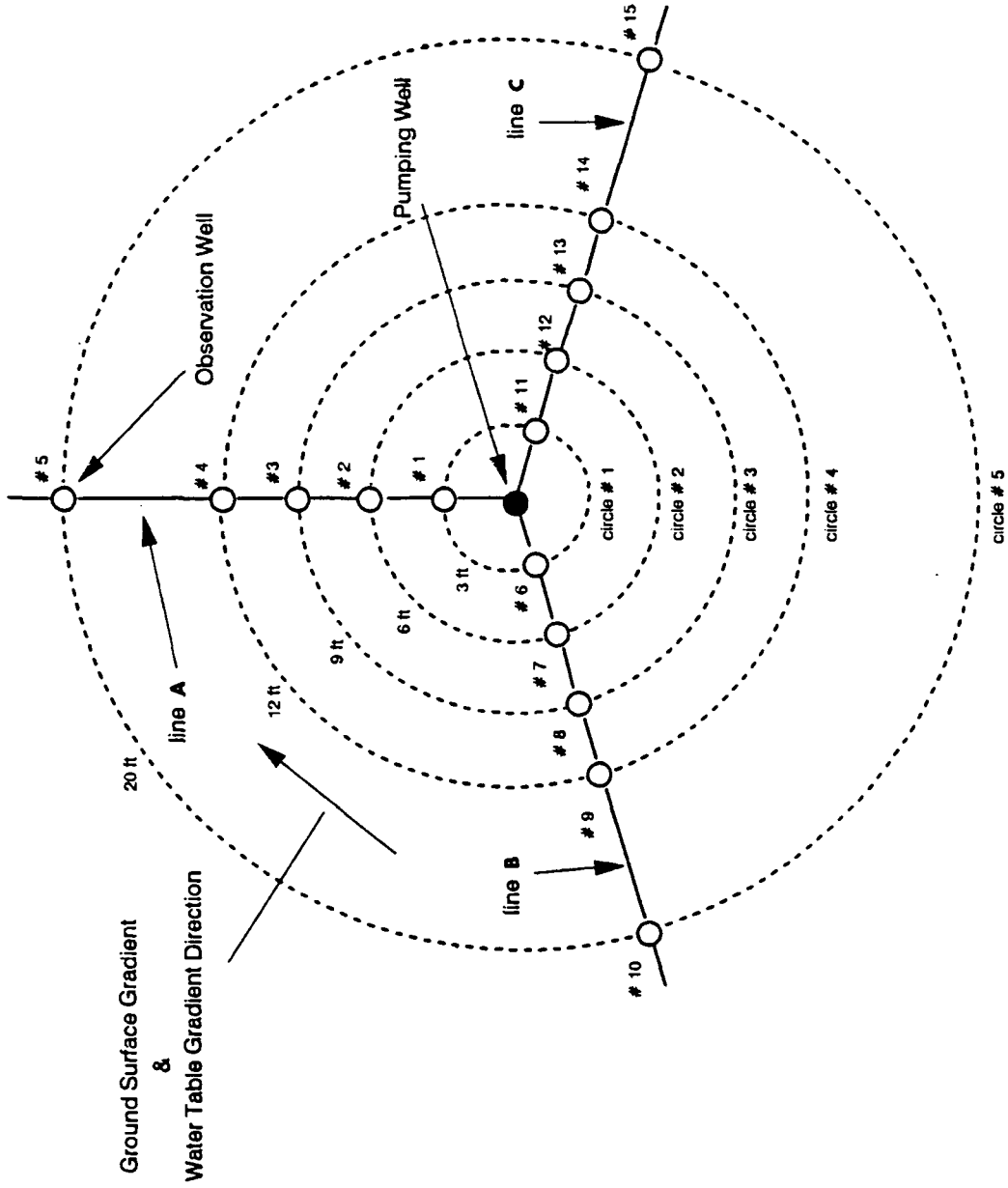


Figure 4. Plan view of the well layout

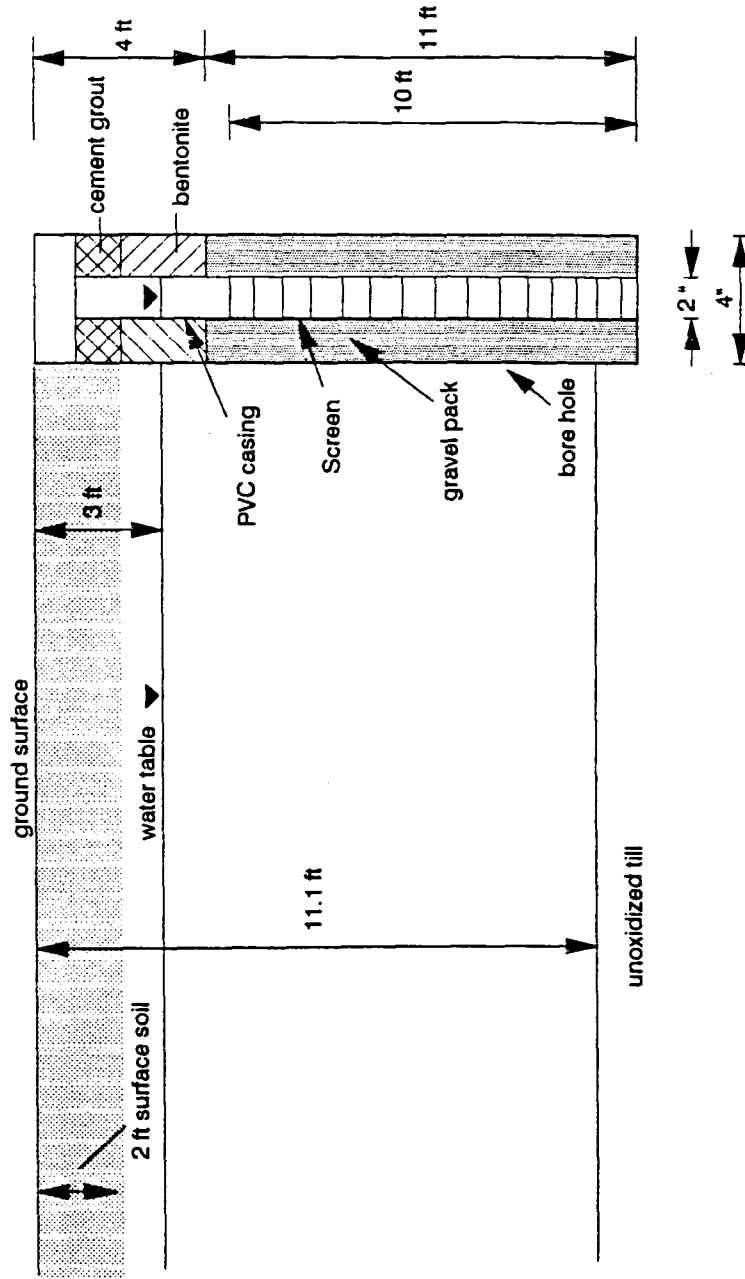


Figure 5. Vertical cross-section view of a representative well

Experiment Procedure

This experiment includes two phases; field test and data analysis.

Field test

During the well construction, soil samples were taken by shelly tubes with a length of 2.5' from each well at two different depths: 5' to 7.5' and 10' to 12.5' from the ground surface. The shelly tubes were sealed by wax and duct tape right after the sampling. Before the soil character tests, the shelly tubes were cut into three equal sections and were sealed again. The tests of determining particle size distribution, particle density, and bulk density of the soil samples were conducted according to Das (1988). From the soil samples taken from 10' to 12.5', the transition zone of the oxidized and unoxidized till was distinguished by color.

After the construction of wells, well development work was done by repeatedly pumping out water, pouring water in, and applying air pressure until the water in the well was fairly clean. Site survey and ground water table monitoring were also performed to determine the gradients and directions of the ground surface and ground water flow. Then, the site is ready for the pumping test.

Two constant-head pumping tests were conducted in the test site. The first one, with three feet of constant drawdown in the pumping well, was performed on July, 31, 1990

and the duration of pumping was about 9.5 hours. The second one, with five feet of constant drawdown in the pumping well, was performed on August, 6, 1990 and the duration of pumping was about 24 hours. Test #1 had a thicker saturated zone and a larger natural drawdown rate than test #2. The different conditions between the two pumping tests are summarized in Table 2.

Immediately prior to the tests, the initial depths from the ground surface to the water table in all of the wells were recorded. Then the average initial thickness of the saturated zone was determined by subtracting the initial average depth to the water table from the average depth of the transition zone(11.1'). The transition zone will be discussed in the soil character test section. The test site natural drawdown rate was determined by the water table level data recorded one day before the beginning of the test and the data recorded just before the test was conducted. It was assumed that the average rate of the natural drawdown during the pumping test is the same as that of the 24 hours preceding the test.

Preparation prior to the beginning of the pumping test includes: connecting two 12-foot rubber tubings to a peristaltic pump with two pumping heads, using a steel rod to support the tubings and lower the tubings from the top of the pumping well to the desired depth, and starting a generator

Table 2. The different conditions between the two pumping tests

	Test #1	Test #2
Pumping time	9.5 hr	24 hr
Initial average depth to water table	2.24 ft	2.90 ft
Initial average thickness of the saturated zone	8.86 ft	8.20 ft
Constant drawdown in the pumping well	3.04 ft	4.92 ft
Natural drawdown rate	0.23 ft/day	0.095 ft/day

to provide electrical power (see Figure 6). The pumping tests were started by running the pump at its full speed (43 ml/sec.). Then the pumping rates were measured with two graduated cylinders as frequently as necessary, while, water levels were manually measured with the aid of an electric probe. Early in the test the water levels in the wells near the pumping well were measured more often due to rapid drawdown response. As the test progressed, measurement periods were adjusted based on the response observed from previous measurements.

Data analysis

To account for the requirement of discrete changes based on the concept of super-position principle, the observed continuously decreasing pumping rates were divided into many intervals. The interval durations are inversely proportional

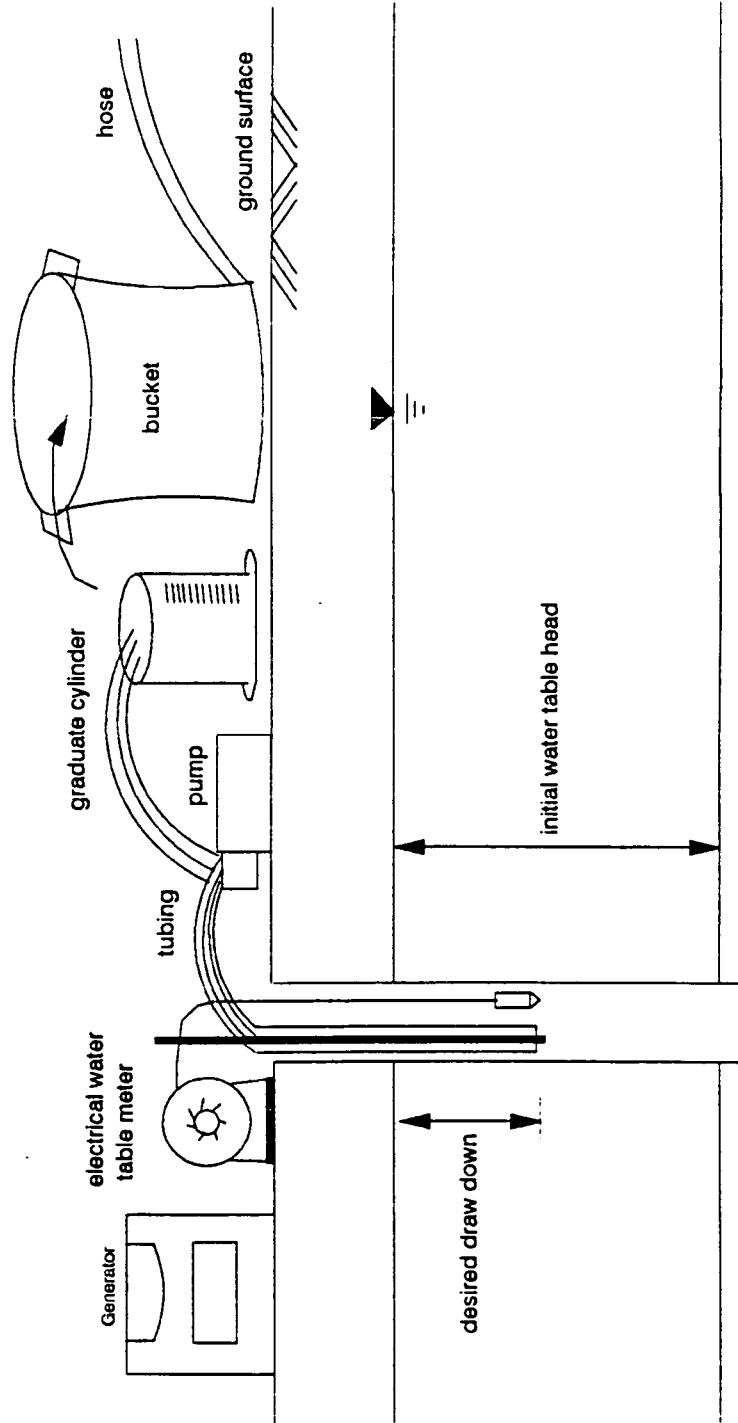


Figure 6. Schematic diagram of the equipment layout

to the rate of change of pumping.

The observed drawdown response data were corrected first by subtracting the natural drawdown, then applying the Jacob correction method, equation (18). Finally, the super-position Theis solution, equation (9) was applied to the adjusted data.

The method used in determining T' and S'_y along with super-position Theis solution is called a least squares fitting method. A theoretical drawdown curve can be obtained by assigning a set of T' and S'_y to the super-position Theis solution. The method of least squares is used as the criteria for determining the best fit. Therefore, the target T' and S'_y are those values which can minimize the sum of squared differences between the observed and predicted corrected drawdown generated by super-position Theis solution, which can be written as,

$$\text{minimize } F(T', S'_y) = \sum_{i=1}^n (S'_{o}(r_i, t_i) - S_t(r_i, t_i, T', S'_y))^2 \quad (22)$$

where S'_o is the observed drawdown data corrected by both natural drawdown and Jacob correction, S_t is the theoretical drawdown predicted by super-position Theis solution, and n is the number of data points.

RESULTS AND DISCUSSION

Soil Character Test

Results

Because of sampling difficulties, soil samples were not obtained from well #3 at both depths; 5'-7.5' and 10'-12.5', and well #5 at the depth; 10'-12.5'. Shelby tubes were found empty after pulling out from the above locations. As a consequence, the information about the depth of the transition zone for well #3 and well #5 and the soil character of well #3 are not available.

The transition zone which is located between the oxidized till and the unoxidized till was very clear visually and was situated at a depth between 10.02' and 12.35'. The results are listed in Table 2. The transition zone in line B in Figure 4 was relatively flat, between 10.02' to 10.34', but fluctuated in line A and line C. The average depth of the transition is 11.1 feet. The results were also plotted in Figure 7.

The soil samples taken from the oxidized zone are mainly yellow-brown soil. Root holes were found in the soil samples taken from depth 5.8' to 6.7', but not in the soil samples taken from a depth greater than 10'. Some roots were found in the root holes, but most of the root holes were empty. The directions of the root holes were random. Fractures

Table 3. The depth of transition zone

Well No.	1	2	4	6	7	8	9
Depth (ft)	11.42	12.35	11.37	10.02	10.3	10.29	10.34
Well No.	10	11	12	13	14	15	P ^a
Depth (ft)	10.24	11.20	11.42	11.67	11.66	12.08	10.89

^aP: the pumping well

characterized by reddish oxidized materials were found in samples taken from oxidized till and most were oriented vertically. The unoxidized till was uniform and consisted of dark gray soil.

Soil character tests were mainly performed on oxidized soil samples from the depth between 5.8' and 6.7'. Two oxidized soil samples from the depth between 11.7' and 12.5', and two unoxidized soil samples from depth between 10.8' and 11.7' were also analyzed.

The particle densities of the oxidized till and unoxidized till were the same, 2.69 ± 0.01 g/cm³. The results of the bulk density tests are shown in Table 4 and indicate that the oxidized till has a slightly lower density than the unoxidized till. The average bulk densities of the oxidized till and the unoxidized till were 1.84 g/cm³, and 1.91 g/cm³ respectively.

The results of the particle size distribution tests are shown in Table 5 and by points in Figure 8. There is no clear

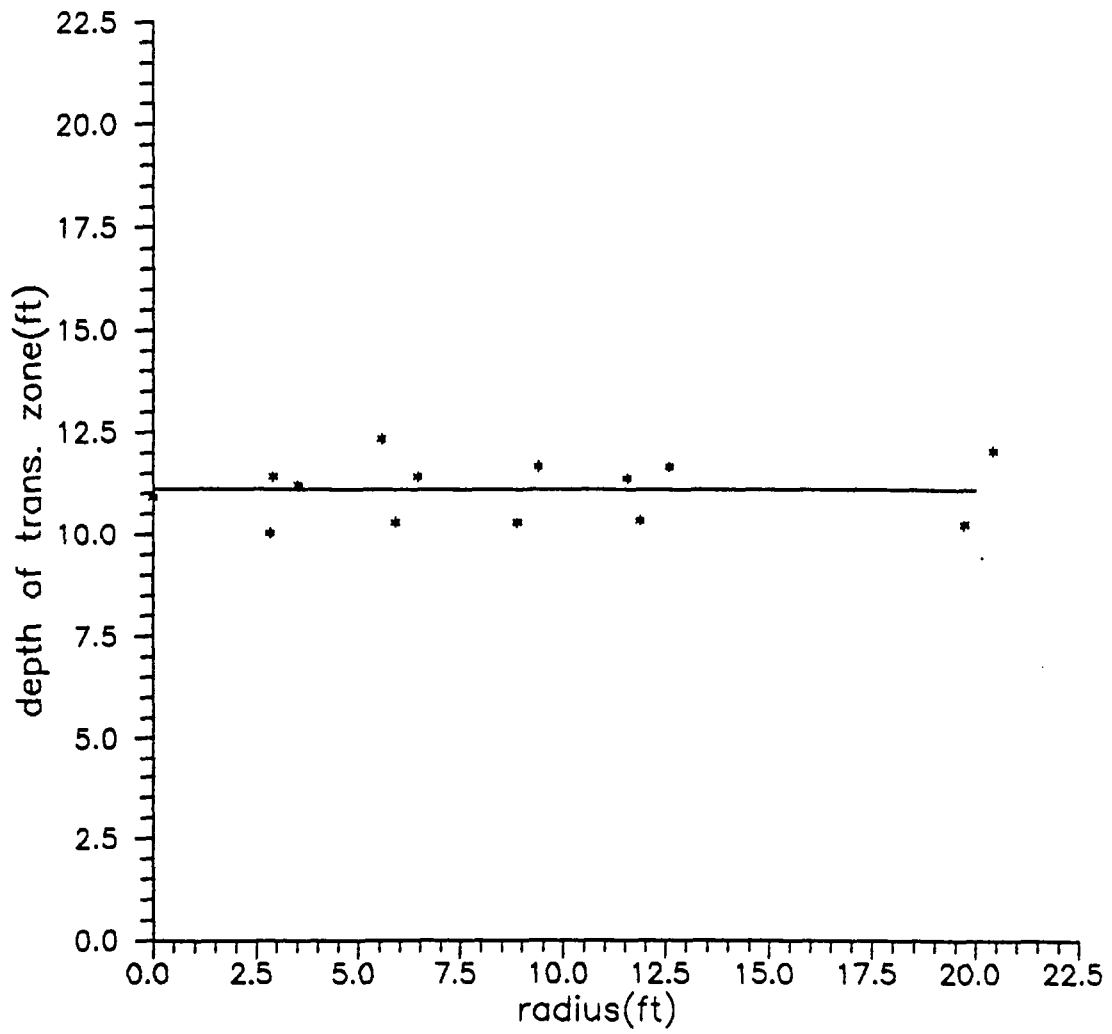


Figure 7. Depth of transition zone versus radial distance

Table 4. Result of soil character tests (A)

Well #	depth ^a ft	weathered	bulk density g/cm ³	porosity %
1	5.8-6.7	yes	1.83	32.0
2	5.8-6.7	yes	1.82	32.3
4	5.8-6.7	yes	1.85	31.2
5	5.8-6.7	yes	1.89	29.7
6	5.8-6.7	yes	1.79	33.5
7	5.8-6.7	yes	1.85	31.2
8	5.8-6.7	yes	1.83	32.0
9	5.8-6.7	yes	1.83	32.0
10	5.8-6.7	yes	1.83	32.0
11	5.8-6.7	yes	1.85	31.2
12	5.8-6.7	yes	1.82	32.3
15	5.8-6.7	yes	1.84	31.6
P	5.8-6.7	yes	1.84	31.6
12	11.7-12.5	yes	1.86	30.9
15	11.7-12.5	yes	1.86	30.9
7	10.8-11.7	No	1.90	29.4
9	10.8-11.7	No	1.91	29.0
average			1.85	31.3
standard deviation			0.03	1.10

^aDepth: measured from the ground surface

Table 5. Result of soil character tests (B)

Well #	depth ^b ft	weathered	particle size distribution ^a			
			gravel %	sand %	silt %	clay %
1	5.8-6.7	yes	2.6	58.2	27.9	11.4
2	5.8-6.7	yes	2.4	57.2	28.6	11.8
4	5.8-6.7	yes	4.6	51.4	31.6	12.4
5	5.8-6.7	yes	3.3	54.5	32.1	10.1
6	5.8-6.7	yes	3.4	52.4	34.1	10.1
7	5.8-6.7	yes	2.9	54.4	31.9	10.8
8	5.8-6.7	yes	3.3	52.8	31.5	12.4
9	5.8-6.7	yes	3.0	57.1	30.1	9.8
10	5.8-6.7	yes	3.5	56.1	28.0	12.4
11	5.8-6.7	yes	3.1	54.9	29.7	12.4
12	5.8-6.7	yes	3.2	55.7	31.3	9.8
15	5.8-6.7	yes	1.5	55.4	33.2	9.8
P	5.8-6.7	yes	2.8	55.2	31.0	11.1
12	11.7-12.5	yes	5.0	52.7	35.5	6.8
15	11.7-12.5	yes	4.3	48.8	38.2	8.8
7	10.8-11.7	No	4.7	51.9	31.3	12.1
9	10.8-11.7	No	5.6	50.2	34.1	10.1
average			3.5	54.1	31.8	10.7
standard deviation			1.0	2.5	2.6	1.5

^aParticle classification: (USDA classification)

gravel: >2 mm, sand: 2-0.05 mm

silt: 0.05-0.002 mm, clay: <0.002 mm

^bDepth: measured from the ground surface

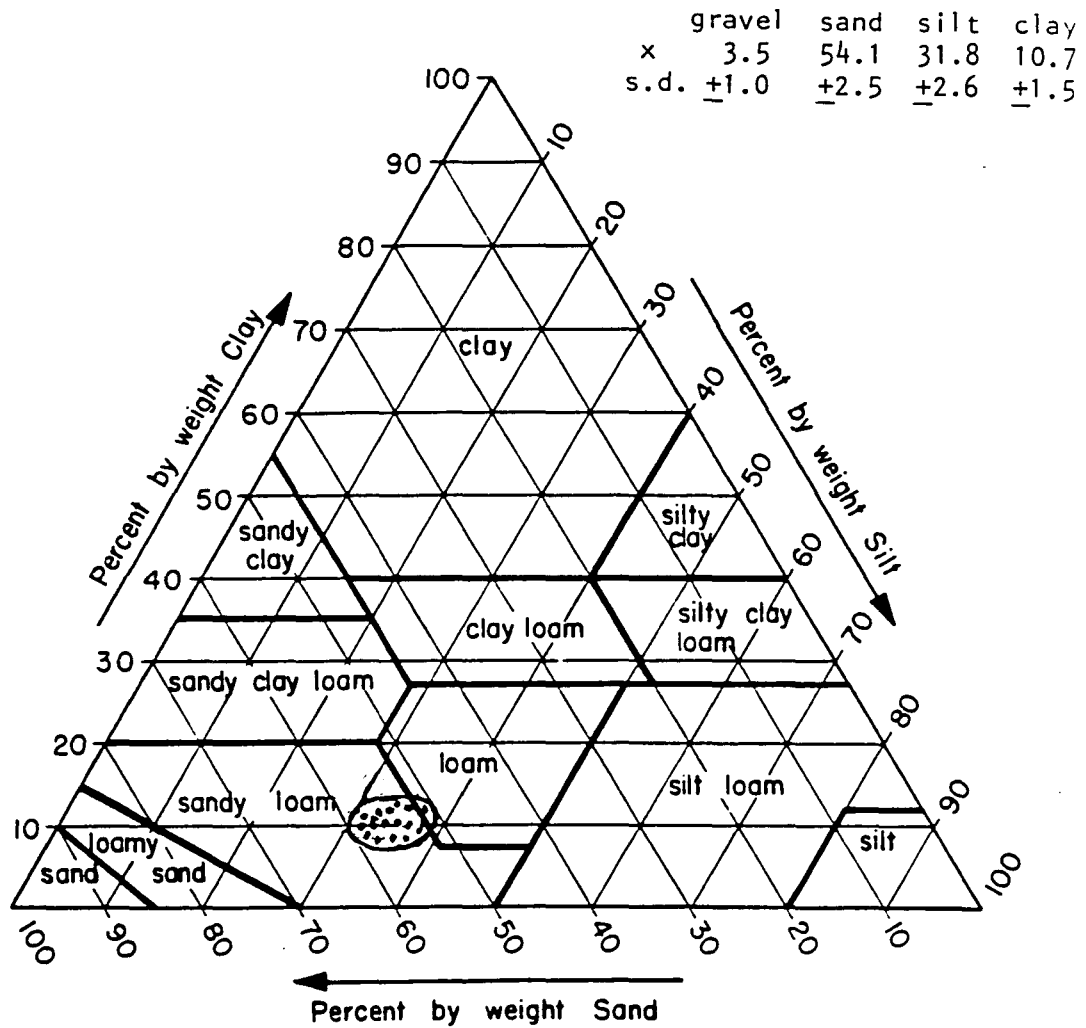


Figure 8. Textural data for the test site

difference between the oxidized till and the unoxidized till. The soil is uniform and classified as sandy loam, close to loam. The average percentage of particle size are: clay (<0.002 mm diameter) 10.7% (S.D.= ± 1.5), silt (0.002-0.05 mm) 31.8% (S.D.= ± 2.6), sand (0.05-2.00 mm) 54.1% (S.D.= ± 2.5), and gravel (>2.00 mm) 3.5% (S.D.= ± 1.0).

Discussion

It is clear that the bottom of the oxidized till layer is not flat and horizontal. However, for practical purposes, it is assumed that the bottom of the oxidized till is flat and horizontal, and has an average depth, 11.1'. The error associated with this assumption is ignored.

Root holes and fractures may affect not only the bulk density, but also the hydraulic conductivity. It is recognized that fractures may dramatically increase the hydraulic conductivity. But, the knowledge about how the root holes affect the hydraulic conductivity is very limited.

Two pieces of evidences suggest that the till deposit at the test site consists of subglacial till. (i) The bulk density of this study area, 1.85 g/cm³, is close to the mean value of subglacial till density, 1.89 g/cm³, given by Lutenegger (1983). (ii) The soil in the test site was uniform in texture, a characteristic of subglacial till. In addition, Wang (1990), who did soil classification tests on the same field, also reached the same conclusion.

Constant-Head Pumping Test

Results of pumping test #1

Pumping rate and drawdown response With an initial pumping rate of 43 ml/sec., the water table in the pumping well fell 3.04 feet from its initial level to the desired constant depth in about five minutes. Before the water table reached the desired depth, the pumping rate was in the range of 43 ml/sec to 46.7 ml/sec. The pumping rate clearly started to decline when the water table reached the desired depth. At the end of pumping (9.5 hours of pumping), the pumping rate decreased to 12.5 ml/sec. Figure 9 graphs the curves of the pumping rate over time.

The curve of the pumping rate vs time was also plotted on a log-log scale diagram (Figure 10). From the log-log diagram, there is a linear relationship between $\log Q$ and $\log t$ after reaching the constant drawdown level, which is the same as the relationship predicted by Marino and Yeh(1972) for constant head recharge in unconfined aquifers. The linear best fit line is also plotted in Figure 10.

The drawdown, as measured in the observation wells, responded rapidly to the pumping. Within one minute, there was some drawdown observed in the observation wells three feet away from the pumping well. After one hour of pumping, the wells 20 feet from the pumping well had shown measurable drawdown. The drawdown response in the first 2.5 hours of

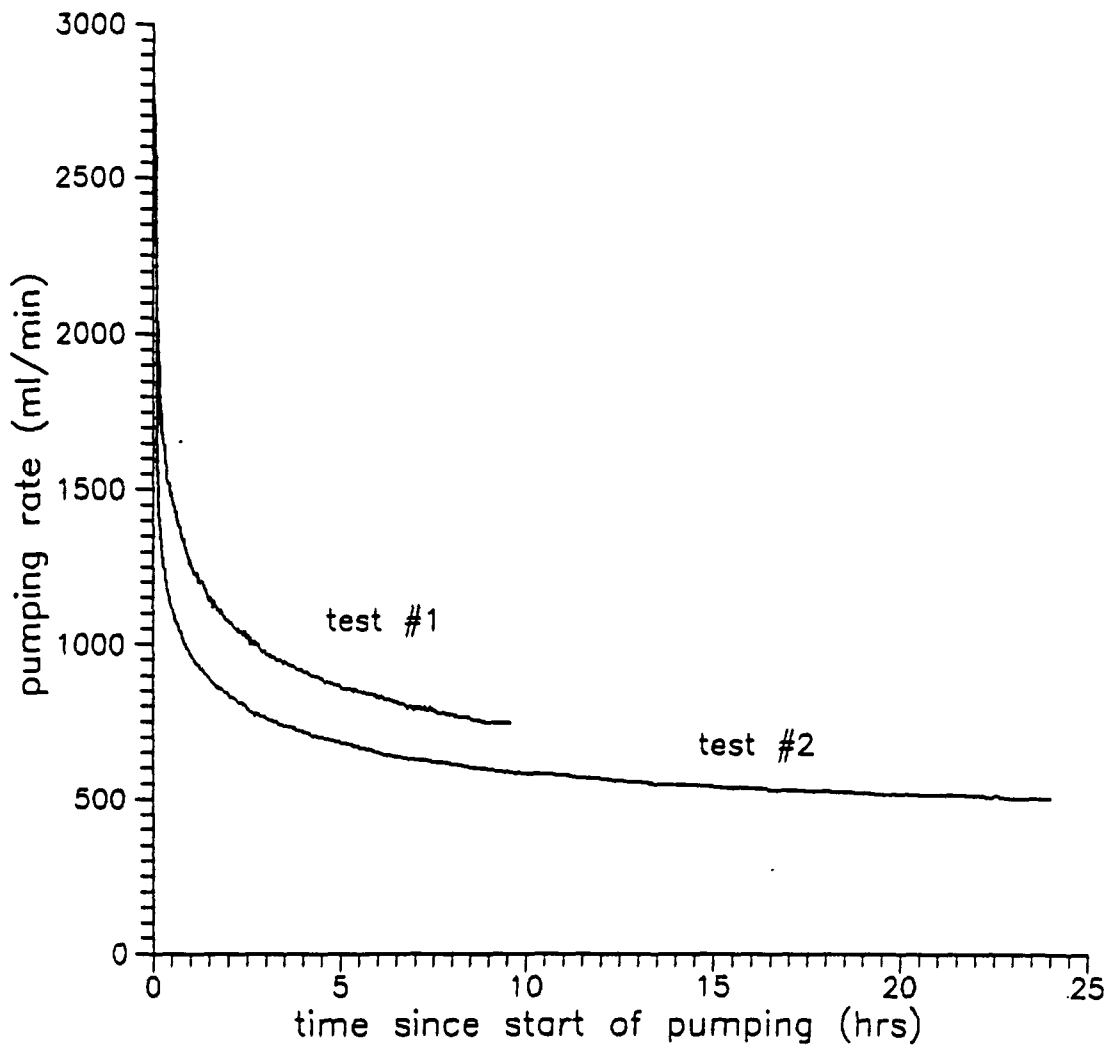


Figure 9. Test #1 & test #2, pumping rate versus time, in normal scale

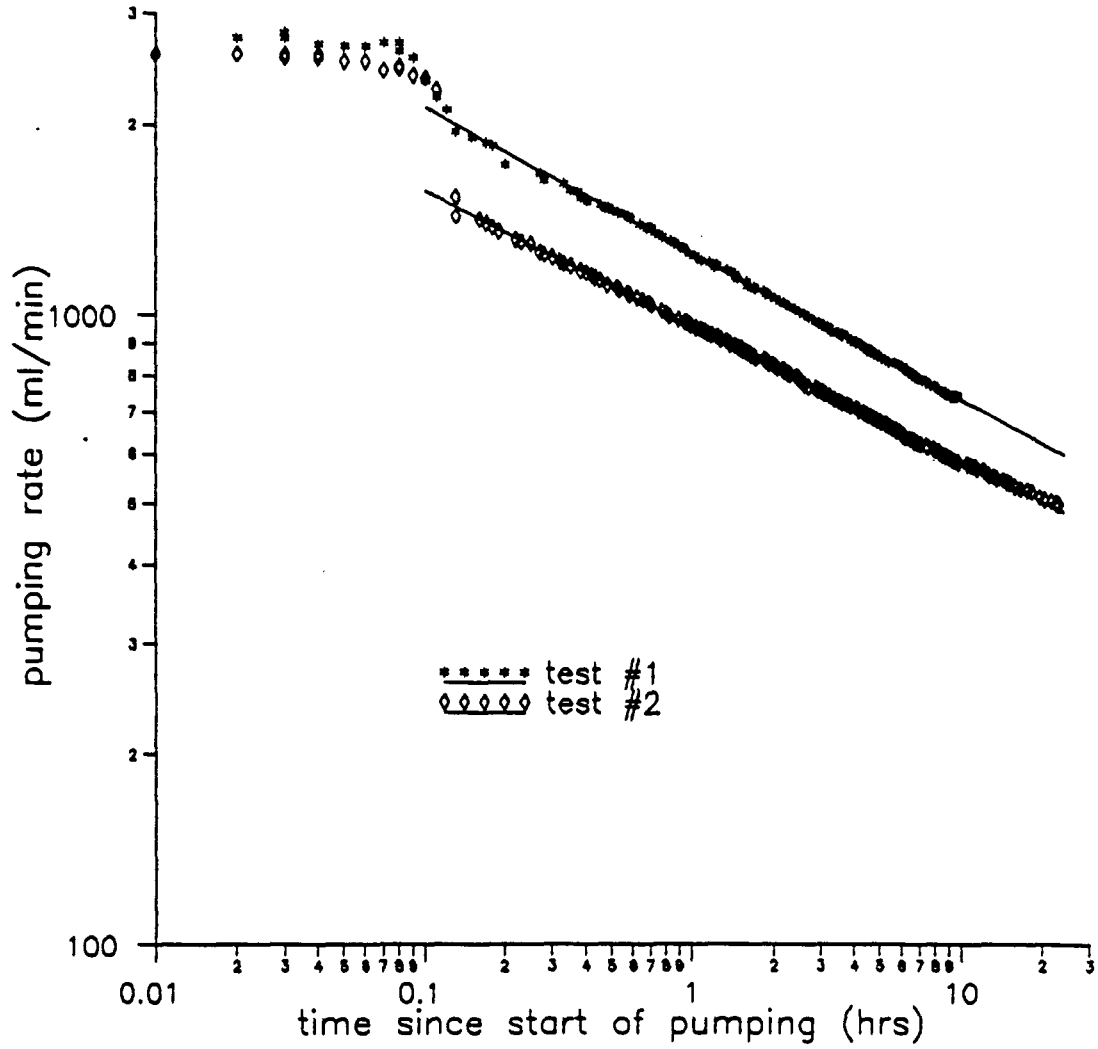


Figure 10. Test #1 & test #2, pumping rate versus time, in log-log scale

pumping are shown in Figures 11, 12, and 13. Each graph represents four observation wells placed on a line radiating from the pumping well (see previous test site description for exact placement). The curves of the drawdown response during the 9.5 hour pumping period for the observation wells located on each radial line are plotted in Figures 14, 15, and 16. From the drawdown response curves shown in Figures 14, 15, and 16, it is evident that the curves are fairly smooth considering the measurement error (± 0.01 ft) of the water table meter. The hydrologic parameters of the wells 20 feet from the pumping well could not be determined because it was uncertain if the low reading was due to measurement error or actual drawdown. Therefore, the drawdown data of the wells located 20 feet from the pumping well were not included in the analysis.

After nine and a half hours of pumping, the pumping rates and drawdown responses appeared fairly stable. In the last hour of pumping, the pumping rate fell only 10 ml/min. (760 ml/min. to 750 ml/min.) and in the last one and one half hours, the drawdown responses of all observation wells increased by 0.02 to 0.03 feet.

Hydraulic conductivity and specific yield The estimations of initial transmissivity and specific yield are based on the data of observed drawdown corrected by subtracting the natural drawdown and applying the Jacob

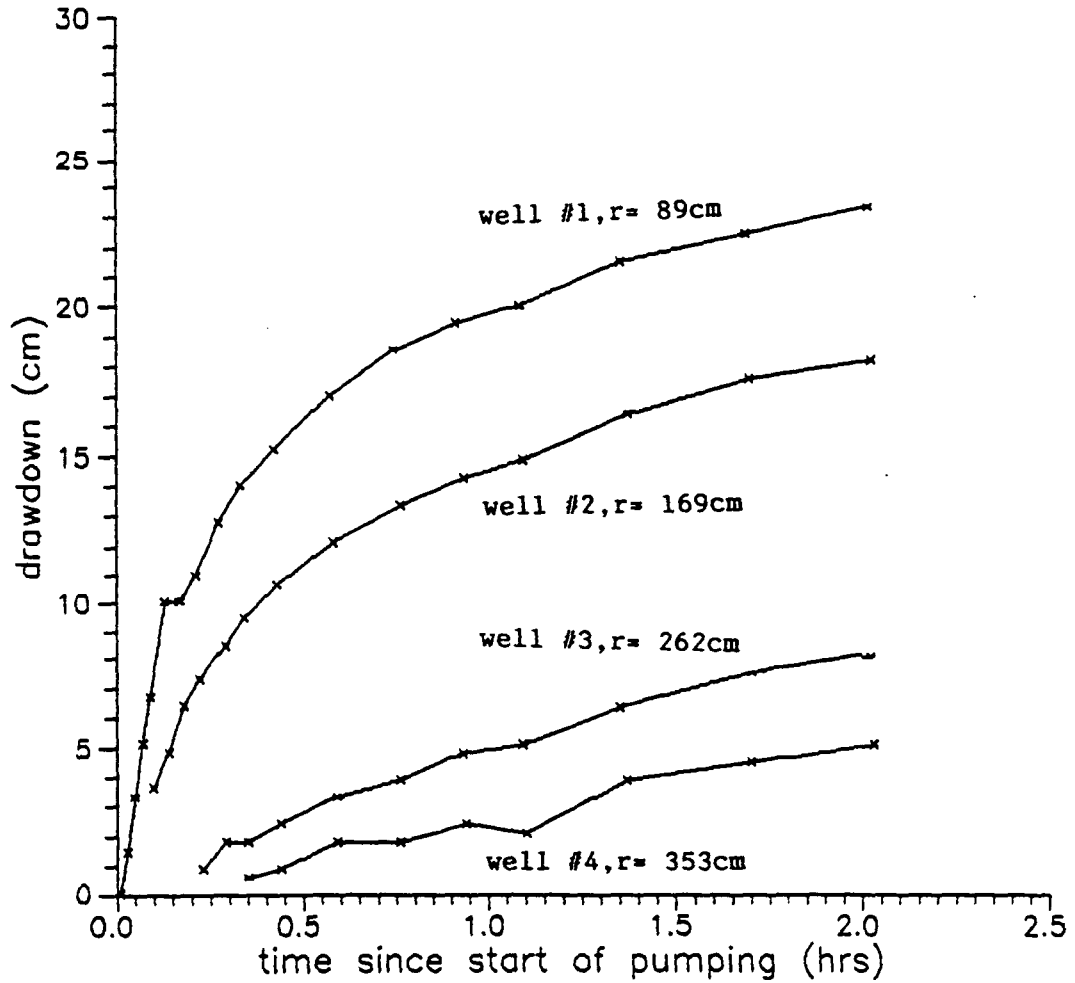


Figure 11. Test #1, drawdown response curves of wells on line A in the first 2.5 hours of pumping

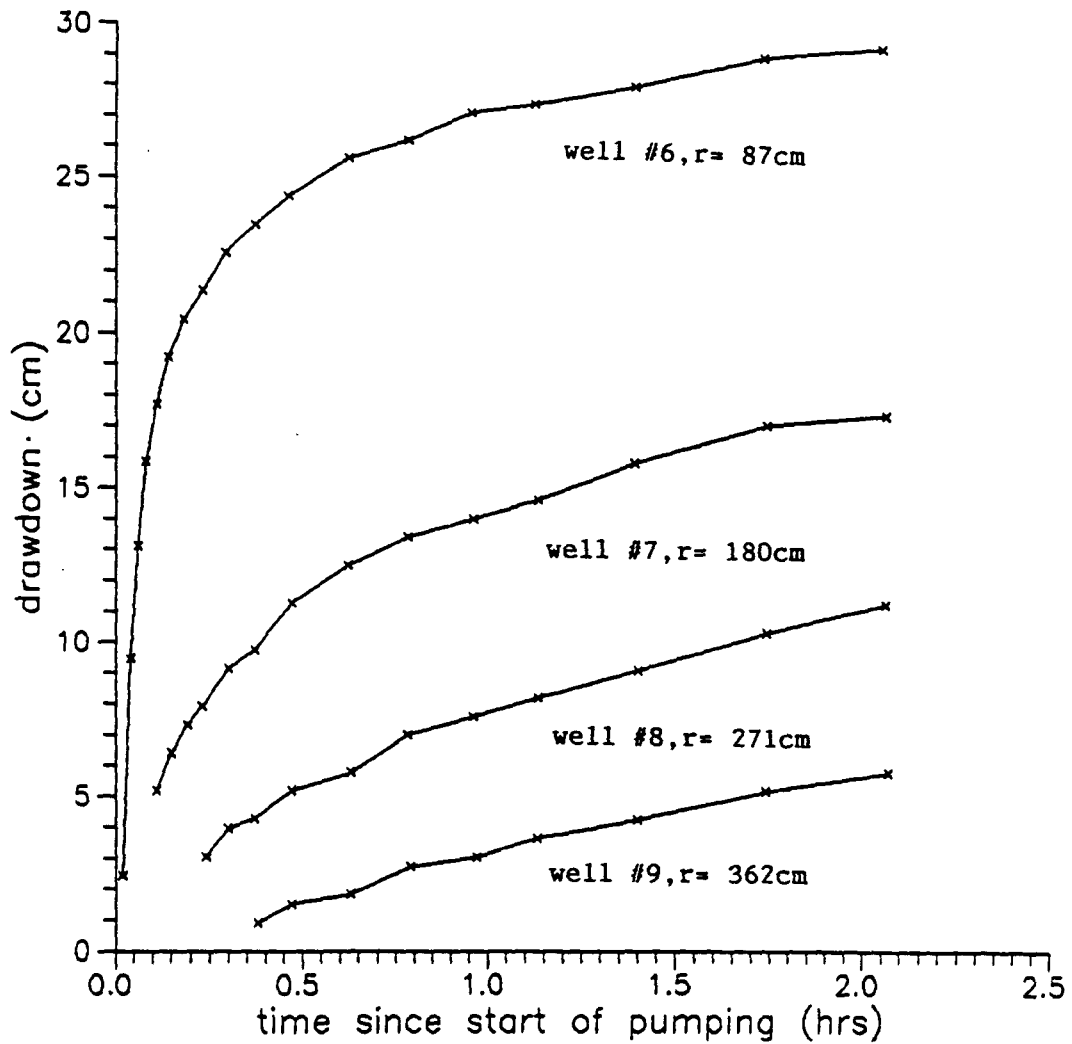


Figure 12. Test #1, drawdown response curves of wells on line B in the first 2.5 hours of pumping

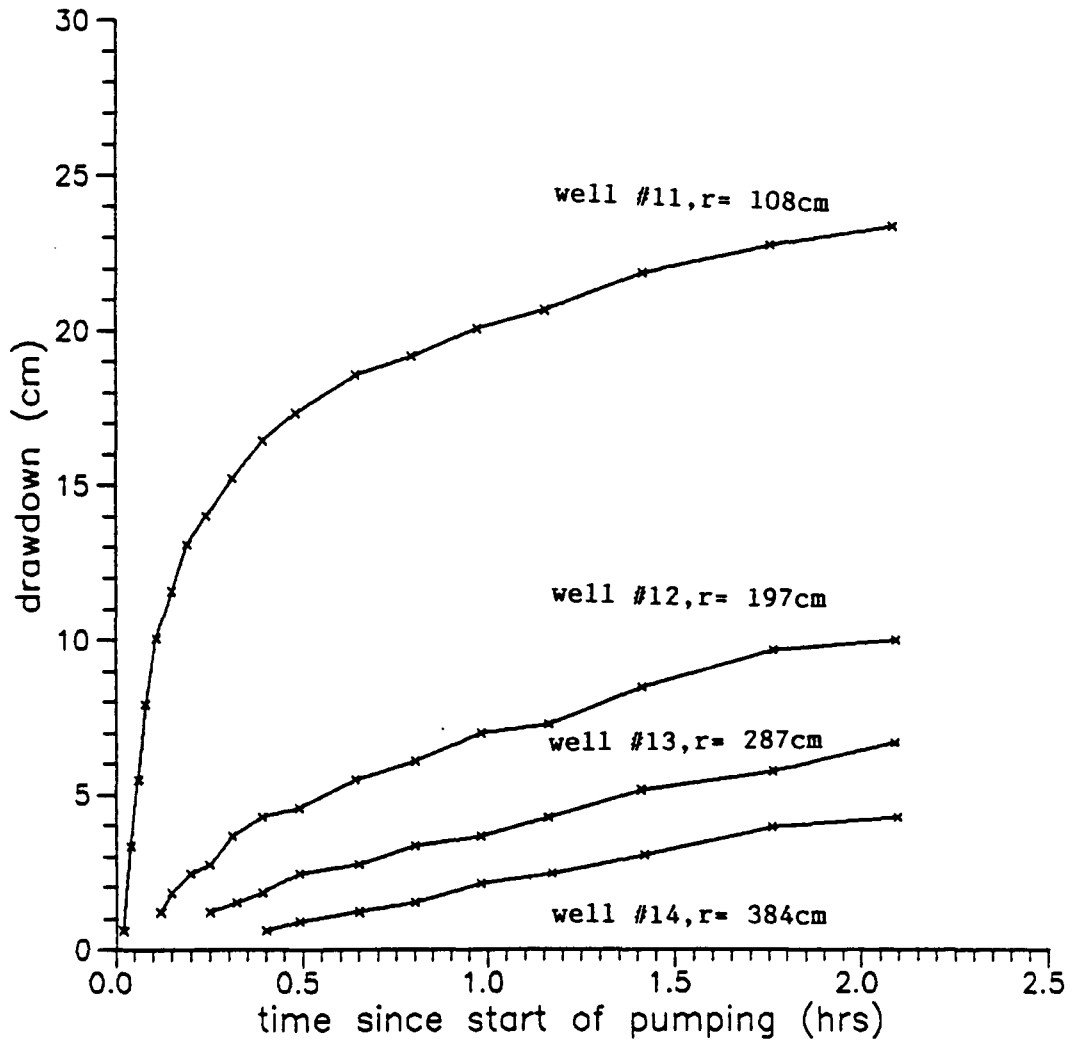


Figure 13. Test #1, drawdown response curves of wells on line C in the first 2.5 hours of pumping

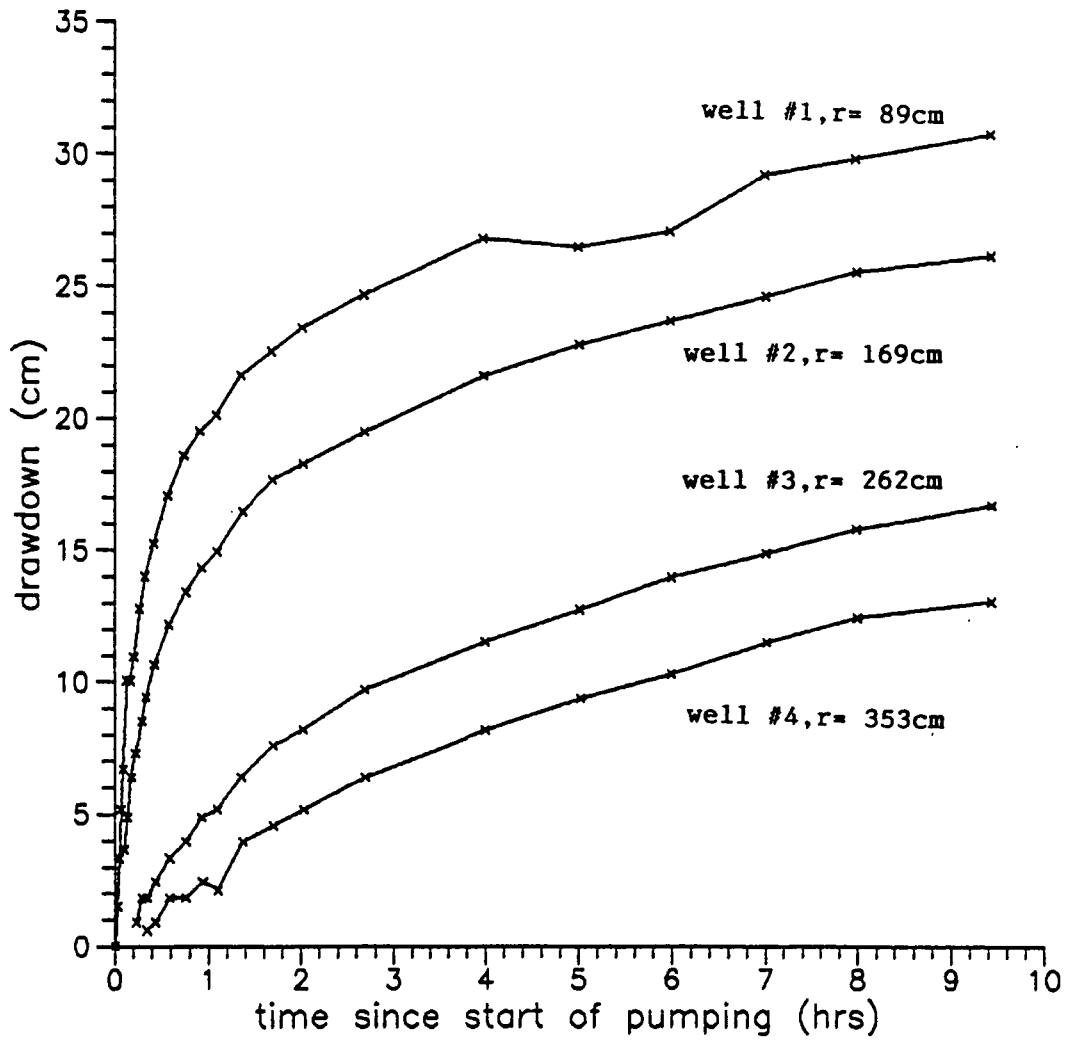


Figure 14. Test #1, drawdown response curves of wells on line A over the 9.5 hour pumping period

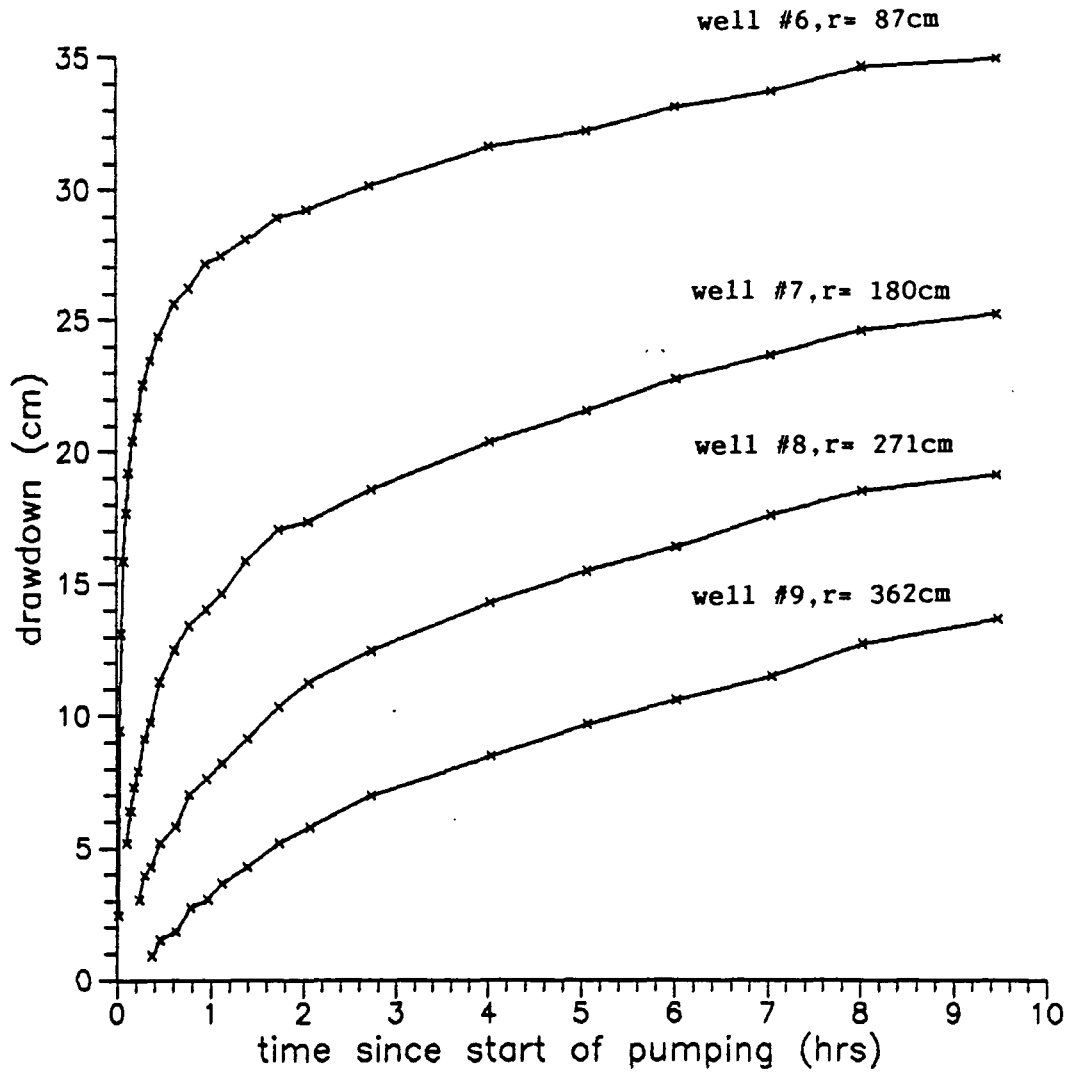


Figure 15. Test #1, drawdown response curves of wells in line B over the 9.5 hour pumping period

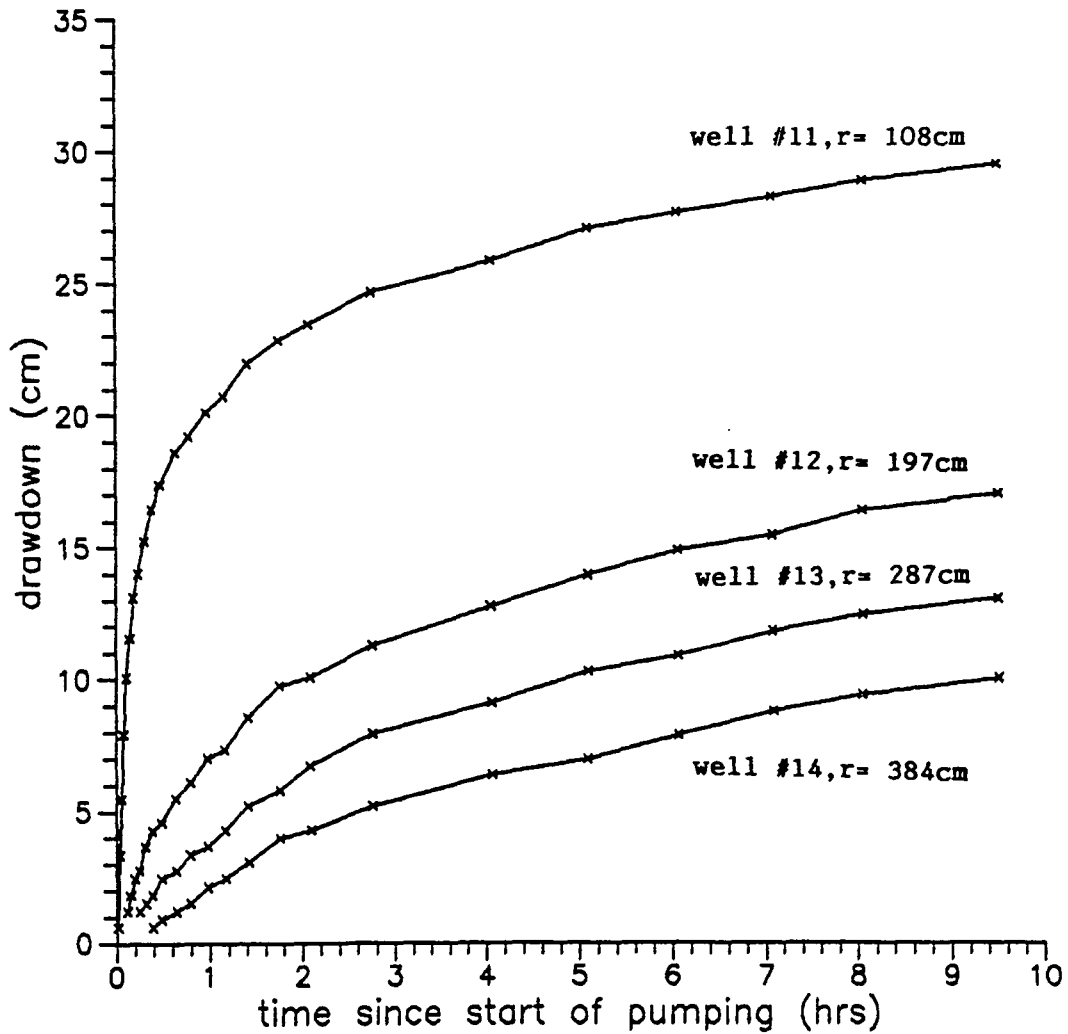


Figure 16. Test #1, drawdown response curves of wells in line C over the 9.5 hour pumping period

correction (18). As mentioned in the literature review, the initial drawdown period following the beginning of pumping may be affected by the vertical flow component and should therefore not be included in the data analysis. Vertical flow is not accounted for in the mathematical model. After several trials, it was determined that the drawdown data of the first two hours of pumping should be excluded in the least squares fitting. The initial transmissivity and specific yield for each individual well was estimated by applying the least squares estimation (22) to the adjusted drawdown data of each individual well. Here, equation (22) was fitted for each of the 12 observation wells. The results are shown in Table 6. The estimated hydraulic conductivities of each well were obtained by dividing the initial transmissivity by the initial thickness of the saturated zone (8.86 feet). The arithmetic mean hydraulic conductivity is 6.9×10^{-4} cm/s and the geometric mean is 6.8×10^{-4} cm/s. The arithmetic mean specific yield is 0.0286, while the geometric mean is 0.0276.

Another average hydraulic conductivity and specific yield were calculated to contrast with the average hydraulic conductivities and the specific yields obtained from the individual wells. They were obtained by using the adjusted drawdown data of all wells to fit the least square equation. The average hydraulic conductivity and specific yield determined by the above method were found to be 6.2×10^{-4}

Table 6. Estimations of the flow parameters by test #1

Well #	distance cm	ME	SEE	S _y	T' cm ² /s	K cm/s
1	89.0	0.0051	0.64	0.048	0.1480	5.5E-04
2	169.0	0.0053	0.39	0.021	0.1525	5.6E-04
3	262.1	0.0077	0.28	0.029	0.1778	6.6E-04
4	352.8	0.0033	0.32	0.027	0.1890	7.0E-04
6	86.9	0.0054	0.53	0.029	0.1447	5.4E-04
7	179.8	0.0069	0.53	0.020	0.1592	5.9E-04
8	271.2	0.0069	0.33	0.018	0.1753	6.5E-04
9	362.1	0.0016	0.35	0.023	0.2053	7.6E-04
11	107.6	0.0029	0.28	0.030	0.1565	5.8E-04
12	196.6	0.0034	0.26	0.037	0.2056	7.6E-04
13	286.6	0.0030	0.15	0.031	0.2376	8.8E-04
14	384.0	0.0044	0.21	0.030	0.3002	1.1E-03
	arithmetic mean			0.0286	0.1876	6.9E-04
	standard deviation			0.0141	0.0880	3.3E-04
	coeff. of variation			0.4916	0.4689	0.4783
	geometric mean			0.0276	0.1833	6.8E-04
all wells		0.11	2.26	0.019	0.1662	6.2E-04

cm/s and 0.019 respectively; these are listed in the last row of Table 6. The values estimated by using all the data are smaller than the values of estimations using the data from individual wells.

The least squares fitting curves of each individual well on each of the three lines are shown in Figures 17, 18, and 19. In the initial pumping period, the fitting curves underestimate the drawdown response and it is not until later that the fitting curves capture the drawdown response well. To better measure the accuracy of the fit, the mean error (ME) and the standard error of the estimate (SEE) are calculated and listed in Table 6. ME is the average of the errors while SEE is the standard deviation of the absolute values of the errors (Herzberg, 1983).

Results of pumping test #2

Pumping rate and drawdown response The conditions of test #2 are contrasted with the conditions of test #1 in Table 2. As expected, the curve of the pumping rate vs time plotted on a log-log scale (Figure 10) appears linear after reaching the constant drawdown level. Figure 10 also shows that the pumping rates of test #2 were lower than those of test #1.

The pattern of the drawdown response of test #2 is quite similar to that of test #1. Figures 20, 21, and 22 show the drawdown response in the first 2.5 hours of pumping and the

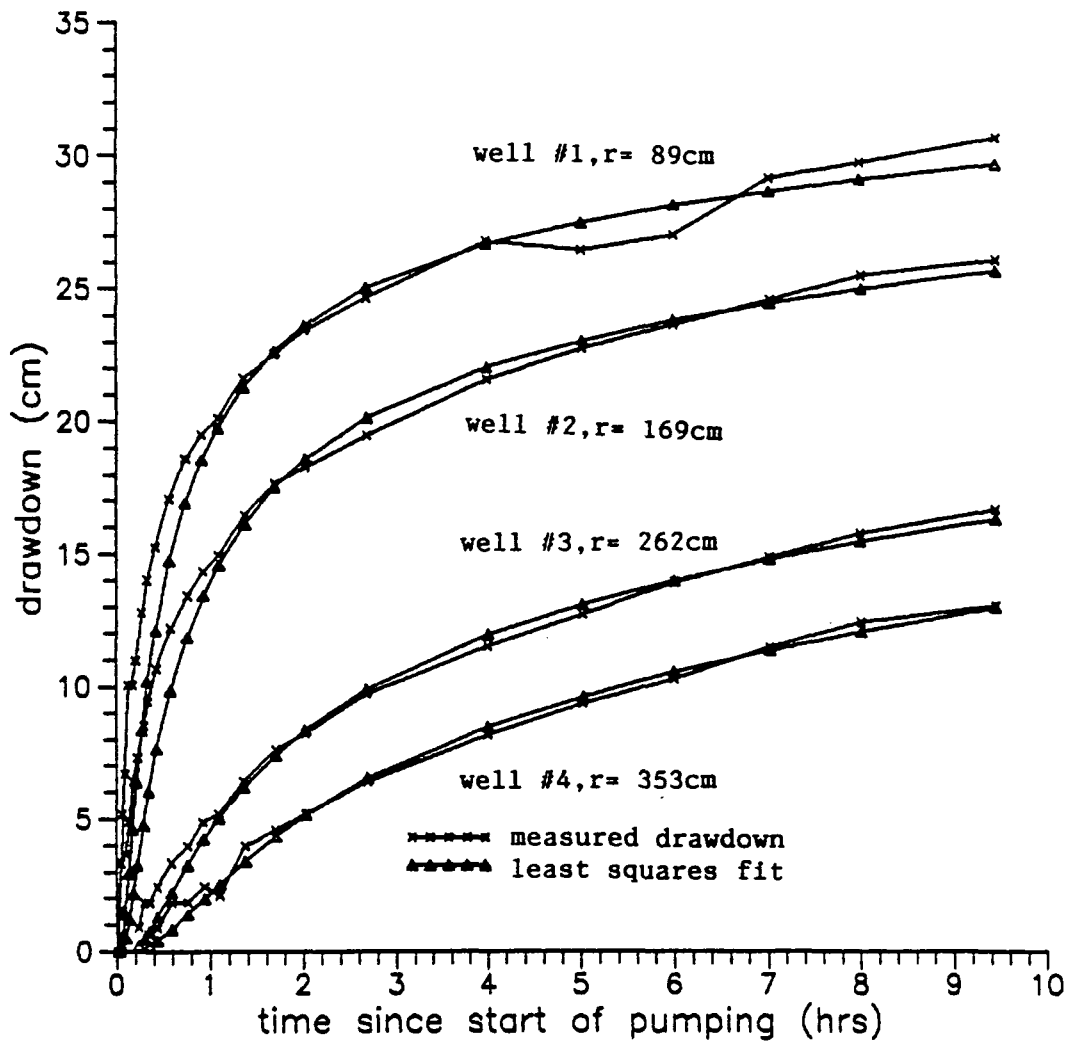


Figure 17. Test #1, the curves of the drawdown response and the least squares fitting for wells on line A

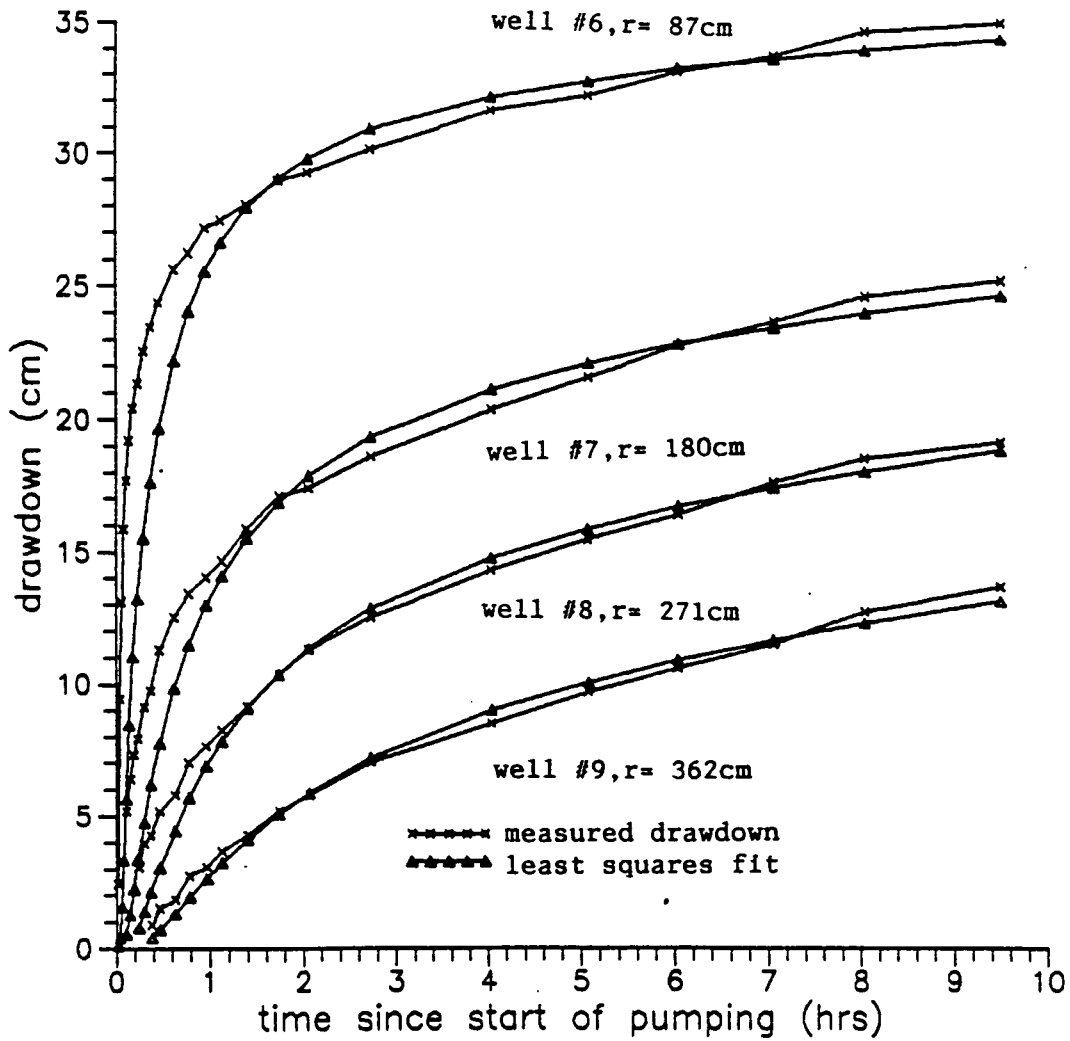


Figure 18. Test #1, the curves of the drawdown response and the least squares fitting for wells on line B

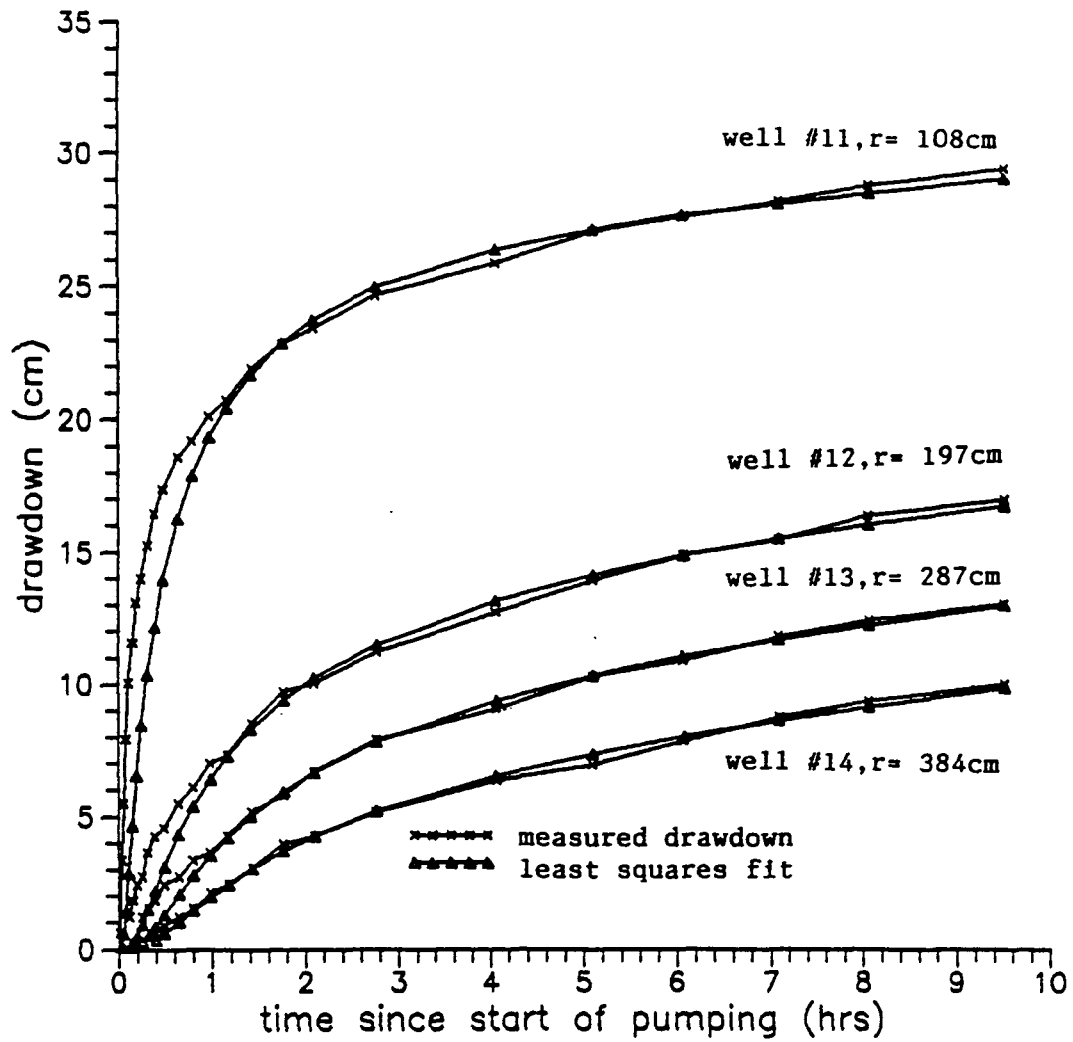


Figure 19. Test #1, the curves of the drawdown response and the least squares fitting for wells on line C

curves of drawdown response over the 24 hour pumping period for the observation wells located on the same radial line are plotted in Figures 23, 24, and 25. As with test #1, the drawdown, as measured in the observation wells, responded rapidly to the pumping. In contrast to test #1, the drawdown response of test #2 are flatter. As with test #1, the drawdown response data from wells located 20 feet from the pumping well were not included in the analysis.

After 24 hours of pumping, the pumping rates and drawdown responses appeared fairly stable. In the last three hours of pumping, the pumping rate fell only 10 ml/min. (513 ml/min. to 503 ml/min) and the drawdown responses of all observation wells increased by 0.02 to 0.03 feet.

Hydraulic conductivity and specific yield As with test #1, drawdown data during the first two hours of pumping were excluded from the least square fitting. Table 7 shows the results of initial transmissivities, specific yields, and estimated hydraulic conductivities of each individual well, along with their arithmetic and geometric means. The estimated hydraulic conductivities were obtained by dividing the initial transmissivities by the initial thickness of the saturated zone (8.20 feet). The arithmetic mean hydraulic conductivity is 5.2×10^{-4} cm/s and the geometric mean is 4.9×10^{-4} cm/s. The arithmetic mean apparent specific yield is 0.045, while the geometric mean is 0.041.

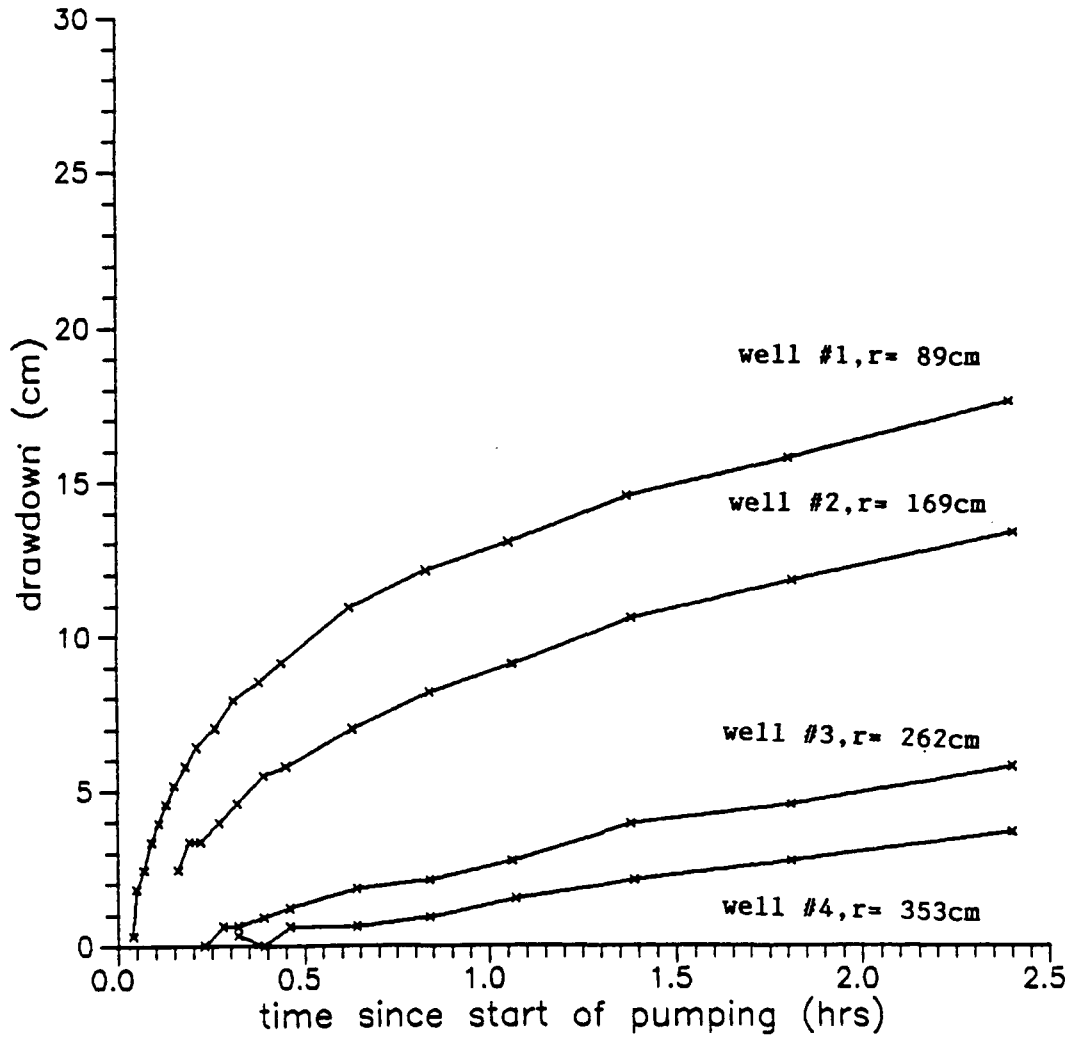


Figure 20. Test #2, drawdown response curves of wells on line A in the first 2.5 hours of pumping

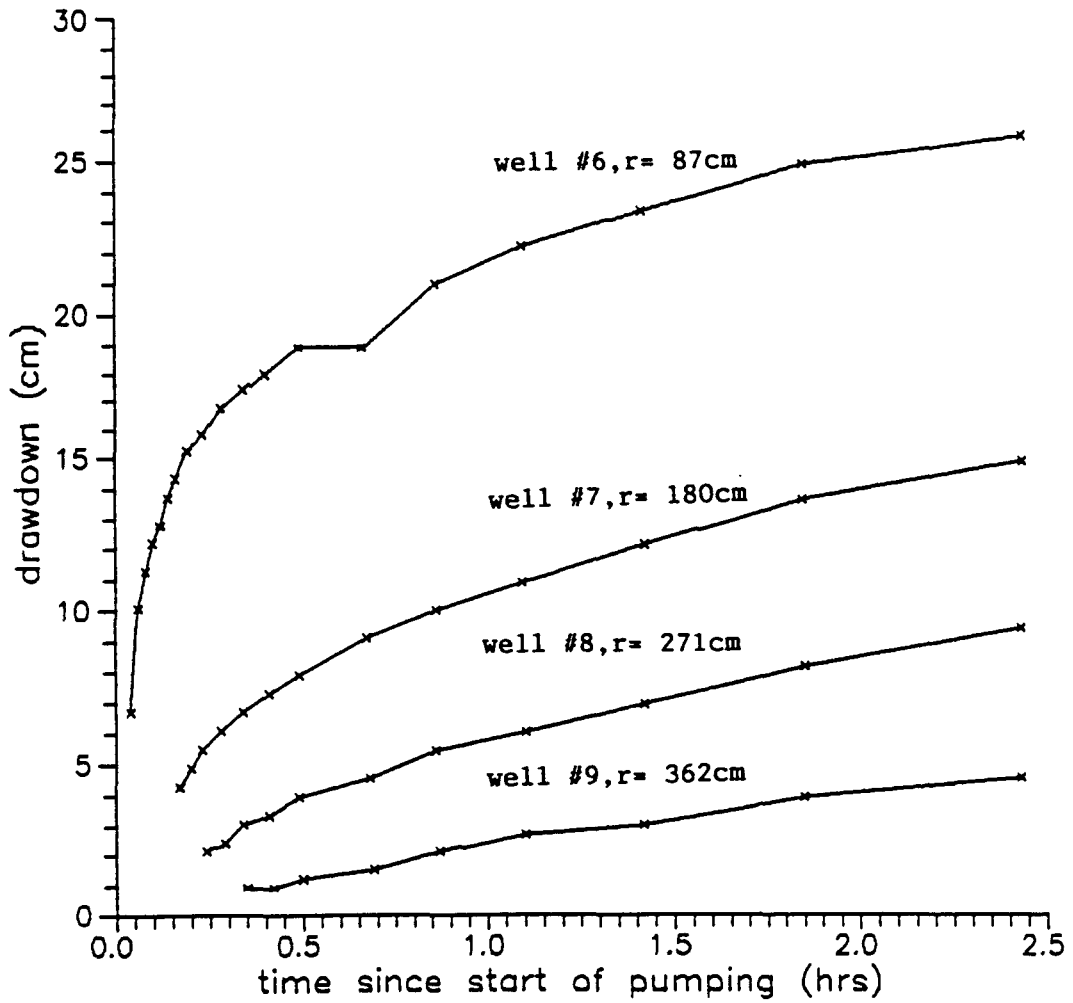


Figure 21. Test #2, drawdown response curves of wells on line B in the first 2.5 hours of pumping

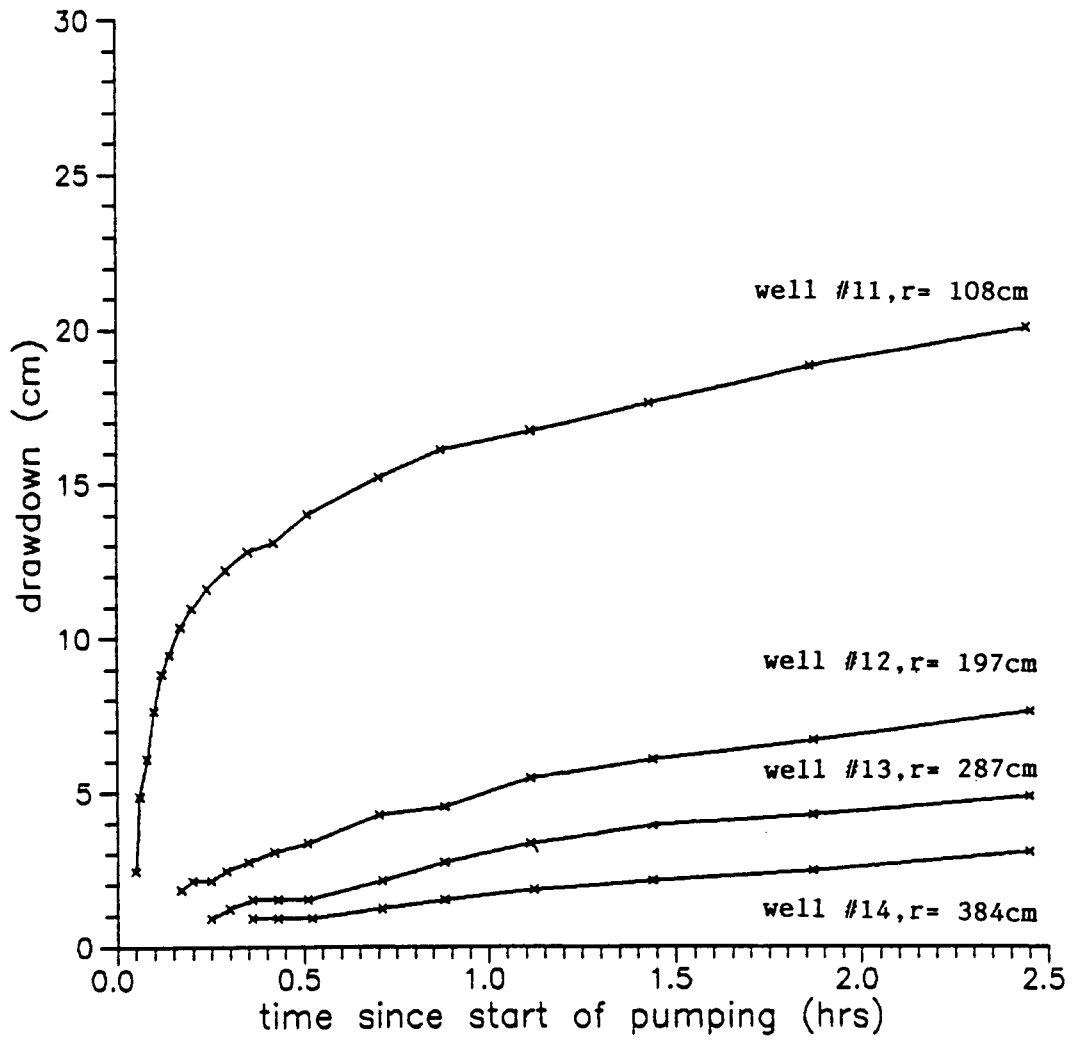


Figure 22. Test #2, drawdown response curves of wells on line C in the first 2.5 hours of pumping

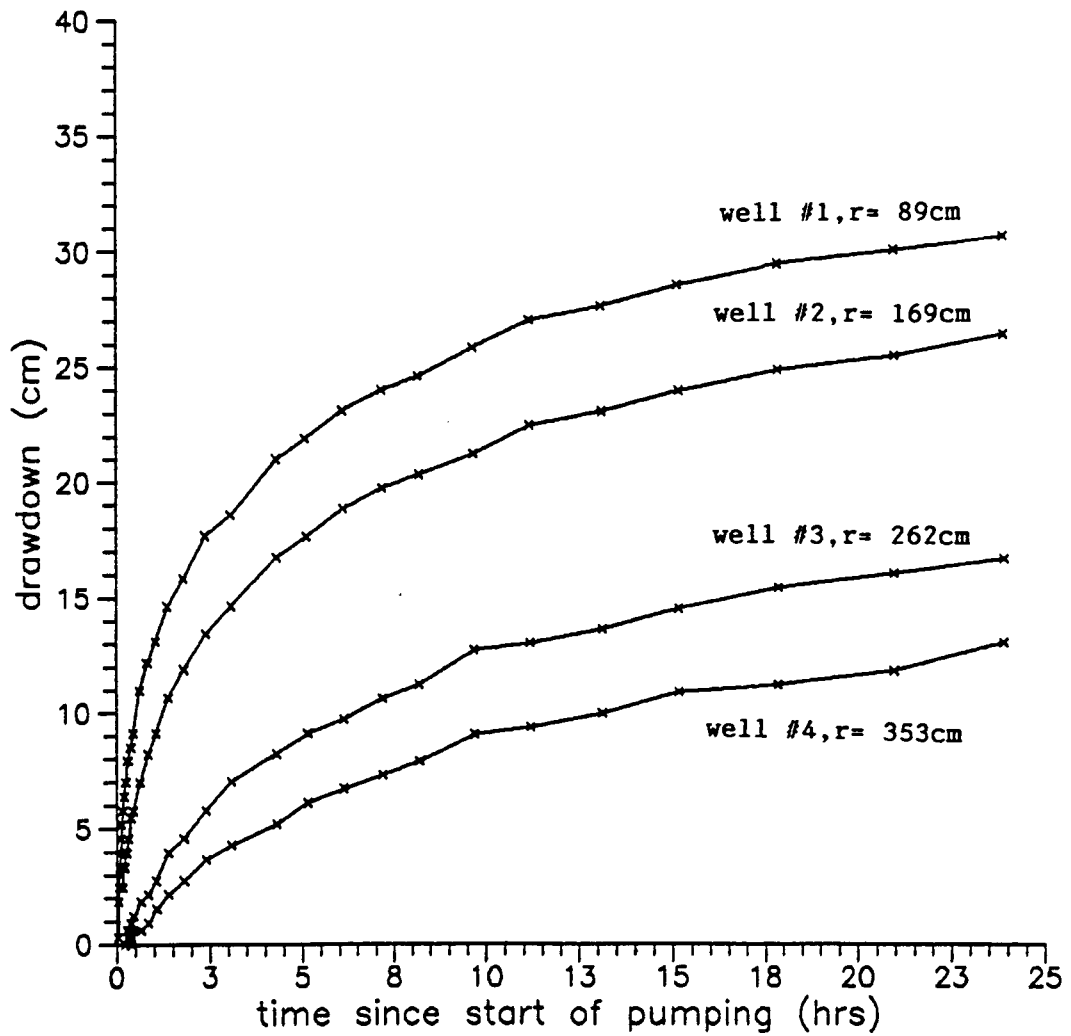


Figure 23. Test #2, drawdown response curves of wells on line A over the 24 hour pumping period

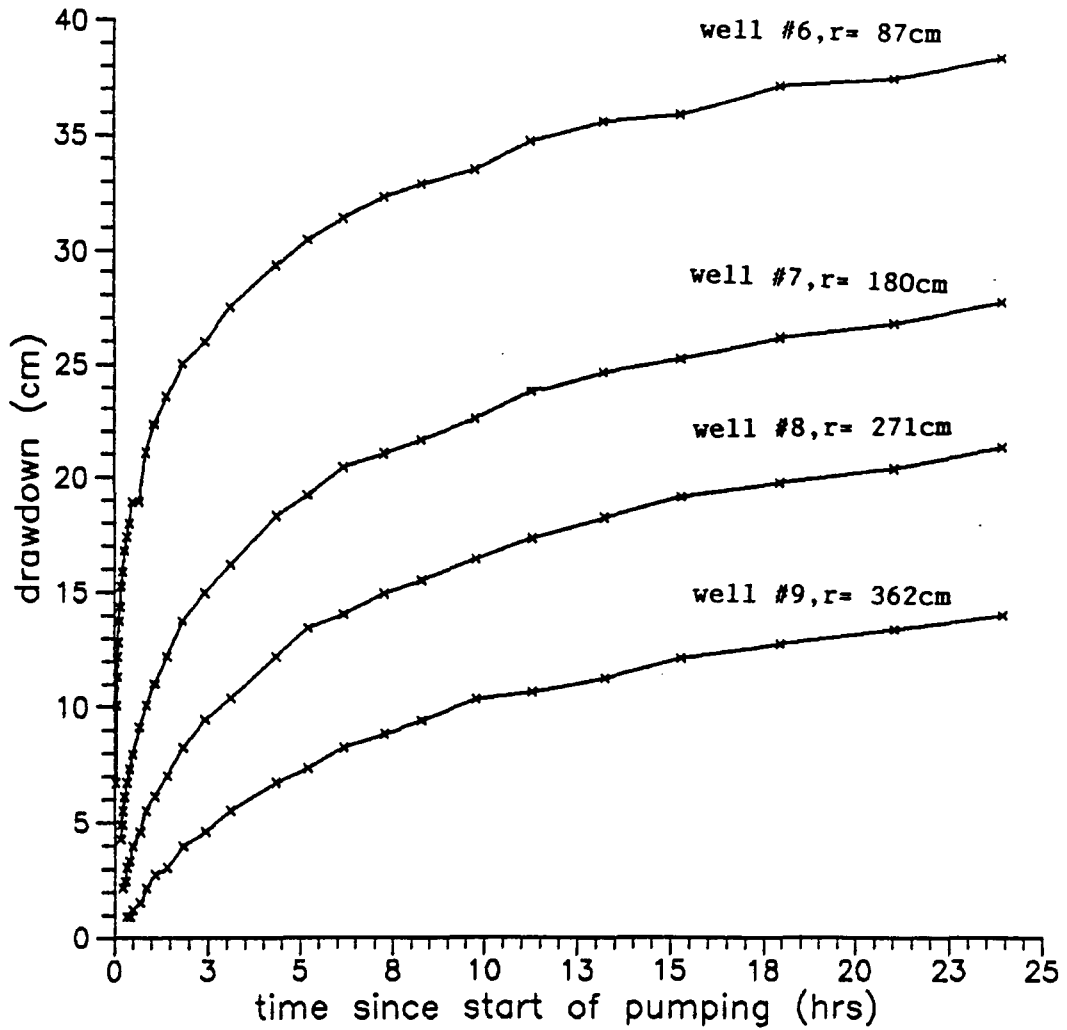


Figure 24. Test #2, drawdown response curves of wells on line B over the 24 hour pumping period

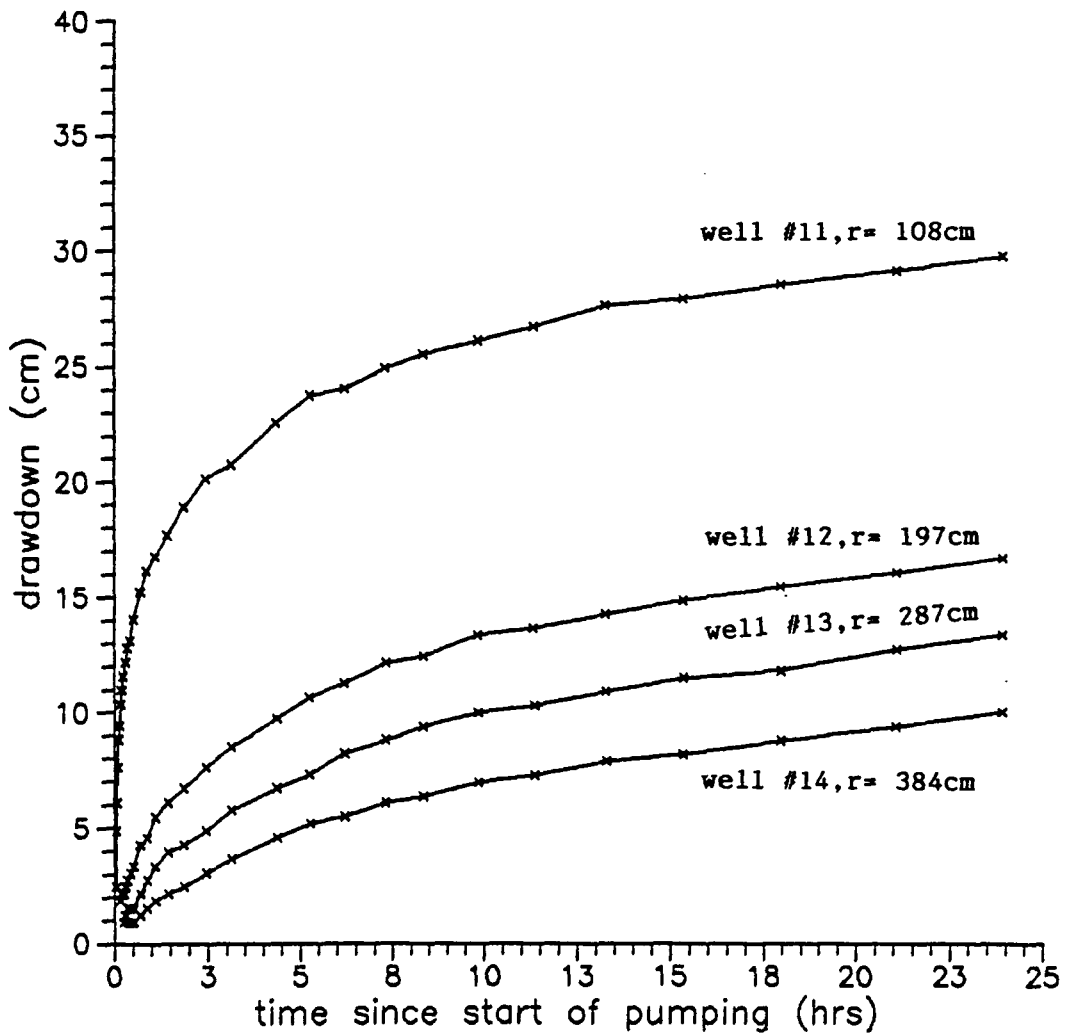


Figure 25. Test #2, drawdown response curves of wells on line C over the 24 hour pumping period

Table 7. Estimations of the flow parameters by test #2

Well #	distance cm	ME	SEE	S _y	T' cm ² /s	K cm/s
1	89.0	0.0023	0.33	0.101	0.0854	3.4E-04
2	169.0	0.0022	0.22	0.040	0.0937	3.7E-04
3	262.1	0.0044	0.26	0.040	0.1252	5.0E-04
4	352.8	0.0060	0.26	0.037	0.1557	6.2E-04
6	86.9	0.0011	0.24	0.059	0.0789	3.2E-04
7	179.8	0.0020	0.26	0.030	0.0932	3.7E-04
8	271.2	0.0031	0.24	0.023	0.1090	4.4E-04
9	362.1	0.0017	0.13	0.027	0.1529	6.1E-04
11	107.6	0.0006	0.22	0.050	0.1014	4.1E-04
12	196.6	0.0005	0.13	0.052	0.1490	6.0E-04
13	286.6	0.0006	0.16	0.040	0.1757	7.0E-04
14	384.0	0.0003	0.20	0.036	0.2419	9.7E-04
arithmetic mean				0.0446	0.1302	5.2E-04
standard deviation				0.0198	0.0454	1.8E-04
coeff. of variation				0.4431	0.3486	0.3462
geometric mean				0.0413	0.1232	4.9E-04
all wells		0.08	2.71	0.039	0.1104	4.4E-04

The average hydraulic conductivity and specific yield obtained by applying the adjusted drawdown data of all wells to the least squares fitting are listed in the last row in Table 7. The average hydraulic conductivity is 4.4×10^{-4} cm/s and specific yield is 0.039. As with test #1, the values estimated by using all the data are smaller than the values of estimations using the data from individual wells.

All the values of hydraulic conductivities of test #2 are relatively smaller than those of test #1, while the values of specific yields are relatively larger. The non-consistency of K 's and S_y 's between the tests will be discussed later.

The least squares fitting curves of the each individual well on each of the three lines are shown in Figures 26, 27, and 28. They show that in the early pumping, as expected, the fitting curves underestimate the drawdown response, but estimate the drawdown response well later. To provide a better evaluation of the accuracy of the fit, ME and SEE are calculated and listed in Table 7.

Discussion

Figure 9 and Table 8 illustrate two major differences between pumping test #1 and test #2. Even though the constant drawdown of test #1 is smaller than that of test #2 (3.04 feet to 4.92 feet), the pumping rate of test #1 is higher, and the estimated hydraulic conductivities from test #1 are

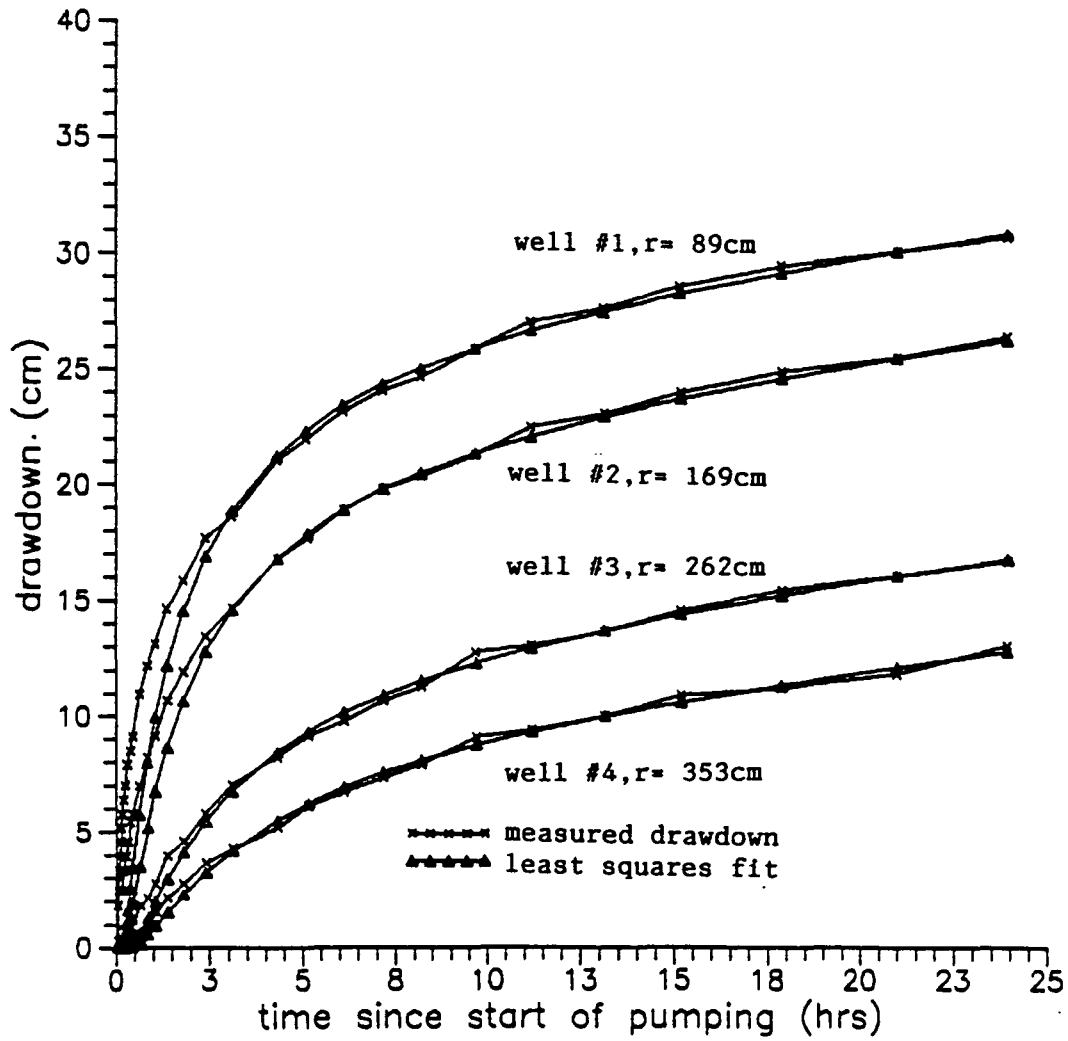


Figure 26. Test #2, the curves of the drawdown response and the least squares fitting for wells on line A

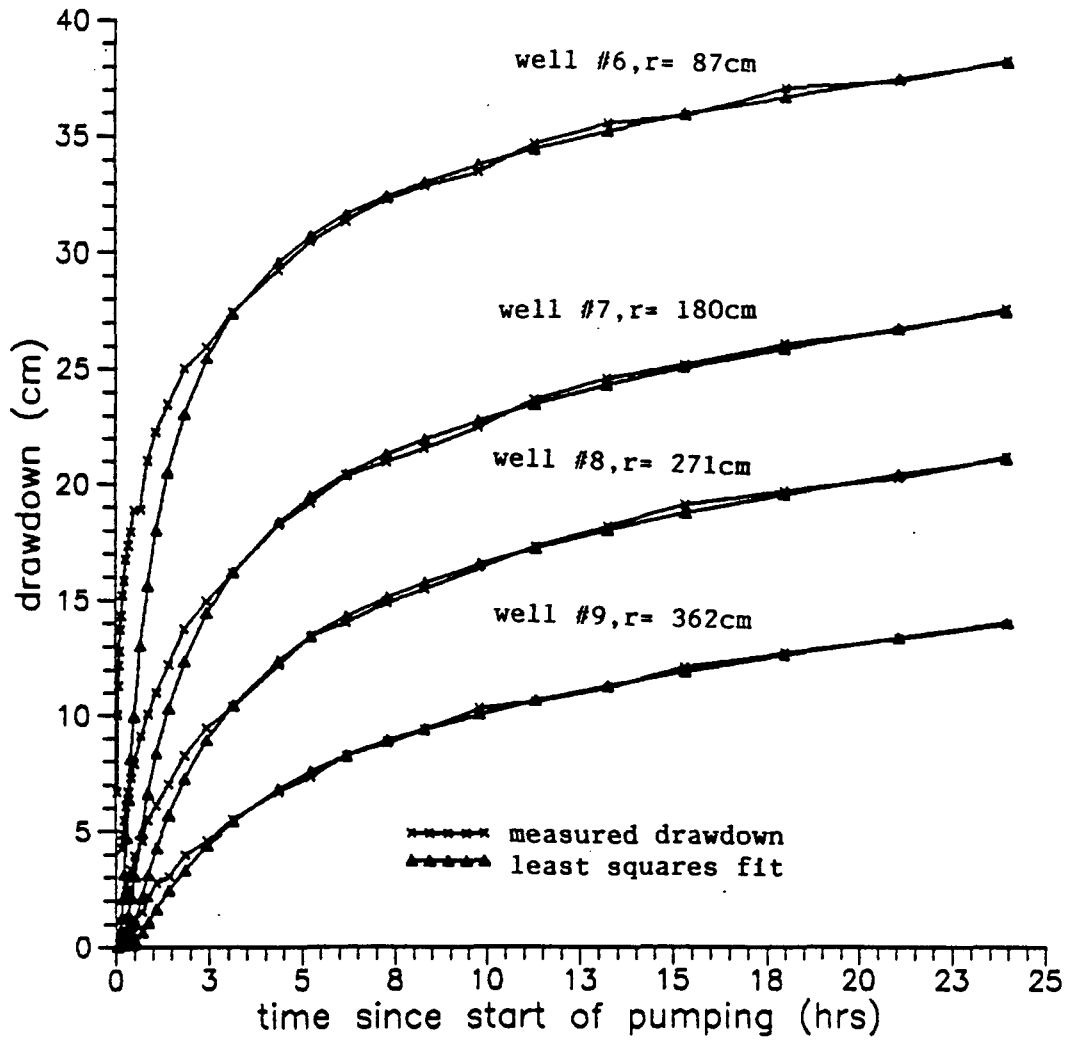


Figure 27. Test #2, the curves of the drawdown response and the least squares fitting for wells on line B

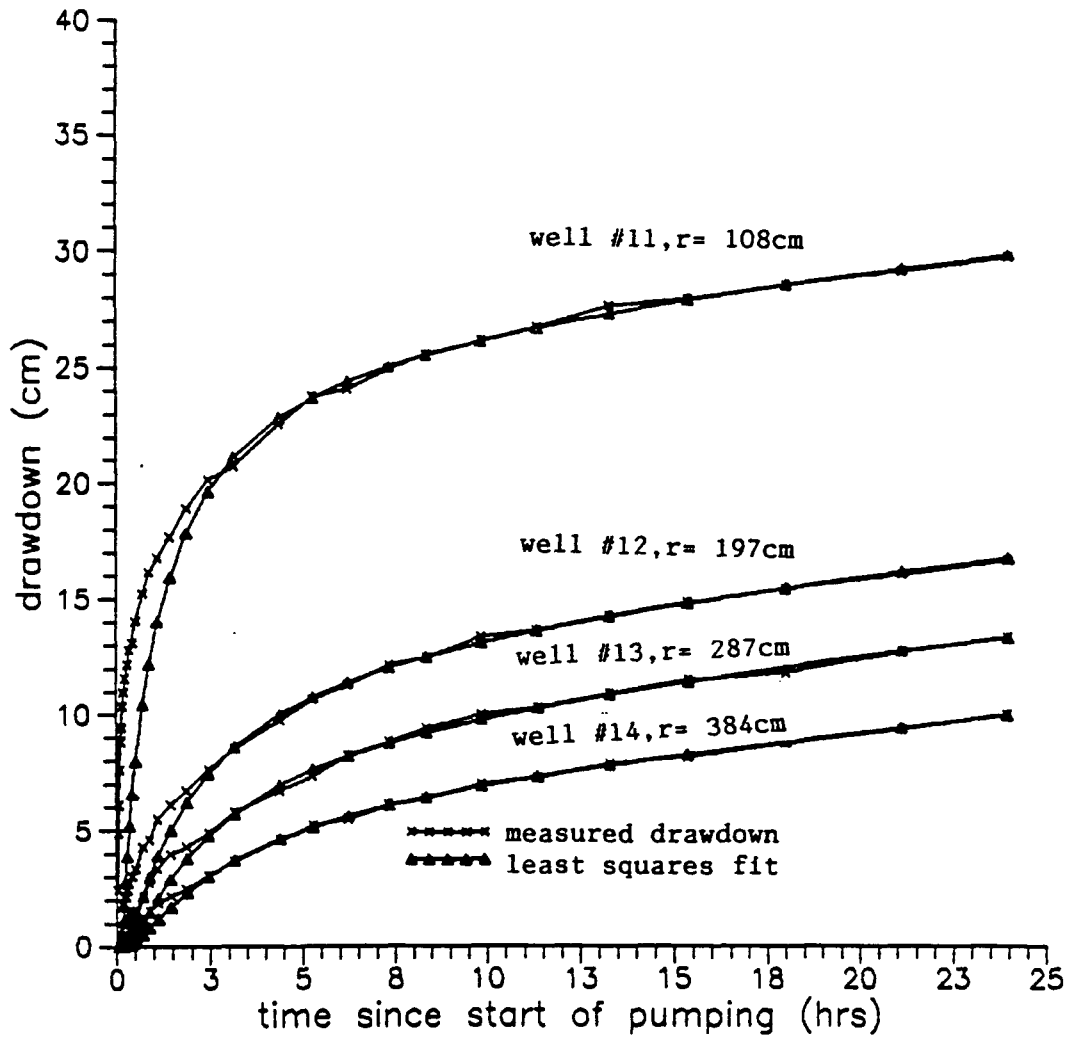


Figure 28. Test #2, the curves of the drawdown response and the least squares fitting for wells on line C

Table 8. Comparison of flow parameters estimated by both pumping tests and slug tests

Well #	Pumping Test				Slug Test
	Test #1		Test #2		
	S_y	K cm/s	S_y	K cm/s	
1	0.048	5.5E-04	0.101	3.4E-04	2.0E-04
2	0.021	5.6E-04	0.040	3.7E-04	1.8E-04
3	0.029	6.6E-04	0.040	5.0E-04	1.0E-04
4	0.027	7.0E-04	0.037	6.2E-04	1.4E-04
6	0.029	5.4E-04	0.059	3.2E-04	2.9E-04
7	0.020	5.9E-04	0.030	3.7E-04	3.3E-04
8	0.018	6.5E-04	0.023	4.4E-04	2.1E-04
9	0.023	7.6E-04	0.027	6.1E-04	2.8E-04
11	0.030	5.8E-04	0.050	4.1E-04	1.9E-04
12	0.037	7.6E-04	0.052	6.0E-04	2.6E-04
13	0.031	8.8E-04	0.040	7.0E-04	2.9E-04
14	0.030	1.1E-03	0.036	9.7E-04	2.6E-04
arithmetic mean	0.029	6.9E-04	0.045	5.2E-04	2.3E-04
geometric mean	0.028	6.8E-04	0.041	4.9E-04	2.2E-04
all wells	0.019	6.2E-04	0.039	4.4E-04	

higher than those of test #2 for each well, while the specific yield estimates are lower. Given the natural variability of field experiments and the difficulty in isolating particular parameters or boundary conditions, firm conclusions about the reasons for the differences between test #1 and #2 cannot be made. The following offers some possible reasons for the differences.

The Theis solution yields a vertically averaged hydraulic conductivity. It has been suggested that the hydraulic conductivity of weathered till decreases with depth and that root holes may significantly increase the bulk hydraulic conductivity (D'Astous et al., 1989). If this is indeed the case, then it would be expected that the larger initial saturated thickness of test #1, when compared to test #2 (0.64 feet), would result in a higher pumping rate and higher estimates of the vertically averaged hydraulic conductivity.

Specific yield is treated as a constant in the mathematical model, but it is well known that gravity drainage takes time and the specific yield increases with time until it approaches an ultimate value (Prill et al., 1965). If the time required for drainage is significant at this site, then it would be expected that test #2, with a duration of 24 hours, would yield a higher estimate of specific yield than test #1, with a duration of 9.5 hours.

Also, it may be noted in table 8 that the estimated hydraulic conductivities generated by both tests increase with increasing radial distance from the pumping well. This phenomenon may be due to the existence of a smeared clay zone along the borehole walls of the pumping well. The smeared clay zone, thought to occur from auger drilling in tills, can significantly reduce the hydraulic conductivity in the immediate vicinity of the pumping well (D'Astous et al., 1989). The Theis solution fit to data from a monitoring well yields an average of the hydraulic conductivity between the pumping well and the monitoring well. If a smeared zone exists, its influence on the Theis least squares fit will decrease with an increase in the monitoring well distance, yielding an apparent increase in the average hydraulic conductivity with an increase in radial distance.

Even though the purpose of the Jacob correction method is to account for the effect associated with the decreasing saturated zone thickness during pumping, the Jacob correction only accounts for a part of the effect associated with the decreasing thickness of the saturated zone when the drawdown is a relatively large portion of the saturated zone thickness. In this case the hydraulic conductivity from the wells near the pumping well, where the drawdown is considered a large portion of the saturated zone thickness, may be underestimated (Jacob, 1963). The degree of underestimation

decreases with increasing radial distance since the drawdown decreases. This could also account in part for the hydraulic conductivity increases with increasing distance from the pumping well. The increase in hydraulic conductivity with distance could be a combination of inadequacy in the Jacob approximation and borehole smearing.

The results of slug tests which were performed by Lemar in the same test site are also shown in Table 8 for the purpose of comparing the results to the pumping tests. It is clear that the average hydraulic conductivity of the slug tests is lower than those generated by the pumping tests. In studies in fluvial materials, Bradbury et al. (1990) also observed the phenomenon that the estimated hydraulic conductivity of a pumping test, which has a larger operational scale (influence area) than a slug test, tends to be higher than that of a slug test. Since slug tests only estimate the hydraulic conductivity in the immediate vicinity of the studied wells, a smeared zone (as mentioned previously) along the borehole walls of the studied wells would significantly reduce the estimated hydraulic conductivities. However, for the pumping tests the reduction of the average hydraulic conductivity due to the smeared zone along the borehole walls of the pumping well may be averaged out and become insignificant, since the pumping tests have a much larger operational scale than the slug tests. The

comparison between the results of the pumping tests and the slug tests suggests that hydraulic conductivity measurements based on slug tests should be used with some caution and are likely to underestimate the bulk hydraulic conductivity.

CONCLUSION

This work has demonstrated that the constant head pumping test is a good tool for investigating the flow parameters in the oxidized glacial till in central Iowa. The constant head pumping test is especially preferred when the aquifer is located in a relatively low permeable media with small saturated thickness. By the two tests, it is estimated that the average hydraulic conductivity in the oxidized till at the test site is about 5.3×10^{-4} cm/s, with a range from 3×10^{-4} cm/s to 1×10^{-3} cm/s. The average specific yield is around 3% with a range from 2% to 10%. The average hydraulic conductivity estimated by the two pumping tests is higher than that estimated by the slug tests. The other important results in this work are summarized below.

1. The results of the soil character tests support that the soil deposit at the test site is subglacial till. The transition zone of the oxidized till and the unoxidized till has an average depth of 11.1 feet and is not smooth.
2. For pumping in a shallow unconfined aquifer of relatively low permeability, increasing the drawdown in the pumping well does not necessarily result in an increasing pumping rate.
3. After the drawdown in the pumping well reaches a constant level, there is a linear relationship between the

pumping rate and the pumping time in a log-log scale. This is true at least within the first day of pumping.

4. The drawdown response was observed to react very rapidly. For the wells which were near the pumping well, the water table started to fall as soon as pumping started.

5. The estimated hydraulic conductivities of the observation wells tends to increase with increasing radial distance from the pumping well.

6. After ignoring the early time drawdown response, the This solution matches the observed drawdown reasonably well.

RECOMMENDATION FOR FURTHER RESEARCH

1. A constant head pumping test with pumping time longer than 24 hours should be performed to verify the pattern of the drawdown response beyond 24 hours of pumping.
2. In order to determine whether the initial thickness of the saturated zone significantly affects the determination of K and S_y , a constant head pumping test with the same initial thickness of the saturated zone as that of test #1 or test #2, and a different constant drawdown in the pumping well should be performed.
3. A constant head pumping test with a smaller constant drawdown in the pumping well than that of test #1 is needed for understanding the effect of the magnitude of the constant drawdown on the estimation of K and S_y .

BIBLIOGRAPHY

- Bear, J. Hydraulics of Groundwater. McGraw-Hill International Book Co., New York, 1979.
- Boulton, G. S. "On the Deposition of Subglacial and Meltout Till at the Margins of Certain Svalbard Glaciers." *Journal of Glaciology*, 9, No. 3 (1976): 159-194.
- Bradbury, K. R. and M. A. Muldoon. "Hydraulic Conductivity Determinations in Unlithified Glacial and Fluvial Materials" *Ground Water and Vadose Zone Monitoring*, ASTM STP 1053 (1990): 138-151.
- Cravens, S. J. and L. C. Ruedisili. "Water Movement in Till of East-Central South Dakota." *Groundwater*, Vol. 25 (1987): 555-561.
- Das, B. M. Soil Mechanics Laboratory Manual. Engineering Press, Inc., San Jose, California, 1982.
- D'Astous, A. Y., W. W. Ruland, J. R. G. Bruce, J. A. Cherry, and R. W. Gillham. "Fracture Effects in the Shallow Groundwater Zone in Weathered Sarnia-area Clay." *Canada Geotechnical Journal*, Vol. 26 (1989): 43-56.
- Desaulniers, D. E., J. A. Cherry, and P. Fritz. "Origin, Age and Movement of Pore Water in Argillaceous Quaternary Deposits at Four Sites in Southwestern Ontario." *Journal of Hydrology*, Vol. 50 (1981): 231-257.
- Freeze, R. A. and J. A. Cherry. Ground Water. Prentice Hall, Inc., Englewood Cliffs, New Jersey, 1979.
- Goldthwait, R. P., ed., "Introduction to Till, Today." *Till/A Symposium*, Ohio State University Press, Columbus, (1971): 3-26.
- Goodall, D. C. and R. M. Quigley. "Pollutant Migration from Two Sanitary Landfill Sites Near Sarma, Ontario." *Canada Geotechnical Journal*, Vol. 14 (1977): 223-236.
- Grisak, G. E. and J.A. Cherry. "Hydrologic Characteristics and Response of Fractured Till and Clay Confining a Shallow Aquifer." *Canadian Geotechnical Journal*, Vol. 12 (1976): 23-43.

Hendry, M. J. "Hydrogeology of Clay Till in a Prairie Region of Canada." *Groundwater*, Vol. 26 (1982): 162-169.

Herzberg, P. A. "Principles of Statistics" John Wiley & Sons, Inc., New York, New York, 1983.

Jacob, C. E. "Determining the Permeability of Water-Table Aquifers" U. S. Geological Survey, Water-Supply Paper, 1536-I (1963): 245-271.

Keller, C. K., G. Van der Kamp, and J. A. Cherry. "Fracture Permeability and Groundwater Flow in Clayey Till Near Saskatoon, Saskatchewan." *Canada Geotechnical Journal*, Vol. 23 (1986): 229-240.

Kemmis, T. J., G. R. Hallberg, and A. J. Lutenecker. "Depositional Environments of Glacial Sediments and Landform on the Des Moines Lobe, Iowa." Iowa Geological Survey Guidebook Series No. 6, 1981.

Law, K. T. and C. F. Lee. "Initial Gradient in a Dense Glacial Till." *Proc. 10th International conference on Soil Mechanics and Foundation Engineering*, Vol. 1 (1981): 441-446.

Lemar, T. "The Application of Aquifer Testing Evaluation Techniques to Oxidized Till Confining Units in Central Iowa." Unpublished M.S. Thesis, Iowa State University, Ames, Iowa, 1990.

Lutenecker, A. J., A. M. ASCE, T.J. Kemmis, and R. G. Hallberg. "Origin and Properties of Glacial Till and Diamictions." ASCE Geotechnical Engineering Division, Special Publication, 1983.

Lutenecker, A. J. "Geotechnical/Hydrogeologic studies of Glacial Till." Annual Report to Department of Natural Resources Geological Survey Bureau, State of Iowa, 1990.

Marino, M. A. and W. W-G. Yeh. "Nonsteady Flow in a Recharge Well-Unconfined Aquifer System." *Journal of Hydrology*, No. 16 (1972): 159-176.

Prill, R. C., A. I. Johnson, and D. A. Morris. "Specific Yield-Laboratory Experiments Showing the Effect of Time on Column Drainage." United States Geological Survey Water-Supply Paper 1662-B, 1965.

Prudic, D. E. "Hydraulic Conductivity of a Fine Grained Till, Cattaraugus County, NY." *Groundwater*, Vol. 20, No. 2 (1981): 194-200.

Stallman, R. W. "Variable Discharge Without Vertical Leakage." U. S. Geological Survey, Water-Supply Paper, 1536-E (1962): 118-122.

Sharp, J. M. "Hydrogeologic Characteristics of Shallow Glacial Drift Aquifers in Dissected Till Plains (North-Central Missouri)." Groundwater, Vol. 22 (1984): 683-689.

Starrett, R. J. and T. B. Edil. "Ground-Water Flow Systems and Stability of a Slope." Groundwater, Vol. 20 (1982): 5-11.

Theis, C. V. "The Relation Between Lowering of the Piezometric Surface and the Rate and Duration of Discharge of a Well Using Ground Water Storage." Transactions of American Geophysical Union, 16th annual meeting, Pt.2 (1935): 519-524.

Wang, H. Y. "In Situ Lateral Earth Pressure and Its Effect on Vertical Hydraulic Conductivity in a Glacial Till Deposit." Ph.D. Thesis, Iowa State University, Ames, Iowa, 1990.

ACKNOWLEDGMENTS

I wish to express my sincere appreciation to my major professor, Dr. LaDon Jones for his support, encouragement, and guidance through every stage of my study. Thanks to Dr. Al Austin and Dr. Robert Horton, Jr. for serving on my program of study committee.

I would like to express my thanks to my family for their support. A very special thanks to my wife, Hui-Ling. Her optimism and confidence in my abilities were the major driving force to complete this work. Finally, this work is a special gift for my son, Max, who was born on March 19, 1991.

APPENDIX A. ORIGINAL DATA of PUMPING RATE
vs TIME

Pumping Test #1, 07/17/90

Recorded Pumping Rate vs Time

Time (sec)	Time (hr)	Flow Rate (ml/min)	Time (sec)	Time (hr)	Flow Rate (ml/min)
30	0.01	2580	1560	0.43	1520
60	0.02	2740	1620	0.45	1500
90	0.03	2740	1680	0.47	1480
120	0.03	2800	1740	0.48	1490
150	0.04	2680	1800	0.50	1470
180	0.05	2660	1860	0.52	1460
210	0.06	2660	1920	0.53	1460
240	0.07	2700	1980	0.55	1450
270	0.08	2700	2040	0.57	1440
300	0.08	2620	2100	0.58	1430
330	0.09	2560	2160	0.60	1430
360	0.10	2360	2220	0.62	1430
390	0.11	2220	2280	0.63	1400
420	0.12	2120	2340	0.65	1400
450	0.13	1960	2400	0.67	1380
480	0.13	1960	2460	0.68	1390
540	0.15	1920	2520	0.70	1380
600	0.17	1880	2580	0.72	1360
660	0.18	1860	2640	0.73	1360
720	0.20	1740	2700	0.75	1350
780	0.22	1680	2760	0.77	1340
840	0.23	1750	2820	0.78	1340
900	0.25	1680	2880	0.80	1330
960	0.27	1680	2940	0.82	1340
1020	0.28	1640	3000	0.83	1320
1080	0.30	1640	3060	0.85	1310
1140	0.32	1600	3120	0.87	1310
1200	0.33	1620	3180	0.88	1300
1260	0.35	1580	3240	0.90	1300
1320	0.37	1570	3300	0.92	1290
1380	0.38	1540	3360	0.93	1280
1440	0.40	1520	3420	0.95	1280
1500	0.42	1520	3480	0.97	1260
Continued			Continued		

Time (sec)	Time (hr)	Flow Rate (ml/min)
3540	0.98	1260
3600	1.00	1270
3660	1.02	1250
3720	1.03	1260
3780	1.05	1250
3840	1.07	1230
3900	1.08	1240
3960	1.10	1230
4020	1.12	1230
4080	1.13	1230
4140	1.15	1220
4200	1.17	1230
4260	1.18	1230
4320	1.20	1200
4380	1.22	1210
4440	1.23	1210
4500	1.25	1200
4560	1.27	1200
4620	1.28	1200
4680	1.30	1200
4740	1.32	1200
4800	1.33	1190
4860	1.35	1190
4920	1.37	1190
4980	1.38	1180
5040	1.40	1180
5100	1.42	1170
5160	1.43	1160
5220	1.45	1150
5280	1.47	1150
5340	1.48	1140
5400	1.50	1150
5460	1.52	1150
5520	1.53	1140
5580	1.55	1140
5640	1.57	1140
5700	1.58	1120

Continued

Time (sec)	Time (hr)	Flow Rate (ml/min)
5760	1.60	1120
5820	1.62	1140
5880	1.63	1130
6000	1.67	1115
6060	1.68	1110
6120	1.70	1120
6180	1.72	1110
6240	1.73	1110
6300	1.75	1110
6360	1.77	1100
6420	1.78	1110
6480	1.80	1110
6540	1.82	1100
6600	1.83	1100
6660	1.85	1090
6720	1.87	1090
6780	1.88	1090
6840	1.90	1090
6900	1.92	1080
6960	1.93	1080
7020	1.95	1080
7080	1.97	1080
7140	1.98	1080
7200	2.00	1070
7260	2.02	1070
7320	2.03	1070
7380	2.05	1070
7440	2.07	1070
7500	2.08	1060
7560	2.10	1060
7740	2.15	1053
7800	2.17	1050
7860	2.18	1050
7920	2.20	1050
7980	2.22	1050
8040	2.23	1050
8100	2.25	1040

Continued

Time (sec)	Time (hr)	Flow Rate (ml/min)	Time (sec)	Time (hr)	Flow Rate (ml/min)
8160	2.27	1050	10740	2.98	970
8220	2.28	1040	10860	3.02	970
8280	2.30	1040	10980	3.05	970
8340	2.32	1040	11100	3.08	960
8400	2.33	1040	11220	3.12	965
8460	2.35	1040	11340	3.15	960
8520	2.37	1030	11460	3.18	960
8580	2.38	1030	11580	3.22	960
8640	2.40	1040	11700	3.25	950
8700	2.42	1030	11820	3.28	950
8760	2.43	1040	11940	3.32	950
8820	2.45	1020	12060	3.35	950
8880	2.47	1030	12180	3.38	950
8940	2.48	1030	12300	3.42	945
9000	2.50	1020	12420	3.45	940
9060	2.52	1030	12540	3.48	945
9120	2.53	1030	12660	3.52	940
9180	2.55	1010	12780	3.55	940
9240	2.57	1000	12900	3.58	935
9300	2.58	1020	13020	3.62	935
9360	2.60	1010	13140	3.65	935
9420	2.62	1010	13260	3.68	930
9480	2.63	1000	13380	3.72	930
9540	2.65	1010	13500	3.75	930
9600	2.67	1000	13620	3.78	925
9660	2.68	1000	13740	3.82	920
9720	2.70	1000	13860	3.85	920
9780	2.72	1010	13980	3.88	920
9840	2.73	1000	14100	3.92	920
9900	2.75	1000	14220	3.95	920
9960	2.77	1000	14340	3.98	915
10020	2.78	1000	14460	4.02	910
10140	2.82	985	14580	4.05	910
10260	2.85	985	14700	4.08	910
10380	2.88	975	14820	4.12	910
10500	2.92	980	14940	4.15	905
10620	2.95	980	15060	4.18	905
Continued			Continued		

Time (sec)	Time (hr)	Flow Rate (ml/min)	Time (sec)	Time (hr)	Flow Rate (ml/min)
15180	4.22	900	19620	5.45	850
15300	4.25	900	19740	5.48	850
15420	4.28	900	19860	5.52	850
15540	4.32	895	19980	5.55	850
15660	4.35	895	20100	5.58	845
15780	4.38	895	20220	5.62	850
15900	4.42	895	20340	5.65	845
16020	4.45	890	20460	5.68	845
16140	4.48	890	20580	5.72	840
16260	4.52	890	20700	5.75	840
16380	4.55	885	20820	5.78	840
16500	4.58	880	20940	5.82	840
16620	4.62	880	21060	5.85	840
16740	4.65	880	21180	5.88	835
16860	4.68	880	21300	5.92	840
16980	4.72	875	21420	5.95	830
17100	4.75	875	21540	5.98	835
17220	4.78	875	21660	6.02	830
17340	4.82	870	21780	6.05	830
17460	4.85	870	21900	6.08	835
17580	4.88	870	22020	6.12	830
17700	4.92	870	22140	6.15	825
17820	4.95	870	22260	6.18	825
17940	4.98	870	22380	6.22	825
18060	5.02	860	22500	6.25	825
18180	5.05	860	22620	6.28	825
18300	5.08	860	22740	6.32	820
18420	5.12	860	22860	6.35	820
18540	5.15	855	22980	6.38	820
18660	5.18	860	23100	6.42	815
18780	5.22	860	23220	6.45	815
18900	5.25	855	23340	6.48	815
19020	5.28	860	23460	6.52	815
19140	5.32	850	23580	6.55	810
19260	5.35	850	23700	6.58	810
19380	5.38	860	23820	6.62	810
19500	5.42	855	23940	6.65	810

Continued

Continued

Time (sec)	Time (hr)	Flow Rate (ml/min)	Time (sec)	Time (hr)	Flow Rate (ml/min)
24060	6.68	810	28500	7.92	775
24180	6.72	805	28620	7.95	775
24300	6.75	805	28740	7.98	775
24420	6.78	795	28860	8.02	775
24540	6.82	800	28980	8.05	770
24660	6.85	800	29100	8.08	775
24780	6.88	800	29220	8.12	770
24900	6.92	795	29340	8.15	770
25020	6.95	790	29460	8.18	770
25140	6.98	800	29580	8.22	770
25260	7.02	795	29700	8.25	770
25380	7.05	800	29820	8.28	765
25500	7.08	795	29940	8.32	770
25620	7.12	800	30060	8.35	770
25740	7.15	795	30180	8.38	770
25860	7.18	795	30300	8.42	765
25980	7.22	795	30420	8.45	770
26100	7.25	800	30540	8.48	765
26220	7.28	790	30660	8.52	760
26340	7.32	790	30780	8.55	760
26460	7.35	790	30900	8.58	760
26580	7.38	800	31020	8.62	760
26700	7.42	790	31140	8.65	760
26820	7.45	795	31260	8.68	760
26940	7.48	790	31380	8.72	755
27060	7.52	785	31500	8.75	760
27180	7.55	790	31620	8.78	755
27300	7.58	780	31740	8.82	755
27420	7.62	780	31860	8.85	750
27540	7.65	780	31980	8.88	755
27660	7.68	780	32100	8.92	750
27780	7.72	780	32220	8.95	750
27900	7.75	785	32340	8.98	750
28020	7.78	780	32460	9.02	750
28140	7.82	780	32580	9.05	750
28260	7.85	775	32700	9.08	750
28380	7.88	780	32820	9.12	750
Continued			Continued		

Time (sec)	Time (hr)	Flow Rate (ml/min)
32940	9.15	750
33060	9.18	750
33180	9.22	750
33300	9.25	750
33420	9.28	750
33540	9.32	750
33660	9.35	750
33780	9.38	750
33900	9.42	750
34020	9.45	750
34140	9.48	750
34260	9.52	750
34380	9.55	750

Pumping Test #2, 08/06/90

Pumping Rate vs Time:

Time (sec)	Time (hr)	Flow Rate (ml/min)	Time (sec)	Time (hr)	Flow Rate (ml/min)
20	0.01	2580	1260	0.35	1200
40	0.01	2580	1320	0.37	1200
60	0.02	2580	1380	0.38	1180
80	0.02	2580	1440	0.40	1170
100	0.03	2580	1500	0.42	1160
120	0.03	2550	1560	0.43	1150
140	0.04	2580	1620	0.45	1140
160	0.04	2550	1680	0.47	1140
180	0.05	2520	1740	0.48	1120
210	0.06	2520	1800	0.50	1120
240	0.07	2440	1860	0.52	1110
270	0.08	2460	1920	0.53	1100
300	0.08	2480	1980	0.55	1100
330	0.09	2400	2040	0.57	1090
360	0.10	2380	2100	0.58	1080
390	0.11	2280	2160	0.60	1080
420	0.12	2120	2220	0.62	1070
450	0.13	1540	2280	0.63	1070
480	0.13	1440	2340	0.65	1060
510	0.14	1440	2400	0.67	1060
540	0.15	1440	2460	0.68	1050
570	0.16	1420	2520	0.70	1040
600	0.17	1400	2580	0.72	1040
630	0.18	1400	2640	0.73	1040
660	0.18	1380	2700	0.75	1040
690	0.19	1360	2760	0.77	1020
720	0.20	1360	2820	0.78	1020
780	0.22	1320	2880	0.80	1010
840	0.23	1310	2940	0.82	1000
900	0.25	1300	3000	0.83	1000
960	0.27	1260	3060	0.85	1000
1020	0.28	1250	3120	0.87	1000
1080	0.30	1240	3180	0.88	990
1140	0.32	1220	3240	0.90	990
1200	0.33	1210	3300	0.92	990
continued			continued		

Time (sec)	Time (hr)	Flow Rate (ml/min)	Time (sec)	Time (hr)	Flow Rate (ml/min)
3360	0.93	980	7800	2.17	820
3420	0.95	980	7920	2.20	820
3480	0.97	980	8040	2.23	815
3540	0.98	970	8160	2.27	810
3600	1.00	970	8280	2.30	810
3720	1.03	960	8400	2.33	810
3840	1.07	955	8520	2.37	810
3960	1.10	950	8640	2.40	805
4080	1.13	940	8760	2.43	800
4200	1.17	935	8880	2.47	795
4320	1.20	935	9000	2.50	790
4440	1.23	930	9120	2.53	790
4560	1.27	920	9240	2.57	780
4680	1.30	920	9360	2.60	780
4800	1.33	915	9480	2.63	780
4920	1.37	905	9600	2.67	775
5040	1.40	905	9720	2.70	765
5160	1.43	900	9840	2.73	775
5280	1.47	895	9960	2.77	775
5400	1.50	890	10080	2.80	775
5520	1.53	885	10200	2.83	770
5640	1.57	880	10320	2.87	770
5760	1.60	875	10440	2.90	765
5880	1.63	870	10560	2.93	765
6000	1.67	865	10680	2.97	765
6120	1.70	860	10800	3.00	760
6240	1.73	865	10920	3.03	760
6360	1.77	855	11040	3.07	755
6480	1.80	860	11160	3.10	755
6600	1.83	855	11280	3.13	755
6720	1.87	850	11400	3.17	755
6840	1.90	845	11520	3.20	750
6960	1.93	845	11640	3.23	750
7080	1.97	840	11760	3.27	750
7200	2.00	835	11880	3.30	750
7320	2.03	830	12000	3.33	740
7440	2.07	830	12120	3.37	740
7560	2.10	830	12240	3.40	740
7680	2.13	825	12360	3.43	740

continued

continued

Time (sec)	Time (hr)	Flow Rate (ml/min)	Time (sec)	Time (hr)	Flow Rate (ml/min)
12480	3.47	735	17160	4.77	690
12600	3.50	735	17280	4.80	690
12720	3.53	735	17400	4.83	685
12840	3.57	730	17520	4.87	685
12960	3.60	730	17640	4.90	685
13080	3.63	730	17760	4.93	685
13200	3.67	730	17880	4.97	685
13320	3.70	730	18000	5.00	680
13440	3.73	725	18120	5.03	680
13560	3.77	730	18240	5.07	680
13680	3.80	725	18360	5.10	680
13800	3.83	720	18480	5.13	680
13920	3.87	720	18600	5.17	680
14040	3.90	720	18720	5.20	675
14160	3.93	720	18840	5.23	675
14280	3.97	715	18960	5.27	675
14400	4.00	720	19080	5.30	675
14520	4.03	715	19200	5.33	670
14640	4.07	715	19320	5.37	670
14760	4.10	710	19440	5.40	670
14880	4.13	710	19560	5.43	670
15000	4.17	710	19680	5.47	670
15120	4.20	705	19800	5.50	665
15240	4.23	700	19920	5.53	665
15360	4.27	700	20040	5.57	665
15480	4.30	705	20160	5.60	665
15600	4.33	705	20280	5.63	665
15720	4.37	700	20400	5.67	665
15840	4.40	700	20520	5.70	660
15960	4.43	700	20700	5.75	660
16080	4.47	700	20880	5.80	660
16200	4.50	700	21060	5.85	657
16320	4.53	700	21240	5.90	653
16440	4.57	695	21420	5.95	650
16560	4.60	695	21600	6.00	650
16680	4.63	695	21780	6.05	647
16800	4.67	690	21960	6.10	647
16920	4.70	690	22140	6.15	643
17040	4.73	690	22320	6.20	643

continued

continued

Time (sec)	Time (hr)	Flow Rate (ml/min)	Time (sec)	Time (hr)	Flow Rate (ml/min)
22500	6.25	643	29520	8.20	610
22680	6.30	643	29700	8.25	610
22860	6.35	643	29880	8.30	607
23040	6.40	640	30060	8.35	607
23220	6.45	640	30240	8.40	607
23400	6.50	640	30420	8.45	603
23580	6.55	640	30600	8.50	603
23760	6.60	637	30780	8.55	603
23940	6.65	633	30960	8.60	603
24120	6.70	633	31140	8.65	603
24300	6.75	633	31320	8.70	600
24480	6.80	630	31500	8.75	600
24660	6.85	630	31680	8.80	600
24840	6.90	630	31860	8.85	600
25020	6.95	630	32040	8.90	600
25200	7.00	627	32220	8.95	597
25380	7.05	627	32400	9.00	597
25560	7.10	627	32580	9.05	597
25740	7.15	627	32760	9.10	597
25920	7.20	627	32940	9.15	593
26100	7.25	627	33120	9.20	593
26280	7.30	627	33300	9.25	593
26460	7.35	623	33480	9.30	593
26640	7.40	623	33660	9.35	593
26820	7.45	620	33840	9.40	590
27000	7.50	620	34020	9.45	590
27180	7.55	620	34200	9.50	593
27360	7.60	620	34380	9.55	590
27540	7.65	620	34560	9.60	590
27720	7.70	620	34740	9.65	587
27900	7.75	620	34920	9.70	587
28080	7.80	617	35100	9.75	587
28260	7.85	617	35280	9.80	590
28440	7.90	617	35460	9.85	587
28620	7.95	613	35640	9.90	587
28800	8.00	613	35820	9.95	587
28980	8.05	613	36000	10.00	587
29160	8.10	613	36180	10.05	587
29340	8.15	613	36360	10.10	587
continued			continued		

Time (sec)	Time (hr)	Flow Rate (ml/min)	Time (sec)	Time (hr)	Flow Rate (ml/min)
36540	10.15	587	43560	12.10	570
36720	10.20	587	43740	12.15	567
36900	10.25	587	43920	12.20	567
37080	10.30	587	44100	12.25	567
37260	10.35	587	44280	12.30	563
37440	10.40	583	44460	12.35	563
37620	10.45	583	44640	12.40	563
37800	10.50	587	44820	12.45	563
37980	10.55	587	45000	12.50	563
38160	10.60	583	45180	12.55	563
38340	10.65	583	45360	12.60	560
38520	10.70	583	45540	12.65	560
38700	10.75	580	45720	12.70	560
38880	10.80	580	45900	12.75	560
39060	10.85	580	46080	12.80	560
39240	10.90	580	46260	12.85	560
39420	10.95	580	46440	12.90	560
39600	11.00	580	46620	12.95	560
39780	11.05	580	46800	13.00	560
39960	11.10	580	46980	13.05	560
40140	11.15	577	47160	13.10	557
40320	11.20	577	47340	13.15	557
40500	11.25	577	47520	13.20	557
40680	11.30	573	47700	13.25	557
40860	11.35	573	47880	13.30	553
41040	11.40	573	48060	13.35	557
41220	11.45	573	48240	13.40	553
41400	11.50	573	48420	13.45	553
41580	11.55	573	48600	13.50	553
41760	11.60	573	48780	13.55	553
41940	11.65	573	48960	13.60	553
42120	11.70	573	49140	13.65	553
42300	11.75	573	49320	13.70	553
42480	11.80	573	49500	13.75	553
42660	11.85	573	49680	13.80	553
42840	11.90	573	49860	13.85	553
43020	11.95	570	50040	13.90	553
43200	12.00	570	50220	13.95	553
43380	12.05	570	50400	14.00	553

continued

continued

Time (sec)	Time (hr)	Flow Rate (ml/min)	Time (sec)	Time (hr)	Flow Rate (ml/min)
50580	14.05	553	57600	16.00	537
50760	14.10	553	57780	16.05	537
50940	14.15	550	57960	16.10	537
51120	14.20	553	58140	16.15	537
51300	14.25	553	58320	16.20	537
51480	14.30	550	58500	16.25	537
51660	14.35	550	58680	16.30	537
51840	14.40	550	58860	16.35	537
52020	14.45	550	59040	16.40	537
52200	14.50	550	59220	16.45	533
52380	14.55	550	59400	16.50	533
52560	14.60	546	59580	16.55	533
52740	14.65	546	59760	16.60	533
52920	14.70	546	59940	16.65	533
53100	14.75	546	60120	16.70	533
53280	14.80	546	60300	16.75	533
53460	14.85	546	60480	16.80	533
53640	14.90	543	60660	16.85	533
53820	14.95	546	60840	16.90	533
54000	15.00	543	61020	16.95	533
54180	15.05	543	61200	17.00	533
54360	15.10	543	61380	17.05	533
54540	15.15	543	61560	17.10	533
54720	15.20	540	61740	17.15	533
54900	15.25	540	61920	17.20	533
55080	15.30	540	62100	17.25	533
55260	15.35	540	62280	17.30	533
55440	15.40	540	62460	17.35	533
55620	15.45	540	62640	17.40	533
55800	15.50	537	62820	17.45	530
55980	15.55	540	63000	17.50	530
56160	15.60	540	63180	17.55	530
56340	15.65	540	63360	17.60	530
56520	15.70	540	63540	17.65	530
56700	15.75	537	63720	17.70	530
56880	15.80	537	63900	17.75	530
57060	15.85	540	64080	17.80	530
57240	15.90	537	64260	17.85	530
57420	15.95	537	64440	17.90	530

continued

continued

Time (sec)	Time (hr)	Flow Rate (ml/min)	Time (sec)	Time (hr)	Flow Rate (ml/min)
64620	17.95	530	74520	20.70	513
64800	18.00	530	74700	20.75	513
64980	18.05	530	74880	20.80	513
65160	18.10	530	75060	20.85	513
65340	18.15	527	75240	20.90	513
65520	18.20	527	75420	20.95	513
65700	18.25	527	75600	21.00	517
65880	18.30	527	75780	21.05	513
66060	18.35	527	75960	21.10	517
66240	18.40	527	76140	21.15	513
66420	18.45	527	76320	21.20	513
66600	18.50	527	76500	21.25	513
66780	18.55	527	76680	21.30	513
66960	18.60	527	76860	21.35	513
70020	19.45	517	77040	21.40	513
70200	19.50	517	77220	21.45	510
70380	19.55	517	77400	21.50	513
70560	19.60	517	77580	21.55	510
70740	19.65	517	77760	21.60	513
70920	19.70	517	77940	21.65	513
71100	19.75	513	78120	21.70	513
71280	19.80	520	78300	21.75	510
71460	19.85	517	78480	21.80	510
71640	19.90	517	78660	21.85	510
71820	19.95	517	78840	21.90	510
72000	20.00	517	79020	21.95	510
72180	20.05	517	79200	22.00	510
72360	20.10	517	79380	22.05	510
72540	20.15	517	79560	22.10	510
72720	20.20	517	79740	22.15	510
72900	20.25	513	79920	22.20	510
73080	20.30	513	80100	22.25	510
73260	20.35	513	80280	22.30	506
73440	20.40	513	80460	22.35	506
73620	20.45	513	80640	22.40	506
73800	20.50	513	80820	22.45	506
73980	20.55	513	81000	22.50	510
74160	20.60	513	81180	22.55	510
74340	20.65	513	81360	22.60	510
continued			continued		

Time (sec)	Time (hr)	Flow Rate (ml/min)
81540	22.65	506
81720	22.70	506
81900	22.75	506
82080	22.80	503
82260	22.85	503
82440	22.90	503
82620	22.95	503
82800	23.00	503
82980	23.05	503
83160	23.10	503
83340	23.15	503
83520	23.20	503
83700	23.25	503
83880	23.30	503
84060	23.35	503
84240	23.40	503
84420	23.45	503
84600	23.50	503
84780	23.55	503
84960	23.60	503
85140	23.65	503
85320	23.70	503
85500	23.75	503
85680	23.80	503
85860	23.85	503
86040	23.90	503
86220	23.95	503
86400	24.00	503

**APPENDIX B. SIMPLIFIED DATA of PUMPING RATE
vs TIME, USED for ANALYSIS**

Test #1, Simplified pumping rate data
(for data analysis)

Time sec.	Time hr	Flow rate ml/sec.	Time sec.	Time hr	Flow rate ml/sec.
0	0.00	45.13	10620	2.95	16.12
150	0.04	44.67	11220	3.12	15.93
270	0.08	41.89	11820	3.28	15.78
360	0.10	35.00	12420	3.45	15.65
450	0.13	31.62	13020	3.62	15.50
660	0.18	28.54	13620	3.78	15.33
900	0.25	27.33	14220	3.95	15.18
1140	0.32	26.29	14820	4.12	15.03
1380	0.38	25.25	15420	4.28	14.90
1620	0.45	24.58	16020	4.45	14.75
1860	0.52	24.08	16620	4.62	14.62
2100	0.58	23.58	17220	4.78	14.50
2340	0.65	22.90	17820	4.95	14.37
2640	0.73	22.33	18420	5.12	14.30
2940	0.82	21.80	19020	5.28	14.22
3240	0.90	21.23	19620	5.45	14.15
3540	0.98	20.87	20220	5.62	14.03
3840	1.07	20.50	20820	5.78	13.95
4140	1.15	20.27	21420	5.95	13.87
4440	1.23	20.00	22020	6.12	13.75
4740	1.32	19.77	22620	6.28	13.63
5040	1.40	19.23	23220	6.45	13.53
5340	1.48	19.07	23820	6.62	13.42
5640	1.57	18.72	24420	6.78	13.28
6000	1.67	18.53	25020	6.95	13.30
6300	1.75	18.40	25620	7.12	13.25
6600	1.83	18.13	26220	7.28	13.22
6900	1.92	17.97	26820	7.45	13.08
7200	2.00	17.80	27420	7.62	13.02
7500	2.08	17.55	28020	7.78	12.95
7920	2.20	17.43	28620	7.95	12.88
8220	2.28	17.30	29220	8.12	12.82
8520	2.37	17.20	29820	8.28	12.82
8820	2.45	17.13	30420	8.45	12.68
9120	2.53	16.83	31020	8.62	12.63
9420	2.62	16.70	31620	8.78	12.53
9720	2.70	16.70	32220	8.95	12.50
10020	2.78	16.35	32820	9.12	12.50
continued			34380	9.55	12.50

Test #2, Simplified pumping rate data
(for data analysis)

Time sec.	Time hr	flow rate ml/sec.	Time sec.	Time hr	flow rate ml/sec.
180	0.05	42.78	15840	4.40	11.69
300	0.08	41.25	16440	4.57	11.64
420	0.12	38.25	17040	4.73	11.52
540	0.15	24.42	17640	4.90	11.44
660	0.18	23.34	18240	5.07	11.36
840	0.23	22.17	18840	5.23	11.29
1080	0.30	21.04	19440	5.40	11.19
1320	0.37	20.12	20040	5.57	11.11
1560	0.43	19.41	20700	5.75	11.04
1800	0.50	18.83	21600	6.00	10.89
2040	0.57	18.33	22500	6.25	10.73
2280	0.63	17.91	23400	6.50	10.67
2520	0.70	17.53	24300	6.75	10.57
2820	0.78	17.19	25200	7.00	10.47
3120	0.87	16.69	26100	7.25	10.43
3420	0.95	16.42	27000	7.50	10.36
3840	1.07	16.06	27900	7.75	10.32
4440	1.23	15.62	28800	8.00	10.24
5040	1.40	15.20	29700	8.25	10.18
5640	1.57	14.82	30600	8.50	10.07
6240	1.73	14.44	31500	8.75	10.01
6840	1.90	14.21	32400	9.00	9.96
7440	2.07	13.93	33300	9.25	9.89
8040	2.23	13.70	34200	9.50	9.84
8640	2.40	13.48	35100	9.75	9.78
9240	2.57	13.18	36000	10.00	9.77
9840	2.73	12.91	36900	10.25	9.76
10440	2.90	12.84	37800	10.50	9.73
11040	3.07	12.67	38700	10.75	9.69
11640	3.23	12.54	39600	11.00	9.64
12240	3.40	12.39	40500	11.25	9.61
12840	3.57	12.24	41400	11.50	9.52
13440	3.73	12.14	42300	11.75	9.52
14040	3.90	12.04	43200	12.00	9.50
14640	4.07	11.94	44100	12.25	9.44
15240	4.23	11.77	45000	12.50	9.35
continued			continued		

Time sec.	Time hr	flow rate ml/sec.
45900	12.75	9.31
46800	13.00	9.30
47700	13.25	9.26
48600	13.50	9.20
49500	13.75	9.19
51300	14.25	9.18
53100	14.75	9.11
54900	15.25	9.03
56700	15.75	8.96
58500	16.25	8.92
60300	16.75	8.87
62100	17.25	8.85
63900	17.75	8.81
65700	18.25	8.78
70380	19.55	8.62
72180	20.05	8.57
73980	20.55	8.53
75780	21.05	8.52
77580	21.55	8.51
79380	22.05	8.48
81180	22.55	8.44
86400	24.00	8.38

**APPENDIX C. DATA of OBSERVED DRAWDOWN and
PREDICTED DRAWDOWN vs TIME**

Well #1

Test #1

Time hr	O.D. ^a cm	P.D. ^b cm
0.01	0.03	0.00
0.03	1.52	0.02
0.05	3.35	0.17
0.07	5.18	0.63
0.09	6.71	1.40
0.13	10.06	2.94
0.17	10.06	4.62
0.21	10.97	6.38
0.27	12.80	8.35
0.33	14.02	10.19
0.42	15.24	12.09
0.57	17.07	14.73
0.74	18.59	16.93
0.91	19.51	18.54
1.08	20.12	19.75
1.35	21.64	21.29
1.68	22.56	22.63
2.01	23.47	23.61
2.67	24.69	25.06
3.97	26.82	26.73
4.98	26.52	27.59
5.97	27.13	28.27
6.98	29.26	28.78
7.96	29.87	29.23
9.41	30.78	29.80

Test #2

Time hr	O.D. cm	P.D. cm
0.04	0.30	0.00
0.05	1.83	0.01
0.07	2.44	0.01
0.09	3.35	0.02
0.11	3.96	0.03
0.13	4.57	0.06
0.15	5.18	0.12
0.18	5.79	0.27
0.21	6.40	0.51
0.26	7.01	1.02
0.31	7.92	1.60
0.38	8.53	2.55
0.44	9.14	3.50
0.62	10.97	5.76
0.83	12.19	8.02
1.05	13.11	9.94
1.37	14.63	12.18
1.80	15.85	14.52
2.39	17.68	16.88
3.08	18.59	18.85
4.30	21.03	21.22
5.08	21.95	22.31
6.07	23.16	23.42
7.13	24.08	24.33
8.14	24.69	25.05
9.61	25.91	25.94
11.12	27.13	26.71
13.06	27.74	27.59
15.11	28.65	28.36
17.81	29.57	29.25
20.92	30.18	30.17
23.87	30.78	30.93

^aO.D.: observed drawdown

^bP.D.: predicted drawdown

Well #2

Test #1

Time hr	O.D. cm	P.D. cm
0.10	3.66	0.49
0.14	4.88	1.18
0.18	6.40	2.18
0.22	7.32	3.27
0.29	8.53	4.79
0.34	9.45	6.03
0.43	10.67	7.65
0.58	12.19	9.84
0.76	13.41	11.86
0.93	14.33	13.42
1.09	14.94	14.57
1.37	16.46	16.14
1.69	17.68	17.55
2.02	18.29	18.61
2.68	19.51	20.20
3.98	21.64	22.12
5.00	22.86	23.14
5.98	23.77	23.92
7.00	24.69	24.57
7.98	25.60	25.11
9.42	26.21	25.79

Test #2

Time hr	O.D. cm	P.D. cm
0.16	2.44	0.05
0.19	3.35	0.11
0.22	3.35	0.21
0.27	3.96	0.45
0.32	4.57	0.76
0.39	5.49	1.32
0.45	5.79	1.92
0.63	7.01	3.52
0.84	8.23	5.20
1.06	9.14	6.75
1.38	10.67	8.63
1.81	11.89	10.63
2.40	13.41	12.75
3.09	14.63	14.56
4.31	16.76	16.78
5.12	17.68	17.86
6.09	18.90	18.90
7.16	19.81	19.81
8.18	20.42	20.52
9.64	21.34	21.39
11.14	22.56	22.15
13.09	23.16	23.02
15.14	24.08	23.79
17.83	24.99	24.67
20.94	25.60	25.59
23.88	26.52	26.34

Well #3

Test #1

Time hr	O.D. cm	P.D. cm
0.23	0.91	0.22
0.29	1.83	0.47
0.35	1.83	0.78
0.44	2.44	1.29
0.59	3.35	2.22
0.76	3.96	3.27
0.93	4.88	4.23
1.09	5.18	5.03
1.35	6.40	6.15
1.70	7.62	7.40
2.02	8.23	8.37
2.68	9.75	9.91
3.99	11.58	12.00
5.00	12.80	13.17
5.99	14.02	14.08
7.00	14.94	14.89
7.98	15.85	15.55
9.43	16.76	16.41

Test #2

Time hr	O.D. cm	P.D. cm
0.23	0.00	0.03
0.28	0.61	0.05
0.32	0.61	0.08
0.39	0.91	0.15
0.46	1.22	0.26
0.64	1.83	0.70
0.84	2.13	1.30
1.06	2.74	2.00
1.38	3.96	2.95
1.81	4.57	4.10
2.40	5.79	5.47
3.09	7.01	6.74
4.31	8.23	8.42
5.15	9.14	9.30
6.11	9.75	10.15
7.17	10.67	10.92
8.18	11.28	11.54
9.66	12.80	12.33
11.16	13.11	13.00
13.11	13.72	13.78
15.16	14.63	14.48
17.84	15.54	15.30
20.94	16.15	16.15
23.89	16.76	16.86

Well #4

Test #1

Time hr	O.D. cm	P.D. cm
0.35	0.61	0.23
0.44	0.91	0.41
0.59	1.83	0.82
0.76	1.83	1.39
0.94	2.44	1.99
1.10	2.13	2.52
1.37	3.96	3.41
1.70	4.57	4.34
2.03	5.18	5.16
2.69	6.40	6.53
3.99	8.23	8.52
5.01	9.45	9.69
5.99	10.36	10.62
7.01	11.58	11.45
7.99	12.50	12.14
9.43	13.11	13.05

Test #2

Time hr	O.D. cm	P.D. cm
0.32	0.30	0.04
0.39	0.00	0.07
0.46	0.61	0.10
0.64	0.61	0.27
0.84	0.91	0.56
1.07	1.52	0.94
1.39	2.13	1.53
1.81	2.74	2.28
2.40	3.66	3.23
3.10	4.27	4.17
4.32	5.18	5.49
5.16	6.10	6.20
6.12	6.71	6.90
7.18	7.32	7.55
8.19	7.92	8.09
9.67	9.14	8.77
11.17	9.45	9.36
13.12	10.06	10.05
15.17	10.97	10.68
17.84	11.28	11.42
20.96	11.89	12.19
23.89	13.11	12.85

Well #6

Test #1

Time hr	O.D. cm	P.D. cm
0.02	2.44	0.13
0.04	9.45	0.42
0.06	13.11	1.58
0.08	15.85	3.33
0.11	17.68	5.64
0.14	19.20	8.46
0.18	20.42	11.02
0.23	21.34	13.24
0.29	22.56	15.54
0.37	23.47	17.61
0.46	24.38	19.65
0.62	25.60	22.18
0.78	26.21	24.03
0.95	27.13	25.53
1.12	27.43	26.59
1.39	28.04	27.90
1.73	28.96	29.02
2.05	29.26	29.81
2.72	30.18	30.96
4.02	31.70	32.21
5.06	32.31	32.84
6.02	33.22	33.35
7.04	33.83	33.67
8.02	34.75	34.02
9.47	35.05	34.45

Test #2

Time hr	O.D. cm	P.D. cm
0.04	6.71	0.01
0.06	10.06	0.01
0.08	11.28	0.06
0.10	12.19	0.19
0.12	12.80	0.43
0.14	13.72	0.73
0.16	14.33	1.26
0.19	15.24	2.10
0.23	15.85	3.16
0.28	16.76	4.74
0.34	17.37	6.40
0.40	17.98	8.11
0.49	18.90	9.97
0.66	18.90	13.03
0.86	21.03	15.61
1.09	22.25	18.00
1.41	23.47	20.53
1.84	24.99	23.05
2.43	25.91	25.44
3.12	27.43	27.37
4.35	29.26	29.60
5.21	30.48	30.70
6.16	31.39	31.65
7.24	32.31	32.43
8.26	32.92	33.08
9.73	33.53	33.83
11.23	34.75	34.54
13.18	35.66	35.31
15.26	35.97	36.03
17.92	37.19	36.81
21.01	37.49	37.63
23.91	38.40	38.31

Well #7

Test #1

Time hr	O.D. cm	P.D. cm
0.11	5.18	0.57
0.15	6.40	1.26
0.19	7.32	2.24
0.23	7.92	3.36
0.30	9.14	4.76
0.37	9.75	6.19
0.47	11.28	7.74
0.62	12.50	9.83
0.78	13.41	11.48
0.96	14.02	12.96
1.13	14.63	14.08
1.39	15.85	15.49
1.74	17.07	16.86
2.06	17.37	17.84
2.73	18.59	19.34
4.03	20.42	21.17
5.06	21.64	22.16
6.03	22.86	22.91
7.04	23.77	23.53
8.02	24.69	24.06
9.47	25.30	24.73

Test #2

Time hr	O.D. cm	P.D. cm
0.17	4.27	0.11
0.20	4.88	0.23
0.23	5.49	0.43
0.28	6.10	0.81
0.34	6.71	1.38
0.41	7.32	2.15
0.49	7.92	3.09
0.67	9.14	4.93
0.86	10.06	6.61
1.09	10.97	8.34
1.42	12.19	10.29
1.84	13.72	12.33
2.43	14.94	14.41
3.13	16.15	16.21
4.35	18.29	18.37
5.21	19.20	19.48
6.17	20.42	20.46
7.24	21.03	21.32
8.27	21.64	22.01
9.74	22.56	22.84
11.24	23.77	23.58
13.18	24.69	24.41
15.27	25.30	25.16
17.93	26.21	26.01
21.02	26.82	26.89
23.91	27.74	27.60

Well #8

Test #1

Time hr	O.D. cm	P.D. cm
0.24	3.05	0.79
0.30	3.96	1.40
0.37	4.27	2.12
0.47	5.18	3.05
0.63	5.79	4.45
0.78	7.01	5.68
0.96	7.62	6.87
1.13	8.23	7.82
1.40	9.14	9.06
1.74	10.36	10.35
2.06	11.28	11.32
2.73	12.50	12.85
4.03	14.33	14.82
5.06	15.54	15.92
6.03	16.46	16.76
7.04	17.68	17.49
8.02	18.59	18.10
9.47	19.20	18.89

Test #2

Time hr	O.D. cm	P.D. cm
0.24	2.13	0.09
0.29	2.44	0.18
0.34	3.05	0.36
0.41	3.35	0.65
0.49	3.96	1.06
0.68	4.57	2.10
0.86	5.49	3.09
1.10	6.10	4.26
1.42	7.01	5.68
1.85	8.23	7.23
2.43	9.45	8.92
3.13	10.36	10.46
4.35	12.19	12.38
5.22	13.41	13.40
6.17	14.02	14.30
7.26	14.94	15.14
8.28	15.54	15.80
9.76	16.46	16.61
11.26	17.37	17.32
13.19	18.29	18.12
15.28	19.20	18.85
17.93	19.81	19.68
21.02	20.42	20.55
23.91	21.34	21.26

Well #9

Test #1

Time hr	O.D. cm	P.D. cm
0.38	0.91	0.42
0.47	1.52	0.72
0.63	1.83	1.32
0.79	2.74	1.94
0.97	3.05	2.63
1.13	3.66	3.23
1.40	4.27	4.11
1.74	5.18	5.08
2.07	5.79	5.87
2.73	7.01	7.18
4.04	8.53	9.03
5.07	9.75	10.12
6.03	10.67	10.95
7.05	11.58	11.71
8.03	12.80	12.35
9.48	13.72	13.19

Test #2

Time hr	O.D. cm	P.D. cm
0.35	0.91	0.08
0.42	0.91	0.15
0.50	1.22	0.26
0.69	1.52	0.63
0.87	2.13	1.06
1.10	2.74	1.63
1.42	3.05	2.40
1.85	3.96	3.32
2.43	4.57	4.39
3.13	5.49	5.43
4.35	6.71	6.81
5.22	7.32	7.57
6.18	8.23	8.26
7.27	8.84	8.93
8.28	9.45	9.45
9.77	10.36	10.12
11.27	10.67	10.70
13.21	11.28	11.37
15.28	12.19	11.99
17.94	12.80	12.71
21.03	13.41	13.46
23.92	14.02	14.10

Well #11

Test #1

Time hr	O.D. cm	P.D. cm
0.02	0.61	0.10
0.04	3.35	0.13
0.06	5.49	0.55
0.08	7.92	1.41
0.11	10.06	2.85
0.15	11.58	4.64
0.19	13.11	6.55
0.24	14.02	8.46
0.31	15.24	10.35
0.39	16.46	12.16
0.48	17.37	13.97
0.64	18.59	16.25
0.79	19.20	17.89
0.97	20.12	19.34
1.15	20.73	20.41
1.41	21.95	21.69
1.75	22.86	22.88
2.08	23.47	23.75
2.75	24.69	24.99
4.05	25.91	26.44
5.08	27.13	27.20
6.05	27.74	27.81
7.06	28.35	28.25
8.04	28.96	28.66
9.49	29.57	29.20

Test #2

Time hr	O.D. cm	P.D. cm
0.05	2.44	0.00
0.06	4.88	0.00
0.08	6.10	0.01
0.10	7.62	0.18
0.12	8.84	0.37
0.14	9.45	0.62
0.17	10.36	1.11
0.20	10.97	1.75
0.24	11.58	2.76
0.29	12.19	3.90
0.35	12.80	5.25
0.42	13.11	6.57
0.51	14.02	7.97
0.70	15.24	10.46
0.87	16.15	12.17
1.11	16.76	14.00
1.43	17.68	15.93
1.86	18.90	17.84
2.44	20.12	19.63
3.14	20.73	21.10
4.36	22.56	22.82
5.25	23.77	23.70
6.19	24.08	24.42
7.29	24.99	25.05
8.32	25.60	25.57
9.80	26.21	26.18
11.29	26.82	26.75
13.23	27.74	27.39
15.33	28.04	27.99
17.96	28.65	28.65
21.06	29.26	29.36
23.92	29.87	29.95

Well #12

Test #1

Time hr	O.D. cm	P.D. cm
0.12	1.22	0.09
0.15	1.83	0.23
0.20	2.44	0.49
0.25	2.74	0.92
0.31	3.66	1.51
0.39	4.27	2.23
0.49	4.57	3.09
0.64	5.49	4.35
0.80	6.10	5.38
0.98	7.01	6.42
1.16	7.32	7.29
1.41	8.53	8.30
1.76	9.75	9.41
2.09	10.06	10.25
2.76	11.28	11.55
4.05	12.80	13.23
5.09	14.02	14.19
6.06	14.94	14.93
7.07	15.54	15.58
8.04	16.46	16.12
9.50	17.07	16.84

Test #2

Time hr	O.D. cm	P.D. cm
0.17	1.83	0.04
0.20	2.13	0.06
0.25	2.13	0.13
0.29	2.44	0.26
0.35	2.74	0.48
0.42	3.05	0.79
0.51	3.35	1.20
0.70	4.27	2.15
0.88	4.57	2.94
1.11	5.49	3.89
1.44	6.10	5.00
1.87	6.71	6.20
2.45	7.62	7.45
3.15	8.53	8.58
4.37	9.75	10.00
5.26	10.67	10.76
6.19	11.28	11.41
7.31	12.19	12.05
8.33	12.50	12.53
9.81	13.41	13.14
11.29	13.72	13.68
13.24	14.33	14.30
15.33	14.94	14.89
17.96	15.54	15.55
21.07	16.15	16.26
23.93	16.76	16.84

Well #13

Test #1

Time hr	O.D. cm	P.D. cm
0.25	1.22	0.27
0.32	1.52	0.51
0.39	1.83	0.85
0.49	2.44	1.31
0.65	2.74	2.09
0.80	3.35	2.78
0.98	3.66	3.53
1.16	4.27	4.21
1.41	5.18	5.01
1.76	5.79	5.94
2.09	6.71	6.68
2.76	7.92	7.85
4.06	9.14	9.44
5.09	10.36	10.38
6.06	10.97	11.12
7.07	11.89	11.77
8.05	12.50	12.33
9.50	13.11	13.07

Test #2

Time hr	O.D. cm	P.D. cm
0.25	0.91	0.05
0.30	1.22	0.08
0.36	1.52	0.15
0.43	1.52	0.27
0.51	1.52	0.46
0.71	2.13	0.96
0.88	2.74	1.44
1.11	3.35	2.07
1.44	3.96	2.86
1.87	4.27	3.77
2.45	4.88	4.76
3.15	5.79	5.71
4.37	6.71	6.93
5.26	7.32	7.61
6.21	8.23	8.22
7.32	8.84	8.80
8.33	9.45	9.26
9.82	10.06	9.84
11.32	10.36	10.34
13.26	10.97	10.94
15.34	11.58	11.50
17.97	11.89	12.13
21.07	12.80	12.82
23.93	13.41	13.39

Well #14

Test #1

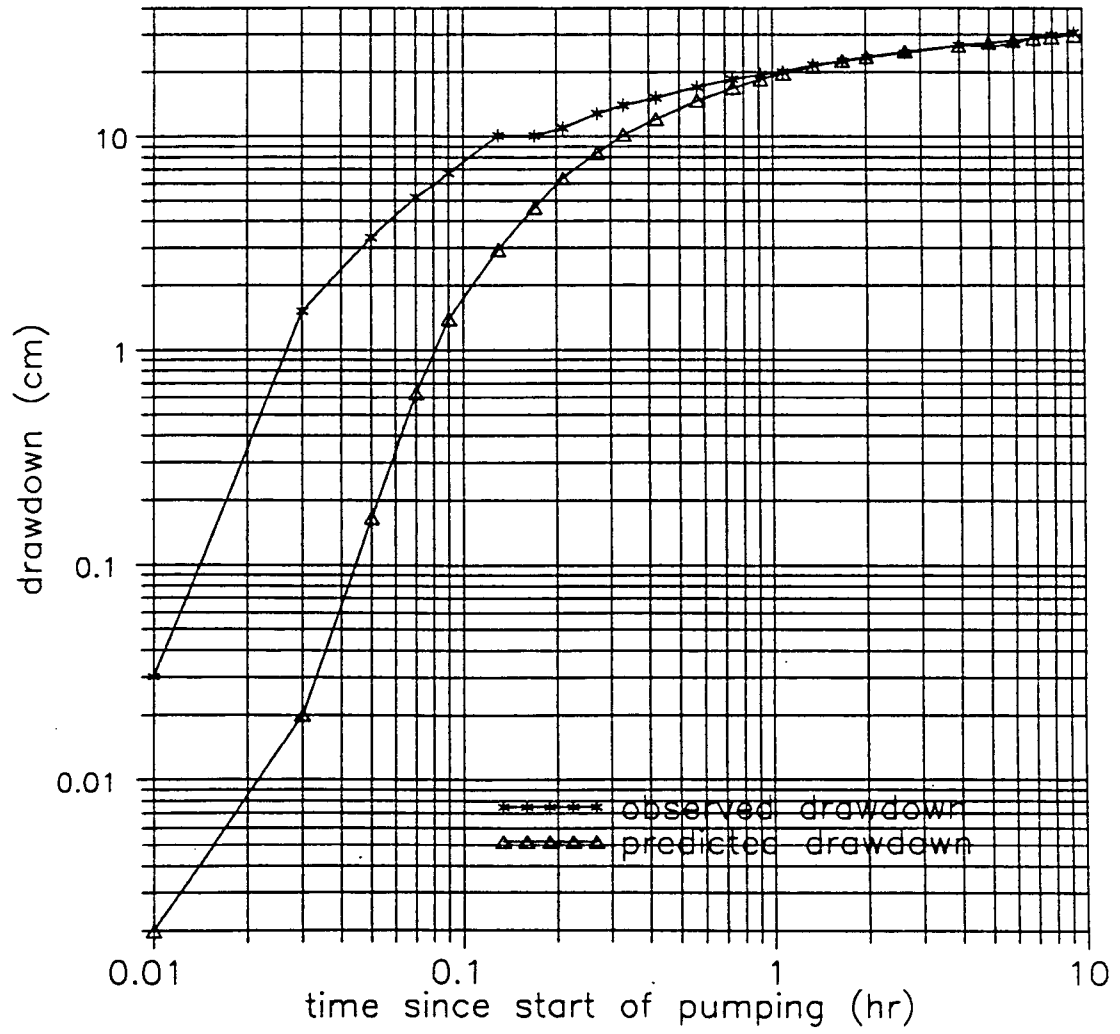
Time hr	O.D. cm	P.D. cm
0.40	0.61	0.37
0.49	0.91	0.61
0.65	1.22	1.04
0.80	1.52	1.47
0.98	2.13	1.96
1.17	2.44	2.43
1.42	3.05	3.01
1.76	3.96	3.71
2.10	4.27	4.28
2.76	5.18	5.23
4.06	6.40	6.59
5.09	7.01	7.42
6.07	7.92	8.08
7.08	8.84	8.68
8.05	9.45	9.21
9.51	10.06	9.92

Test #2

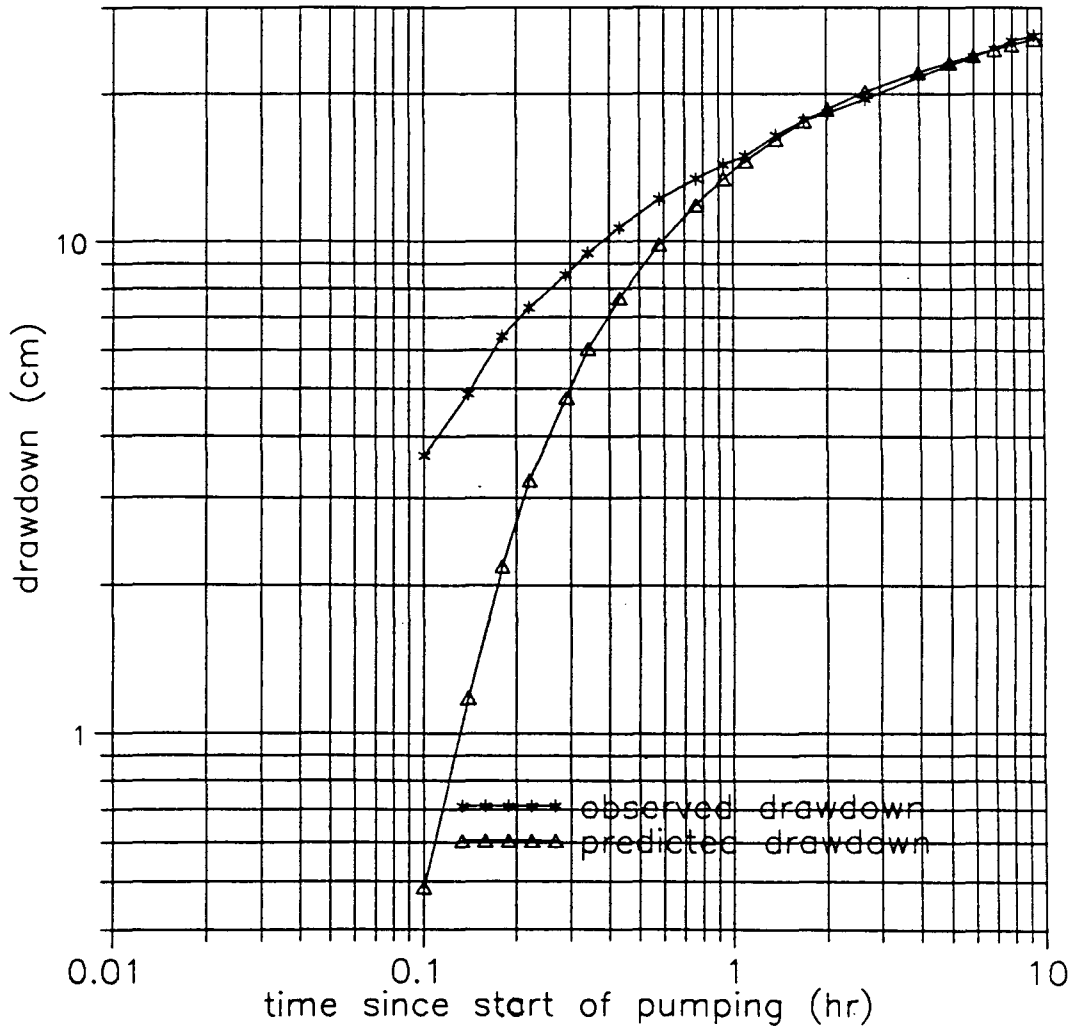
Time hr	O.D. cm	P.D. cm
0.36	0.91	0.08
0.43	0.91	0.14
0.52	0.91	0.23
0.71	1.22	0.50
0.88	1.52	0.78
1.12	1.83	1.18
1.44	2.13	1.69
1.87	2.44	2.30
2.45	3.05	3.00
3.15	3.66	3.69
4.38	4.57	4.61
5.28	5.18	5.13
6.21	5.49	5.60
7.32	6.10	6.07
8.34	6.40	6.44
9.83	7.01	6.91
11.32	7.32	7.34
13.27	7.92	7.84
15.34	8.23	8.32
17.98	8.84	8.88
21.08	9.45	9.49
23.93	10.06	10.00

APPENDIX D. CURVE FITTING DIAGRAMS in
LOG-LOG SCALE

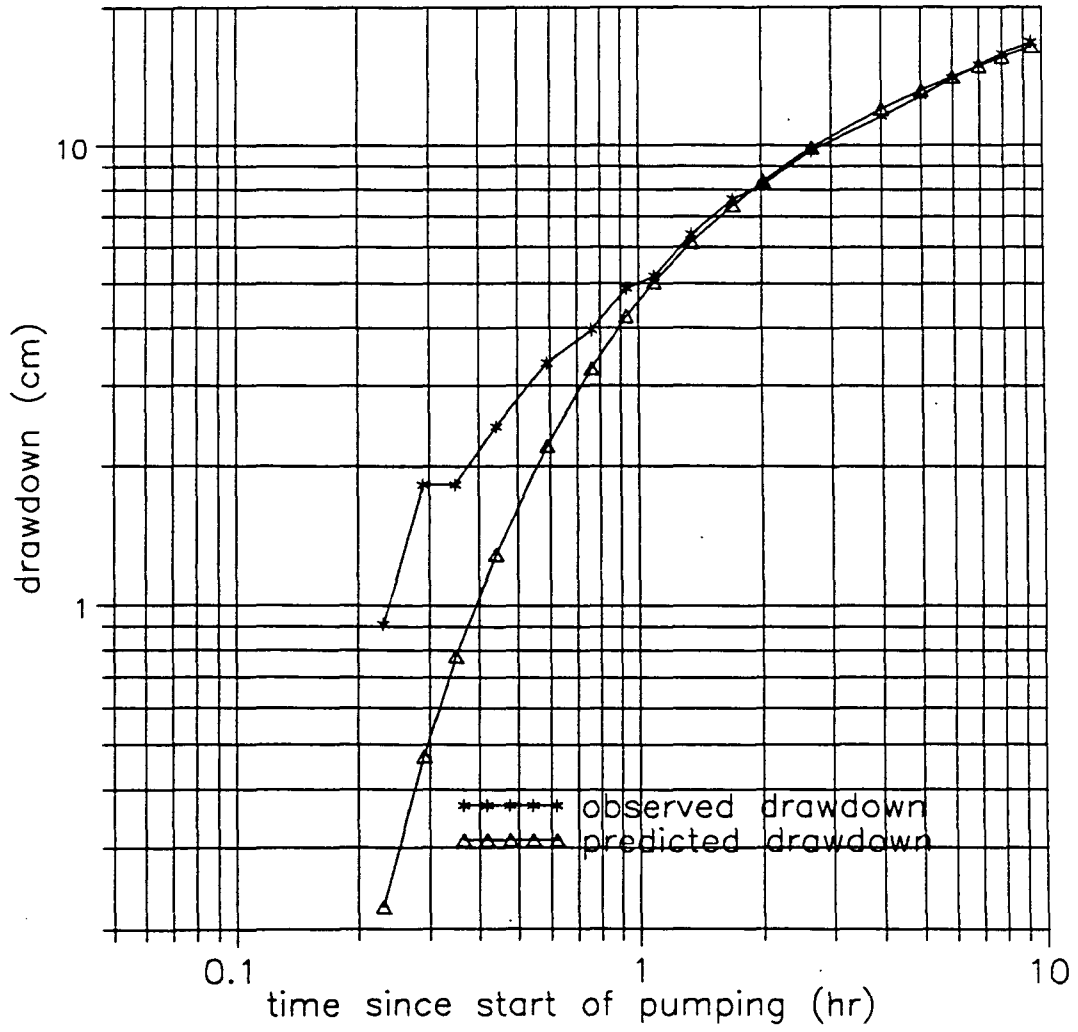
Test #1, Well 1



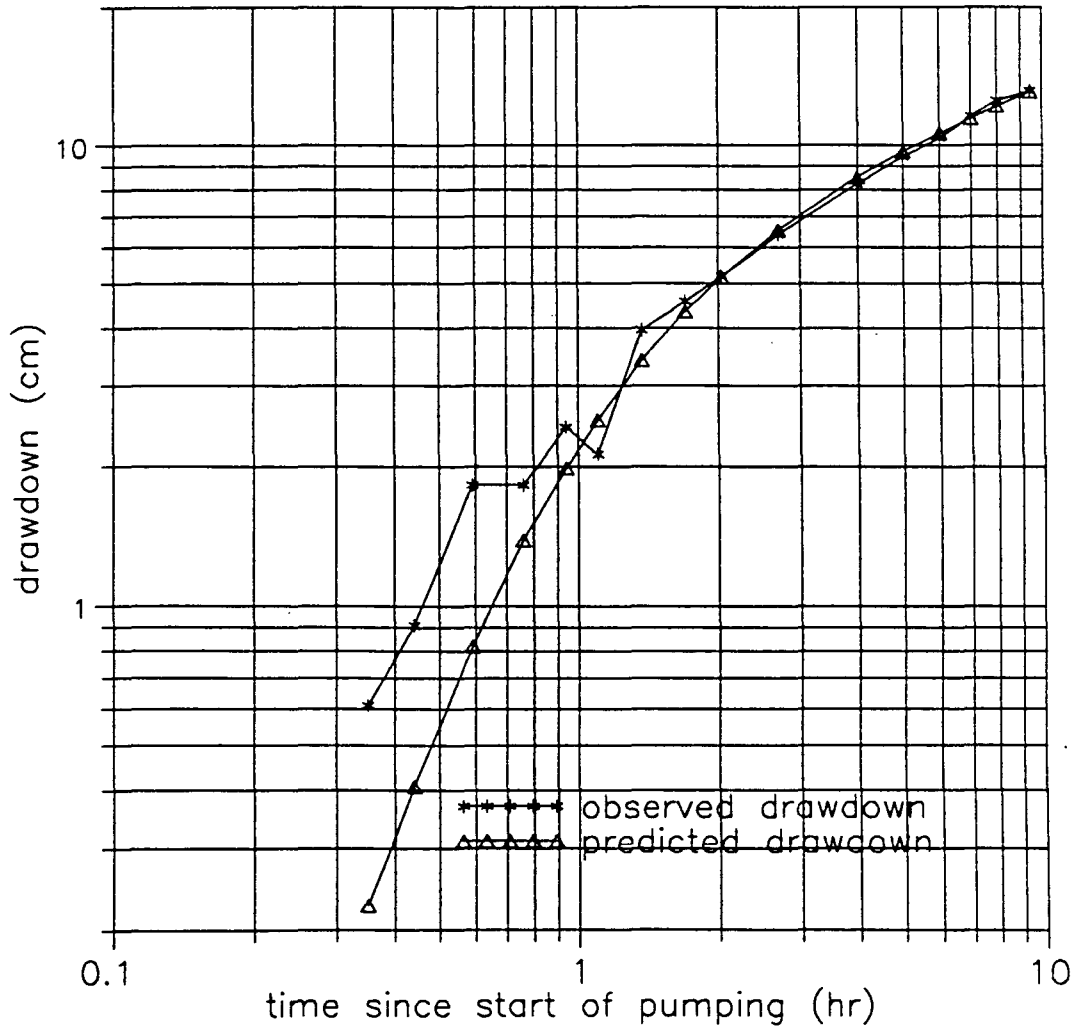
Test #1, Well 2



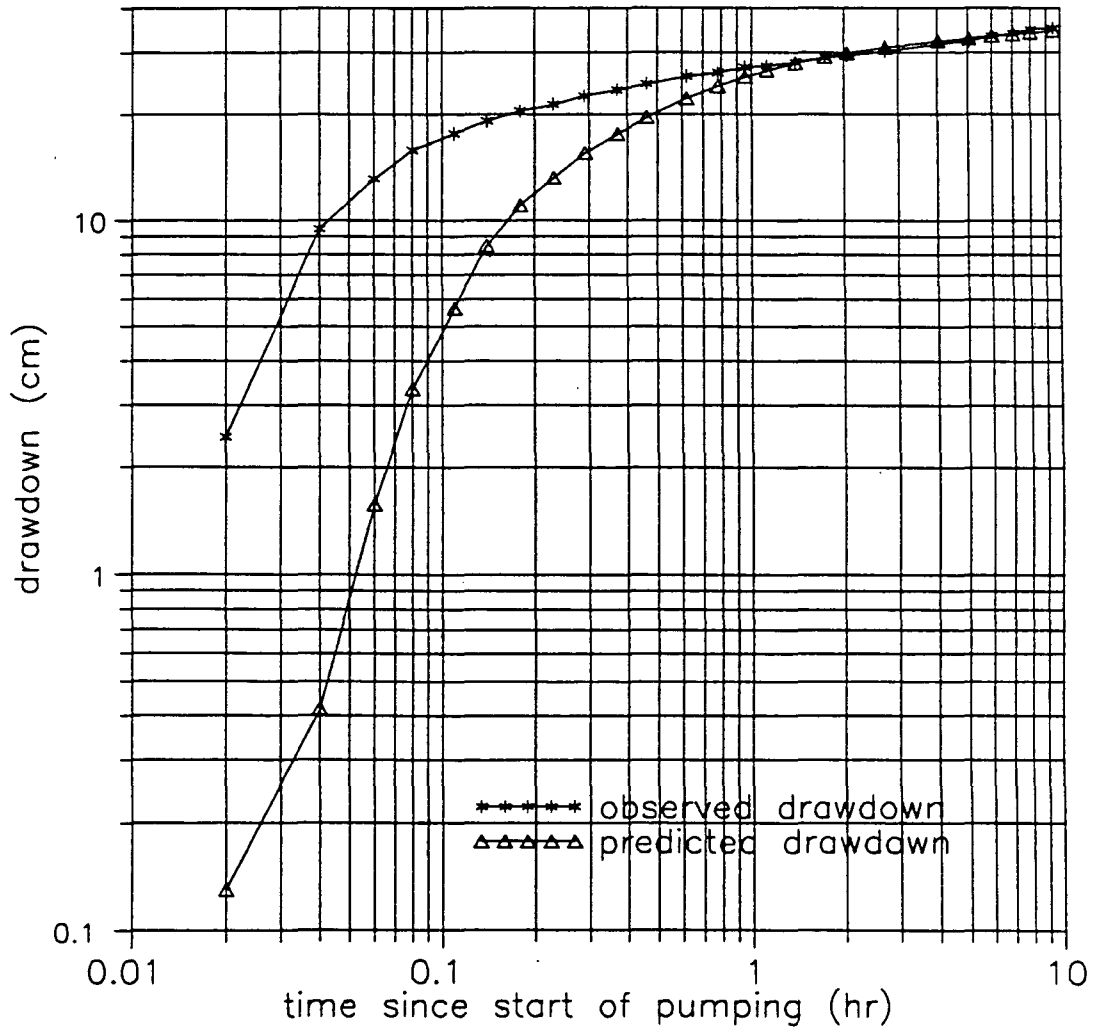
Test #1, Well 3



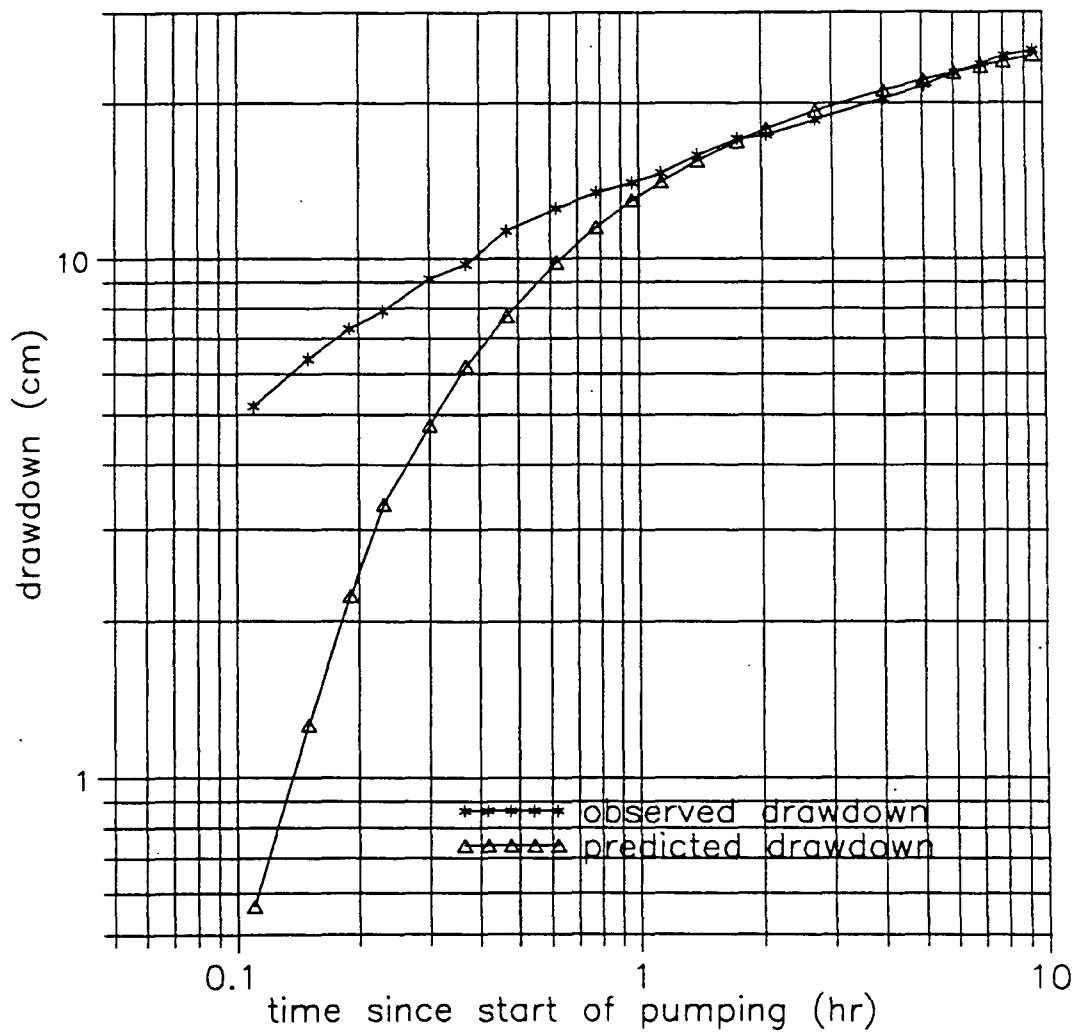
Test #1, Well 4



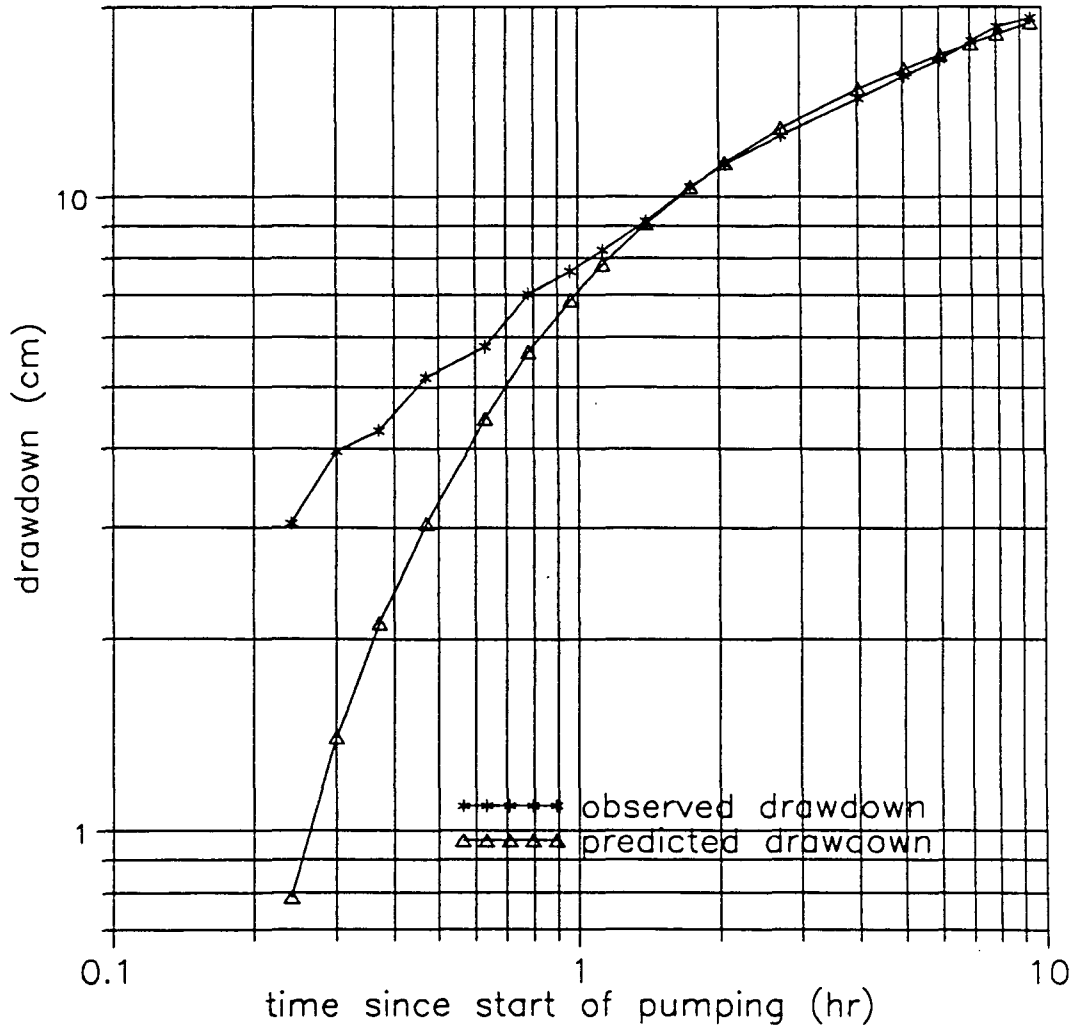
Test #1, Well 6



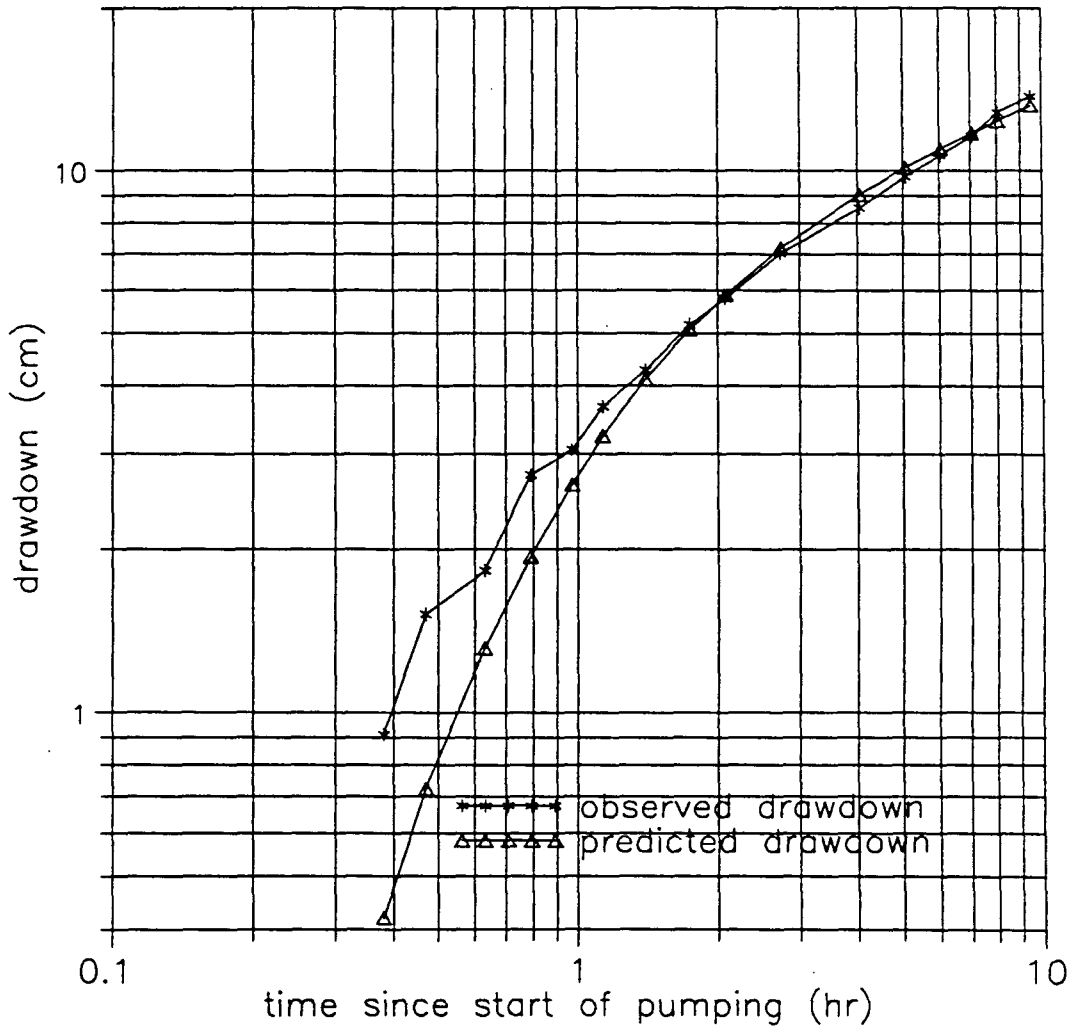
Test #1, Well 7



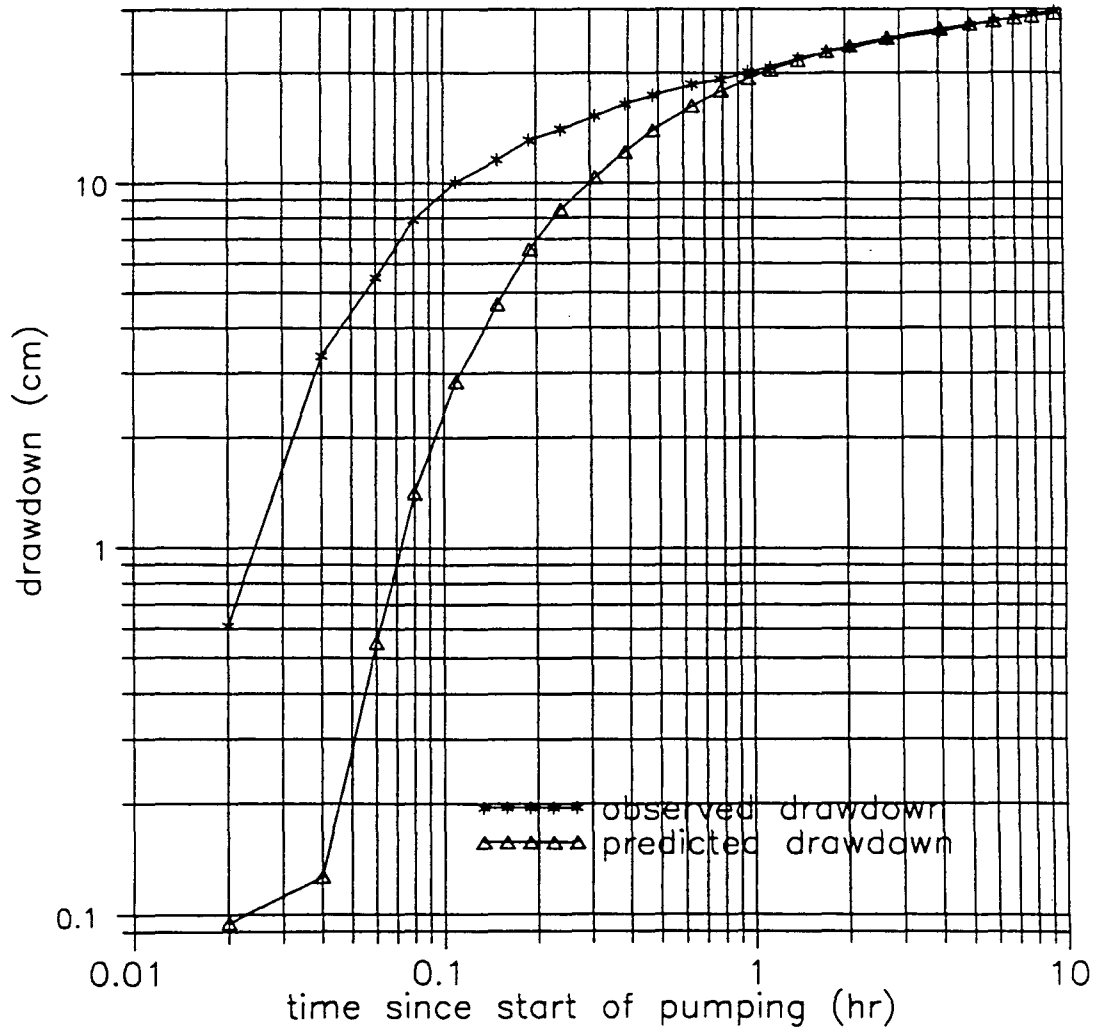
Test #1, Well 8



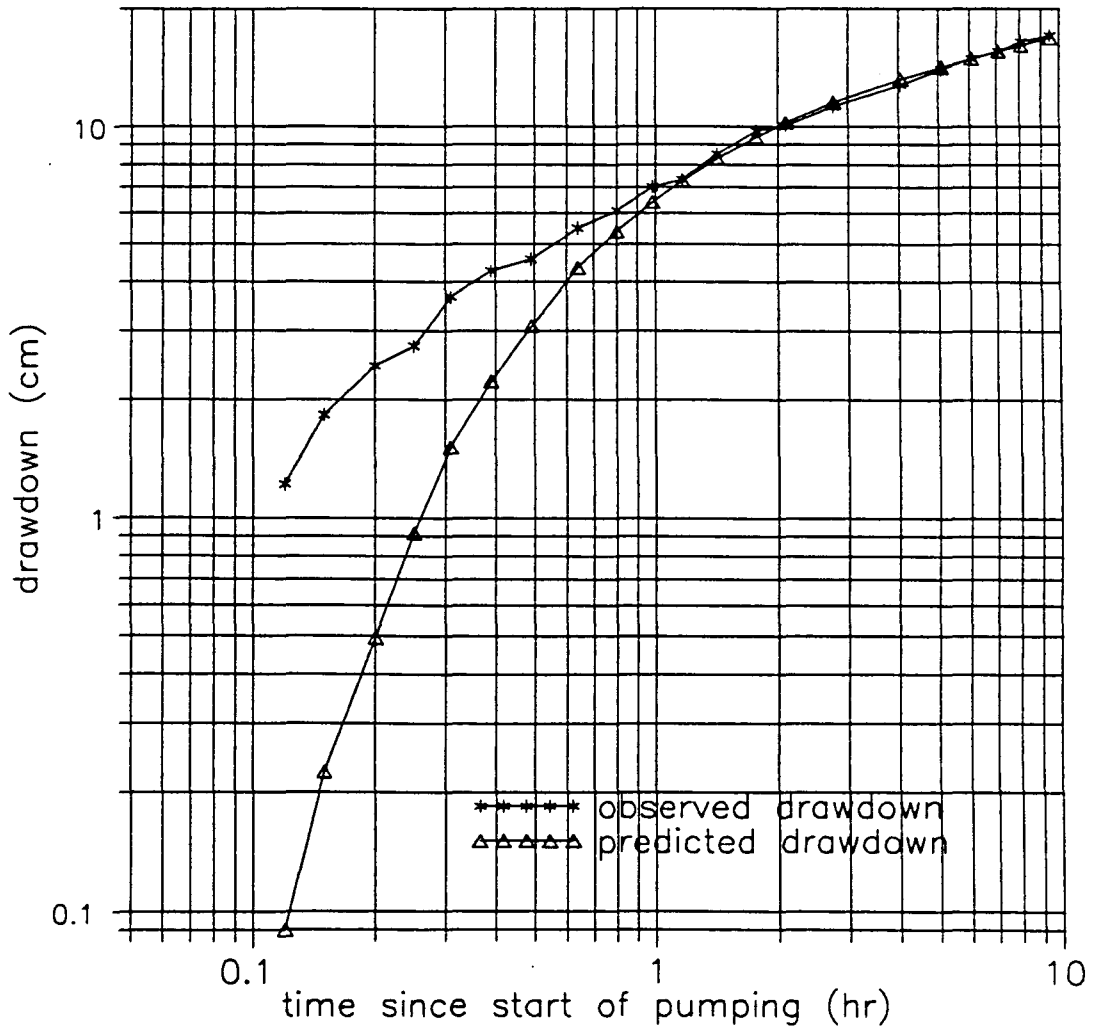
Test #1, Well 9



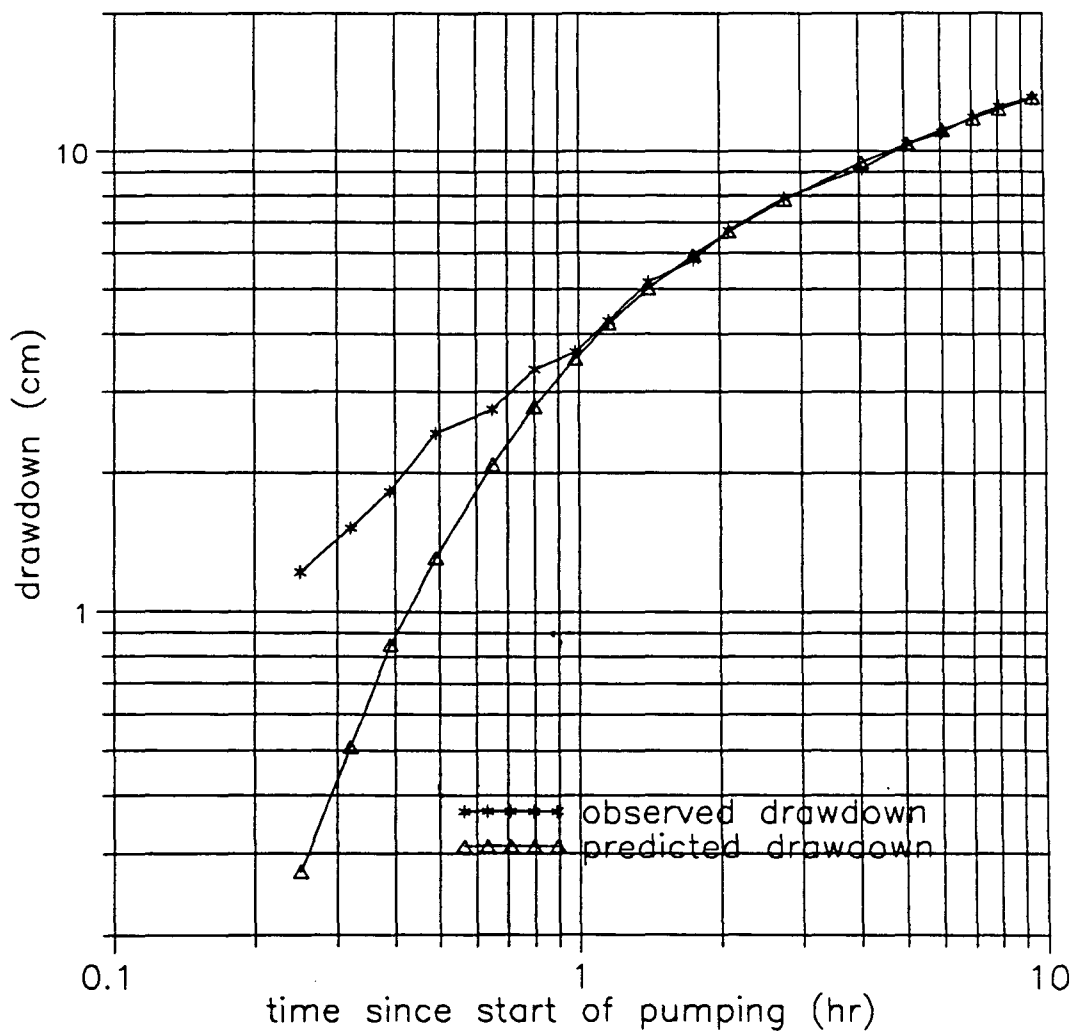
Test #1, Well 11



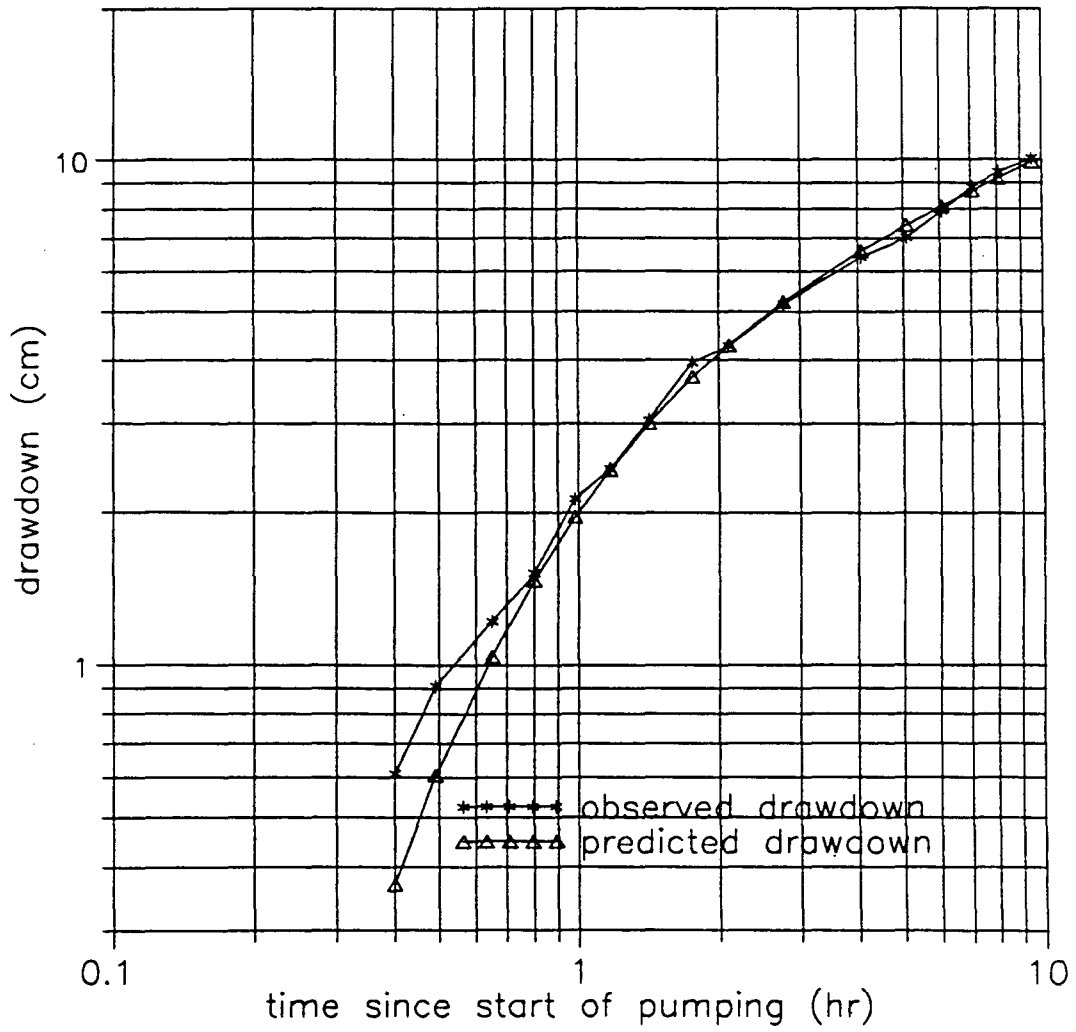
Test #1, Well 12



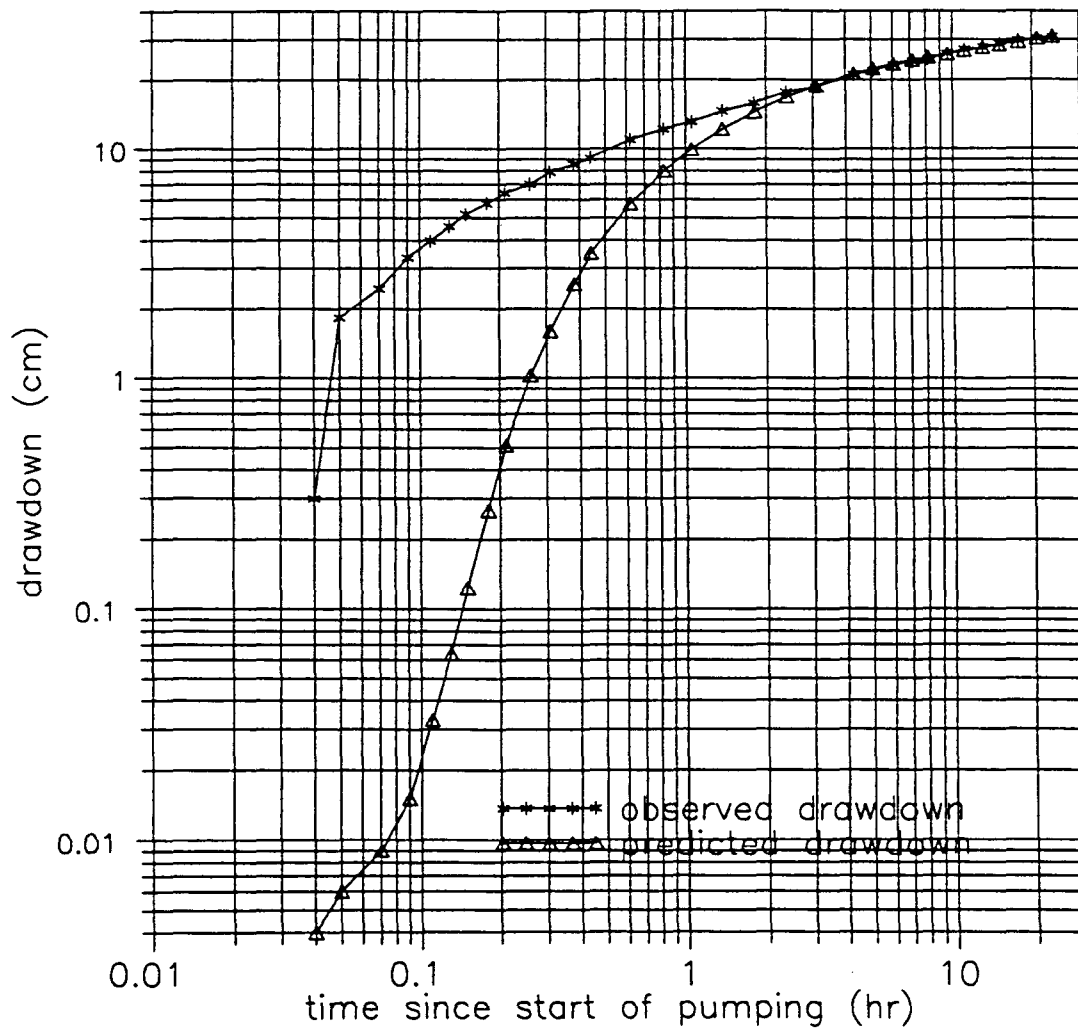
Test #1, Well 13



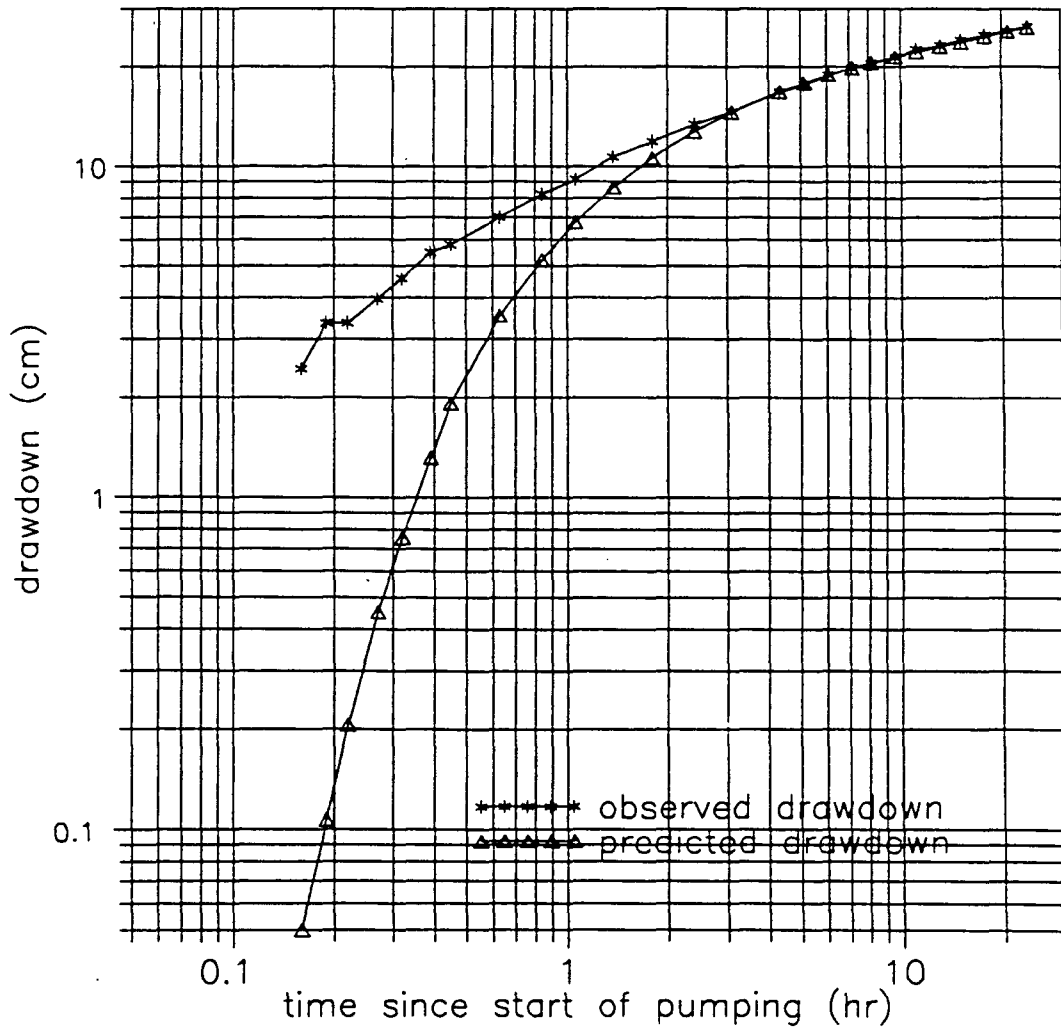
Test #1, Well 14



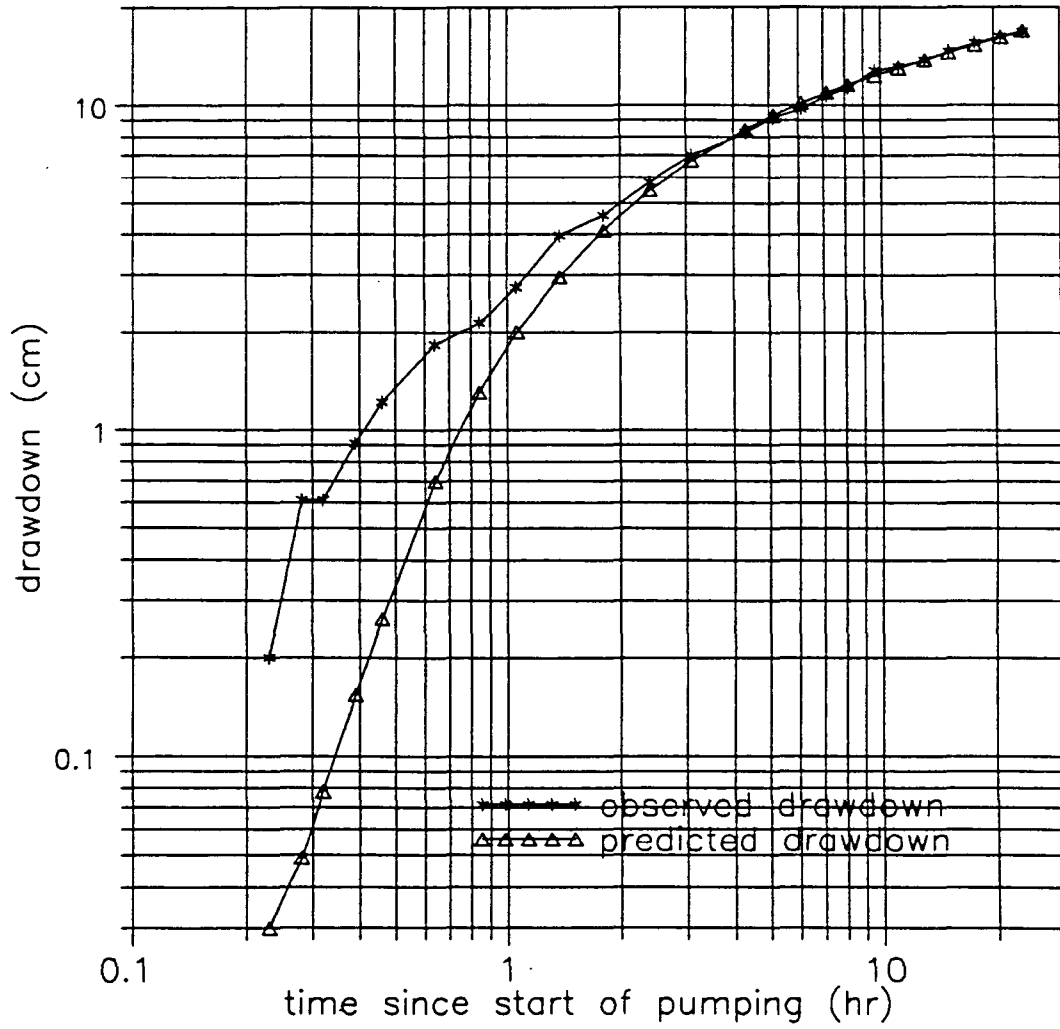
Test #2, Well 1



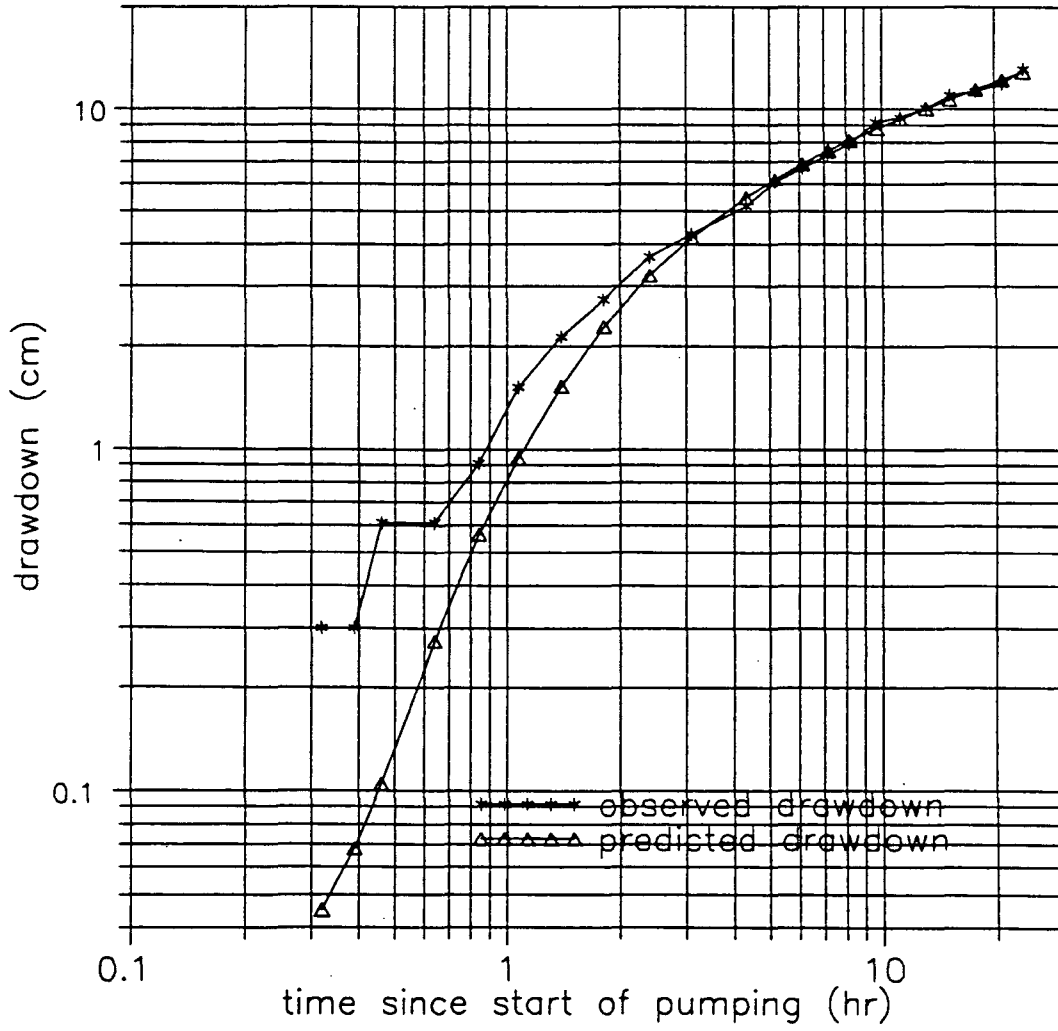
Test #2, Well 2



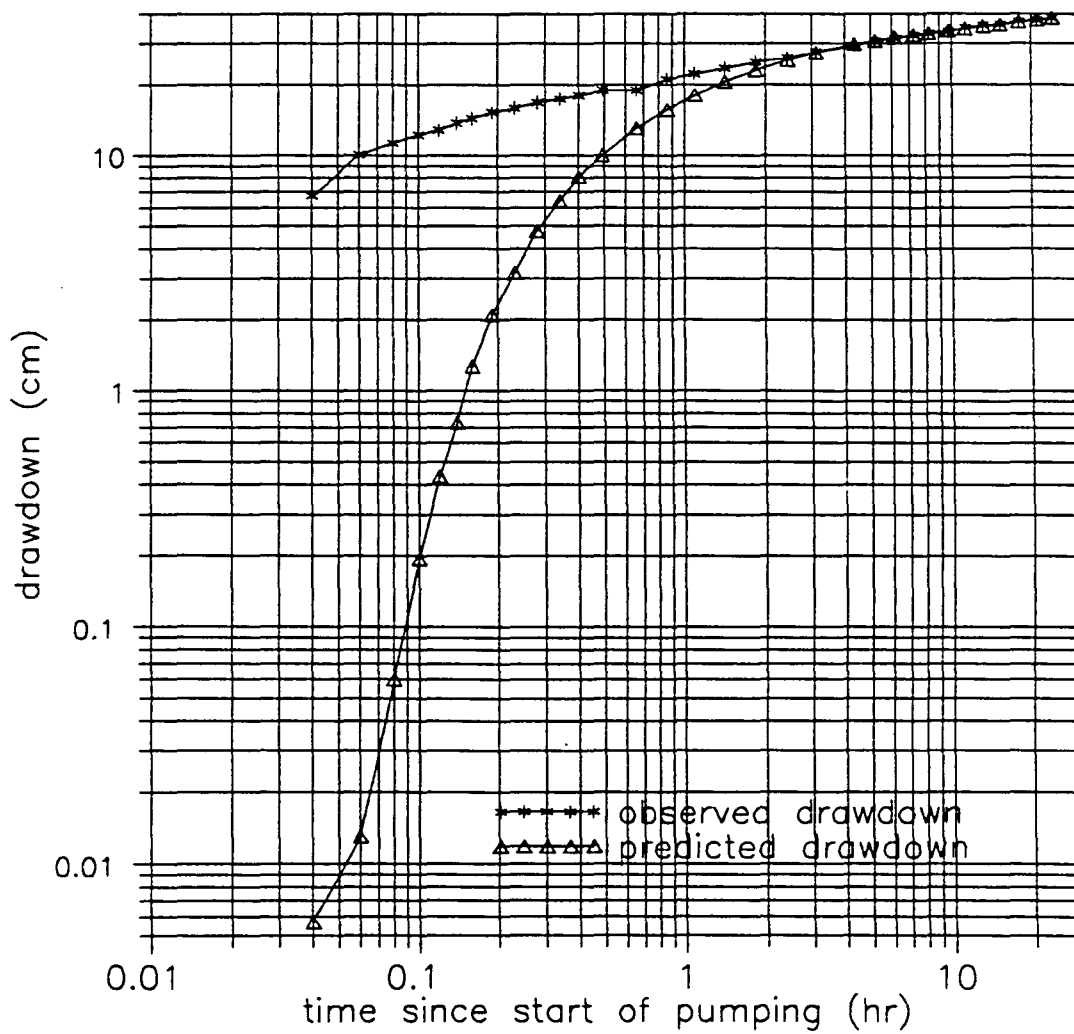
Test #2, Well 3



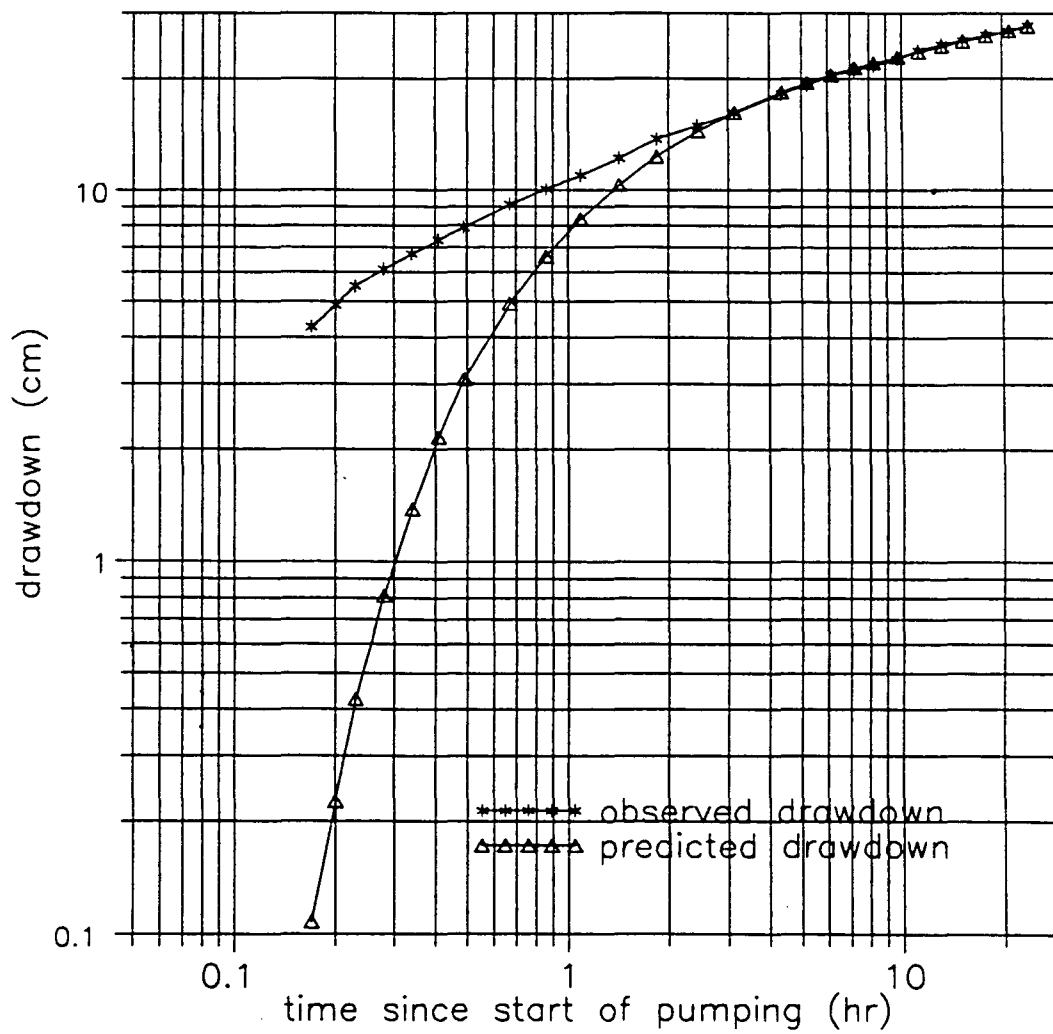
Test #2, Well 4



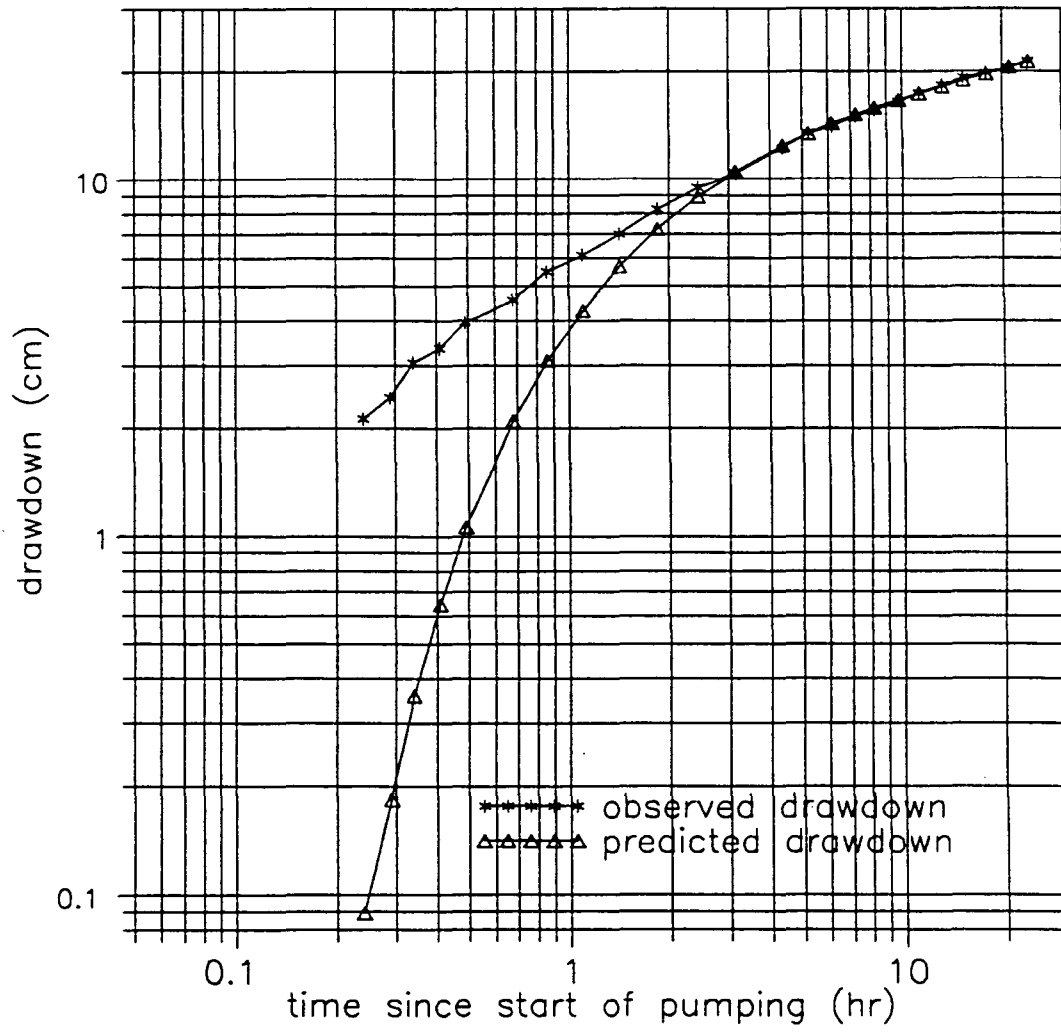
Test #2, Well 6



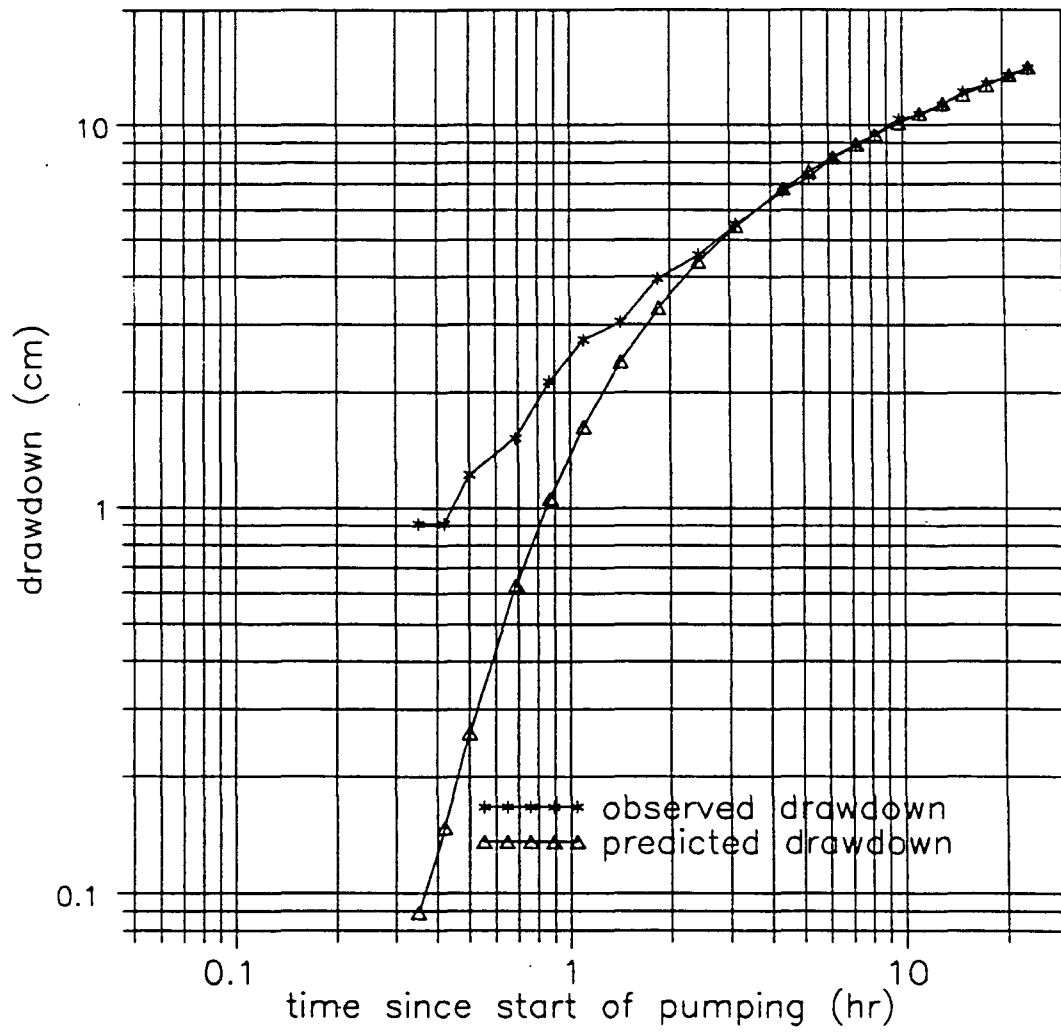
Test #2, Well 7



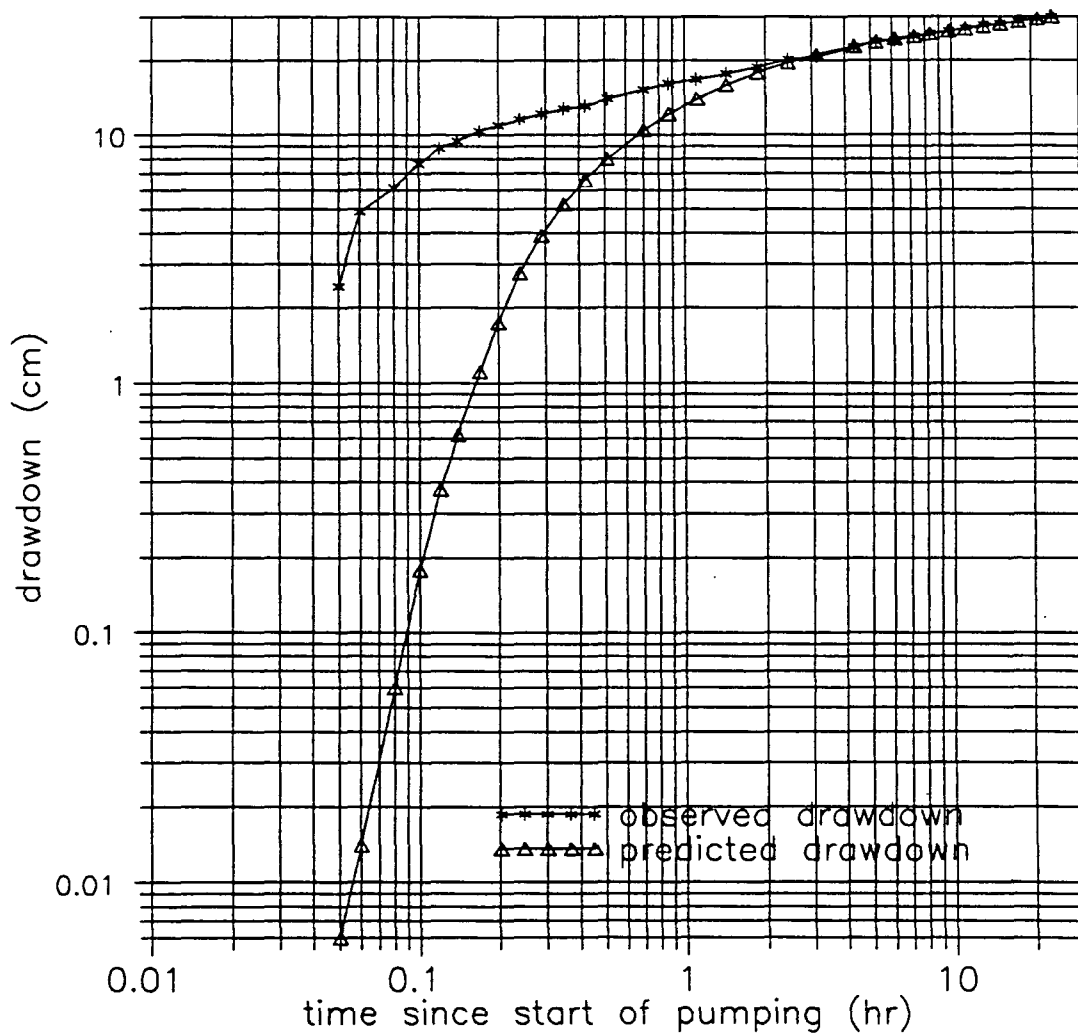
Test #2, Well 8



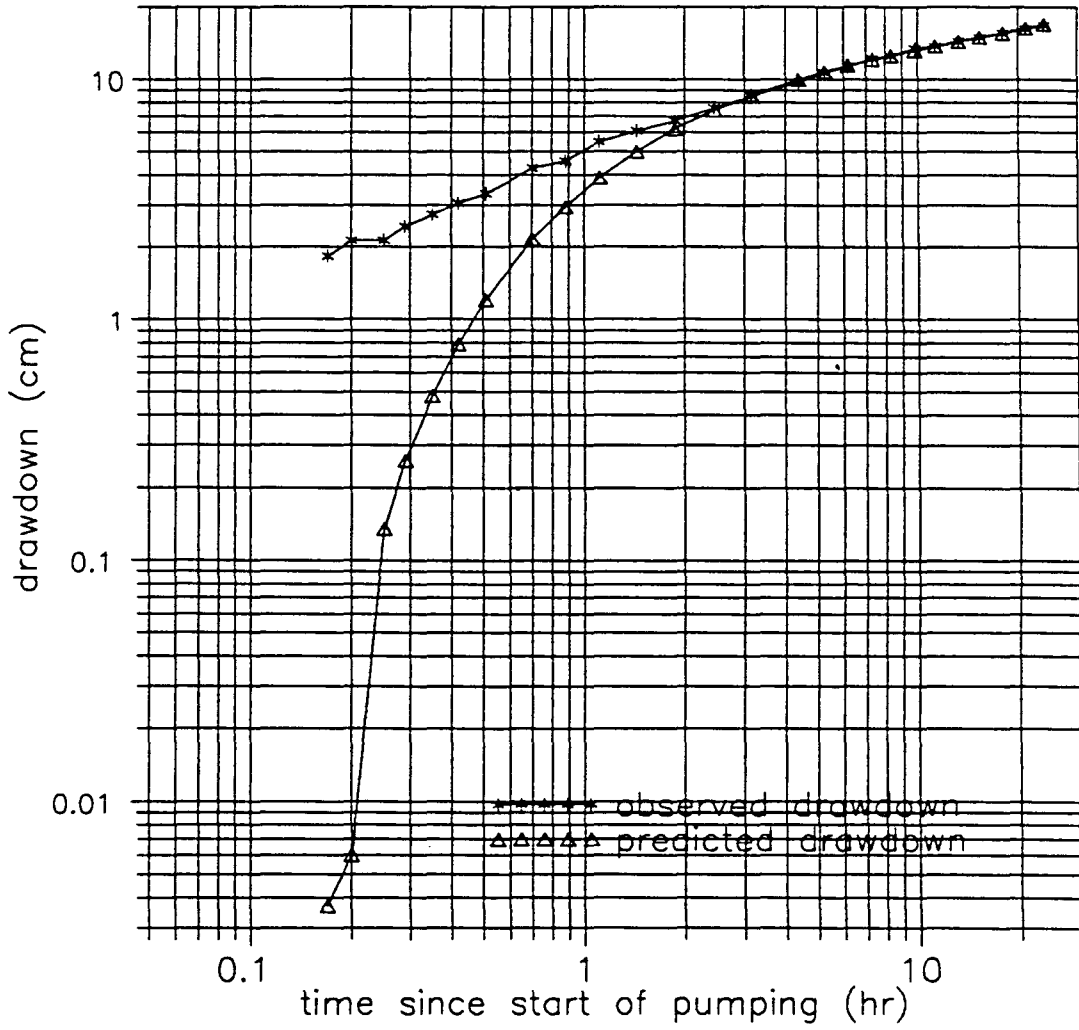
Test #2, Well 9



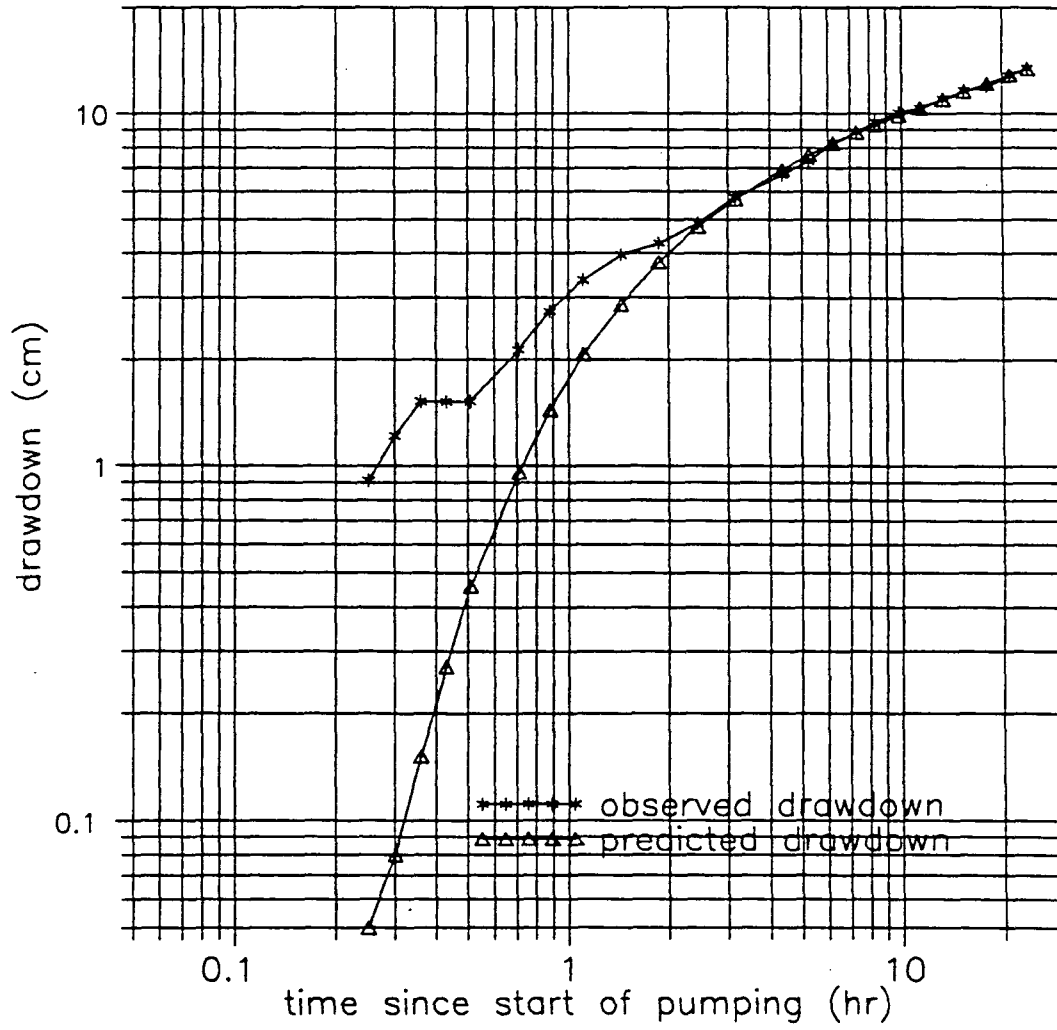
Test #2, Well 11



Test #2, Well 12



Test #2, Well 13



Test #2, Well 14

