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Low temperature heat capacity of  
lutetium and lutetium hydrogen alloys

by

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Signatures have been redacted for privacy

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## INTRODUCTION

The low temperature heat capacity of lutetium has been studied by several investigators<sup>1-5</sup> and many different values have been reported for the electronic specific heat constant,  $\gamma$ , and the Debye temperature,  $\theta_D$ . These values are listed in Table 1. In this light an accurate determination of the heat capacity (1 to 20 K) of high purity lutetium was attempted on two different electrotransport purified samples. Electrotransport purification is currently the only way to reduce interstitial impurity contents to low levels in lutetium.<sup>6</sup>

The low temperature heat capacity of most metals can be expressed as:

$$C(\text{total}) = C_l + C_e \quad (1)$$

where  $C_l$  is the lattice contribution to the heat capacity and  $C_e$  is the electronic contribution. The lattice contribution, according to the Debye model, (for  $T < \theta_D/50$ ) can be written<sup>7</sup>:

$$C_l = (12/5)\pi^4 rR(T/\theta_D)^3 = \beta T^3 \quad (2)$$

where  $r$  is number of atoms per molecule,  $R$  is the gas constant,  $T$  is the absolute temperature, and  $\theta_D$  is the Debye temperature. The important features are that the lattice heat capacity can be expressed with a single parameter,  $\theta_D$ , and that a connection can be made between thermal and elastic properties of metals.

Table 1. Survey of published heat capacity results for lutetium

| Investigator                      | $\gamma$ (mJ/g-atom K) | $\theta_D$ (K) | Conditions  |
|-----------------------------------|------------------------|----------------|-------------|
| Wells, Lanchester                 | $6.8 \pm 1$            | $205 \pm 3$    | 1.5 to 16 K |
| Jones, Jordan (1976) <sup>1</sup> |                        |                |             |
| Lounasmaa (1964) <sup>3</sup>     | 11.27                  | 210            | 0.38 to 4 K |
| and Culbert (1966) <sup>4</sup>   |                        |                | 3 to 25 K   |
| Jennings, Miller                  | 9.5                    | 166            | 15 to 300 K |
| Spedding (1960) <sup>2</sup>      |                        |                |             |

The electronic contribution, according to the free electron model, can be expressed as<sup>7</sup>:

$$C_e = \frac{2}{3} \pi^2 k^2 V n(\epsilon_F) T = \gamma T \quad (3)$$

where  $k$  is Boltzmann's constant,  $V$  is the molar volume,  $n(\epsilon_F)$  is the density of states at the Fermi surface, and  $\gamma$  is the electronic specific heat constant. The important feature in this case is that  $\gamma$  is directly proportional to the density of states at the Fermi surface.

The lutetium-hydrogen system is of interest because of (1) the large concentration of hydrogen per unit volume that can be stored in the metal at room temperature (almost twice that of hydrogen in the liquid phase) and (2) the large solid solution region extending from pure lutetium to approximately 21 atomic percent hydrogen at room temperature.<sup>8</sup> This is the second largest solid solubility range known for any pure metal, hydrogen dissolved in scandium being the largest.

The scandium-hydrogen system would be more difficult to study because use of electrotransport purified material would be necessary.<sup>9</sup> The reason is that scandium shows low temperature magnetic effects caused by traces of iron in solid solution which can only be removed by electro-transport purification. Many of the other rare earth metals, especially the heavy lanthanides, form extensive solid solutions with hydrogen<sup>8</sup>, but due to their magnetic properties the low temperature heat capacities are difficult to analyze and thus the effects of hydrogen on  $\gamma$  and  $\theta_D$  would be difficult if not impossible to determine. This makes lutetium most attractive for a study of this nature.

As well as having a large solid solution region, the lutetium-hydrogen system also has a cubic dihydride phase that exists from about 64.8 to 68.8 atomic percent hydrogen and a hexagonal trihydride phase above 73.6 atomic percent hydrogen.<sup>10</sup>

## EXPERIMENTAL PROCEDURE

## Lutetium Samples

Approximately 65 grams of high purity lutetium metal were obtained from the Rare Earth Preparation Group of the Ames Laboratory (USERDA), Iowa State University for this study. This material will be referred to as Lu-I. Lu-I was arc-melted into a rod 10 cm long and  $0.5 \text{ cm}^2$  in cross-sectional area in a water cooled copper hearth arc-melter. Before melting the lutetium the system was evacuated to  $1 \times 10^{-3}$  Torr then backfilled with high purity argon. A piece of zirconium weighing approximately 35 grams was melted to getter the remaining oxygen from the argon gas. The rod was cut into pieces 0.75 cm long with a low speed diamond saw then electropolished. Electropolishing in this study is always done in a 6 percent perchloric acid in a methanol bath maintained at  $-70^\circ\text{C}$  with a current density of about  $0.2 \text{ A} \cdot \text{cm}^{-2}$ . Samples were stored in helium until needed for hydriding or for calorimetry. The system used for hydriding will be discussed later in this section.

In order to obtain the best  $\gamma$  and  $\theta_D$  values for lutetium a rod 16.5 cm long and 0.25 cm in diameter was prepared for purification by electrotransport as described below. Eleven grams of Lu-I were first arc-melted into a rod as described above. This rod was placed in a tantalum tube and swaged to reduce the cross sectional area by 30 percent. The tantalum was removed, the surface was filed with a new file, and the sample was then electropolished. After this it was placed in a tungsten lined tantalum crucible and heated to  $800^\circ\text{C}$  for one hour in

a vacuum of  $2 \times 10^{-8}$  Torr for stress relief. It was cooled, removed from the vacuum furnace, placed in a new tantalum tube, and swaged again. This process was done five times until the desired dimensions were obtained. After the rod was formed, both ends were threaded with a new 3-48 N.F. die for a length of 0.5 cm. The threads were necessary to attach the sample to the holder used for electrotransport purification. The sample was electropolished just before loading into this system. The system was evacuated and outgassed at  $380^{\circ}\text{C}$  for one week before the electrotransport process was begun. The lutetium was electrotransported for 336 hours at  $1065^{\circ}\text{C}$  in a vacuum of  $1.0 \times 10^{-10}$  Torr. This sample will be called Lu-II. After this purification process the rod was cut into four pieces of equal length with a low speed diamond saw. The pieces were labeled A, B, C, and D as shown in Figure 1a. Only Section A was used for calorimetry as it is the most pure. It was cut as shown in Figure 1b in order to fit the sample holder of the calorimeter. Pieces b, c, and d were used. All pieces were electropolished immediately after cutting to passivate the surface.<sup>11</sup> The resistance ratio,  $R_{298\text{ K}}/R_{4.2\text{ K}}$ , of Lu-II was measured for Sections A, C, and D. The results are given in Table 2. Section B was not measured because it was desired to have a high purity single crystal for de Haas-von Alphen measurements and the sample holder in the resistivity apparatus might cause twinning in the material. Two measurements were made on each section, indicated by the section together with a (+) or (-). The (-)

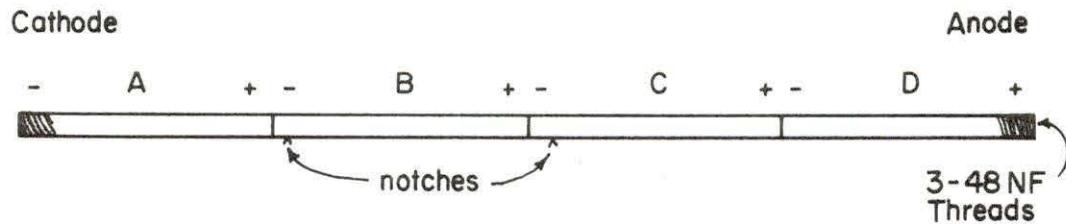


Figure 1a. The electrotransport purified lutetium rod (Lu-11) cut into sections. Sections B and C were marked with a notch to identify the end nearer the cathode

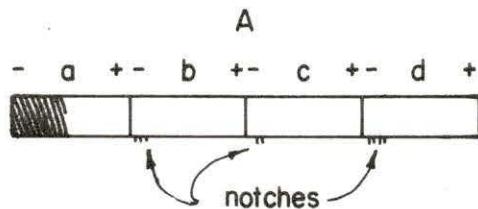


Figure 1b. The section of the electrotransport purified lutetium rod (Lu-11) cut for calorimetry. The cathode ends of b, c, and d were marked with notches for identification as shown

Table 2. Resistance ratio,  $R_{298\text{ K}}/R_{4.2\text{ K}}$  for Lu-II

| Section        | $R_{298\text{ K}}/R_{4.2\text{ K}}$ |
|----------------|-------------------------------------|
| A <sup>-</sup> | 152                                 |
| A <sup>+</sup> | 103                                 |
| B <sup>-</sup> | not measured                        |
| B <sup>+</sup> | not measured                        |
| C <sup>-</sup> | 89                                  |
| C <sup>+</sup> | 88                                  |
| D <sup>-</sup> | 82                                  |
| D <sup>+</sup> | 55                                  |

signifies the end of the section nearer the cathode during the electro-transport process. The (+) signifies the end of each section that was nearer the anode.

A second piece of electrotransport purified lutetium was also obtained. This had been purified in 1967. This sample will be identified as Lu-III. The conditions for electrotransport of this sample were outgassing at  $380^{\circ}\text{C}$  for one week then electrotransport at  $1100^{\circ}\text{C}$  for 96 hours in a vacuum of  $5 \times 10^{-10}$  Torr. The highest resistance ratio (93) was found at the cathode end as in the case of Lu-II.

The chemical analyses for Lu-I, Lu-II, and Lu-III are given in Table 3. The oxygen, hydrogen, and nitrogen are from vacuum fusion analysis, the carbon and fluorine from chemical methods, and the other elements from mass spectrometry.

Table 3. Chemical Analysis of Lu-I, Lu-II, and Lu-III. Hydrogen, nitrogen, and oxygen are from vacuum fusion analysis; all other elements are from mass spectrometry. All are atomic ppm

| Element | Lu-I    | Lu-II         | Lu-III <sup>a</sup> |
|---------|---------|---------------|---------------------|
| H       | 1050    | < 175         | 350                 |
| Li      | < 0.007 | < 0.001       | -                   |
| Be      | < 0.002 | < 0.002       | -                   |
| B       | < 0.05  | 0.2           | < 0.02              |
| C       | 90      | 100           | 100                 |
| N       | 13      | none detected | 113                 |
| O       | 610     | 82            | 635                 |
| F       | < 0.005 | < 0.4         | 0.02                |
| Ne      | < 0.02  | < 0.1         | -                   |
| Na      | 0.9     | 0.1           | 0.9                 |
| Mg      | < 0.3   | < 0.1         | 0.7                 |
| Al      | 1       | 0.50          | 13                  |
| Si      | < 3     | 0.50          | 40                  |
| P       | 0.1     | 0.1           | 0.2                 |
| S       | 0.4     | 2             | 0.5                 |
| Cl      | 0.6     | 3             | -                   |
| Ar      | < 0.2   | < 2           | -                   |
| K       | 1       | < 0.02        | 0.9                 |
| Ca      | 0.40    | < 0.4         | 3                   |
| Sc      | 1       | 0.10          | 2                   |
| Ti      | 1       | 2.6           | 3                   |
| V       | 0.04    | < 0.01        | 1.5                 |
| Cr      | 0.3     | 0.2           | 2                   |
| Mn      | < 0.09  | < 0.02        | 1.5                 |

<sup>a</sup>Mass spectrometric values reported are for the lutetium sample before electrotransport purification; the H, N, and O values were obtained after electrotransport purification in 1977.

Table 3 (continued)

| Element | Lu-I    | Lu-II   | Lu-III |
|---------|---------|---------|--------|
| Fe      | 10      | 1       | 100    |
| Co      | < 0.04  | < 0.04  | 1.3    |
| Ni      | 1       | < 0.2   | 20     |
| Cu      | 5.0     | < 0.03  | 20     |
| Zn      | 0.04    | < 0.02  | 0.8    |
| Ga      | < 0.04  | < 0.02  | -      |
| Ge      | < 0.06  | < 0.1   | -      |
| As      | < 0.02  | < 0.02  | -      |
| Se      | < 0.02  | < 0.01  | < 0.1  |
| Br      | 0.03    | 0.02    | < 0.1  |
| Kr      | < 0.3   | < 0.06  | -      |
| Rb      | < 0.1   | < 0.1   | -      |
| Sr      | < 0.6   | < 0.05  | -      |
| Y       | 0.40    | 0.80    | 12     |
| Zr      | < 0.3   | < 0.3   | 8      |
| Nb      | < 1     | < 0.8   | 0.5    |
| Mo      | < 1     | < 1     | < 0.3  |
| Ru      | < 0.4   | < 0.2   | -      |
| Rh      | < 0.07  | < 0.07  | -      |
| Pd      | < 0.1   | < 0.2   | -      |
| Ag      | < 0.006 | < 0.09  | < 0.07 |
| Cd      | < 0.01  | < 0.01  | -      |
| In      | < 0.03  | < 0.03  | -      |
| Sn      | < 0.1   | < 0.04  | < 0.4  |
| Sb      | < 0.04  | < 0.04  | -      |
| Te      | < 0.01  | < 0.01  | -      |
| I       | < 0.03  | < 0.04  | -      |
| Xe      | < 0.4   | < 0.4   | -      |
| Cs      | < 0.004 | < 0.003 | -      |

Table 3 (continued)

| Element | Lu-I    | Lu-II  | Lu-III |
|---------|---------|--------|--------|
| Ba      | < 0.04  | < 0.04 | < 0.1  |
| Hf      | < 1     | < 1    | < 0.2  |
| Ta      | 3.3     | 4.0    | 75     |
| W       | 20      | 33     | 6.5    |
| Re      | < 0.5   | < 2    | < 0.2  |
| Os      | < 1     | < 3    | < 0.5  |
| Ir      | < 0.3   | < 0.3  | < 0.5  |
| Pt      | < 0.2   | < 0.3  | 18     |
| Au      | < 0.07  | < 0.07 | < 0.2  |
| Hg      | < 0.009 | 1.2    | < 0.6  |
| Tl      | < 0.05  | < 0.05 | < 0.2  |
| Pb      | 0.50    | < 0.2  | 3      |
| Bi      | < 0.04  | < 0.04 | < 0.2  |
| Ra      | < 0.2   | < 0.2  | -      |
| Th      | < 5     | 5.2    | 0.4    |
| U       | < 0.2   | < 0.2  | -      |
| La      | 5.8     | 10     | 12     |
| Ce      | 0.9     | 1.1    | 6      |
| Pr      | 0.3     | 1.5    | 2      |
| Nd      | < 0.9   | < 0.7  | 2.5    |
| Sm      | < 0.7   | < 0.4  | < 0.6  |
| Eu      | < 0.3   | < 0.2  | < 0.13 |
| Gd      | < 1     | < 0.7  | 9      |
| Tb      | < 0.8   | < 2    | 3.6    |
| Dy      | < 2     | 1      | 1      |
| Ho      | < 1     | < 1    | 1      |
| Er      | < 2     | < 1    | 9.5    |
| Tb      | < 1     | < 0.3  | < 0.06 |
| Yb      | < 3     | < 1    | < 0.4  |

The total maximum impurity content before electrotransport purification (Lu-I) was 1850 atomic parts per million (ppm). After electrotransport this value dropped to 447 atomic ppm (Lu-II) mainly due to a decrease in hydrogen and oxygen.

#### Hydriding Apparatus and Procedure

The system used to produce the lutetium hydride samples for calorimetry is a glass system with a liquid nitrogen cold-trapped diffusion pump capable of achieving vacuum of  $1 \times 10^{-7}$  Torr, a mercury manometer to measure the amount of hydrogen introduced to the sample chamber, and a quartz tube to withstand the temperatures required. The tank hydrogen was purified by reacting it with uranium turnings to form  $\text{UH}_3$  which was then thermally decomposed to give hydrogen gas.

The lutetium samples were cut from the rod of Lu-I with a low speed diamond saw and weighed about four grams each. They were electro-polished, washed with acetone, placed in a tantalum boat, and loaded into the quartz sample tube. The sample tube had a ground glass taper which was sealed to the system with Apiezon T grease. The system was then evacuated to about  $2 \times 10^{-7}$  Torr. When this vacuum was achieved, the sample was heated to  $650^{\circ}\text{C}$  in a split-tube resistance furnace. The desired amount of hydrogen was then added and was usually absorbed within one or two hours. The sample was held for 70 hours between  $600^{\circ}\text{C}$  and  $650^{\circ}\text{C}$  to ensure homogeneity. It was then furnace cooled, unloaded, and stored in helium gas until needed. Figure 2 is a diagram of the hydriding system.

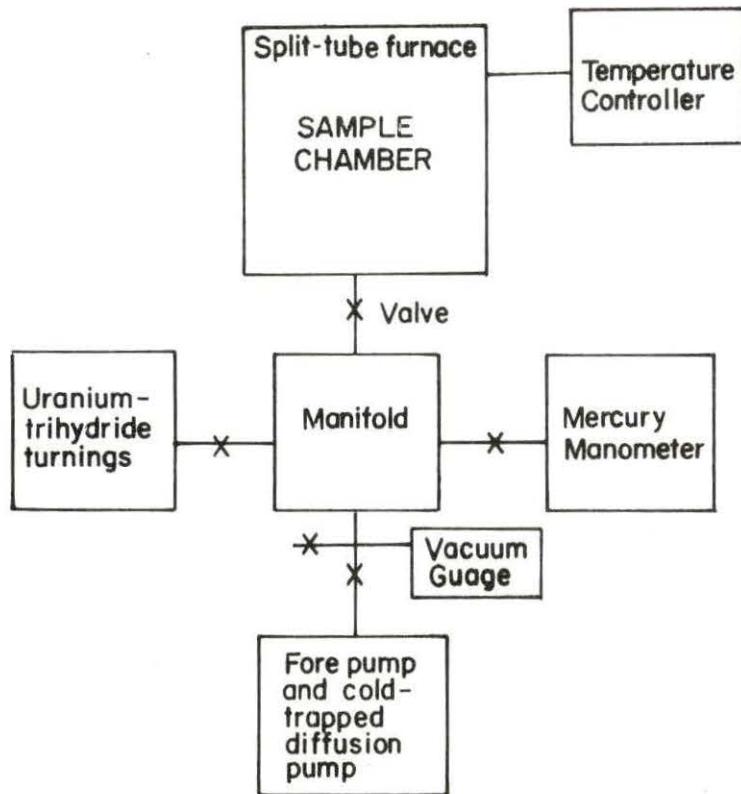


Figure 2. Simplified diagram of hydriding system

### Calorimetry

Samples were prepared for calorimetry by electropolishing, rinsing with acetone, then drying in air. The samples were weighed with a Schaar double pan balance then  $6.0 \pm 0.1$  mg of Apiezon N grease was added to form a bond between the sample and the sample holder of the calorimeter. The calorimeter is described briefly in Appendix A. After the sample was loaded, the vacuum can was soldered into place with Wood's metal and the system was checked for vacuum leaks. It was then placed in the cryostat and the sample chamber evacuated to less than  $1 \times 10^{-6}$  Torr. The outer nitrogen dewar was then filled and the system allowed to cool by radiation for at least 12 hours before liquid helium was transferred. Data points were taken from 4.2 to 20 K then the sample was cooled to 1 K by pumping on the liquid helium in the pumping pot. Data points were then taken from 1 K to 4.2 K. The heat capacity was determined by inputting heat pulses of 16 to 34 seconds duration at the desired heater current. The temperature was monitored on a strip chart recorder and was extrapolated to the center of the heat pulse. The duration of the heat pulse was measured with a Monsanto digital electronic timer. The entire electronic system for the calorimeter is described in Appendix A. All the measured values were coded, then analyzed by an IBM 360 computer. The heat capacity of the sample holder,  $C_{ad}$ , was determined separately, and was subtracted from the measured heat capacity by the equation,

$$C = \frac{\Delta Q}{\Delta T} - C_{ad} \quad (4)$$

X

where  $\Delta Q$  is the heat input,  $\Delta T$  is the temperature change, and  $X$  is the number of gram-atoms of the alloy sample. The heat capacity of a piece of the 1965 Calorimetry Conference Standard Copper Sample was measured in this calorimeter and found to agree within two percent of the results of Osborne, Flotow, and Schreiner.<sup>12</sup> Results of the heat capacity measurements are tabulated in Appendix B. The data are fit to the equation:

$$C/T = \gamma + \beta T^2 \quad (5)$$

between 1 to 5 K by a least squares treatment.

#### Vacuum Fusion and X-ray Analysis

The actual concentration of hydrogen in the samples containing less than 20 atomic percent hydrogen was determined by vacuum fusion analysis. Small samples are dropped into a molten platinum-tin bath containing carbon and the volume of the liberated gases H<sub>2</sub>, N<sub>2</sub>, and oxygen as CO is measured. The gases are then passed over hot CuO converting CO to CO<sub>2</sub> and H<sub>2</sub> to H<sub>2</sub>O. The CO<sub>2</sub> is then condensed in a liquid nitrogen cold trap while the water is absorbed by Mg(ClO<sub>4</sub>)<sub>2</sub> leaving only N<sub>2</sub> in the system. The N<sub>2</sub> is measured then the CO<sub>2</sub> is evaporated and the N<sub>2</sub>

and  $\text{CO}_2$  together are measured thus determining the amount of all three gases. All samples were measured in triplicate to assure accuracy and homogeneity.

Previous work by Beaudry and Spedding<sup>8</sup> has shown that the atomic volume of lutetium increases linearly with increasing hydrogen in solid solution. Lattice parameters for each of the lutetium hydride samples were measured after the heat capacity had been determined and were compared to Beaudry's results. X-ray "needles" were filed from material taken from the center of the sample. After filing to about 0.3 mm diameter

Table 4. Results of x-ray analysis

| Sample | Atomic Percent<br>Hydrogen <sup>a</sup> | $a_0$     | Lattice Parameters <sup>b</sup><br>$c_0$ | unit cell volume |
|--------|---|-----------|--|------------------|
| Lu-II  | < 0.018                                 | -         | -  | -                |
| Lu-III | 0.035                                   | -         | -  | -                |
| Lu-IB  | 0.035                                   | -         | -  | -                |
| Lu-I   | 0.11                                    | 3.5051(4) | 5.5491(5)                                | 59.04(2)         |
| 2-20   | 0.22                                    | 3.5059(1) | 5.5491(1)                                | 59.07(0)         |
| 2-21   | 0.57                                    | 3.5060(2) | 5.5507(2)                                | 59.09(1)         |
| 2-19   | 1.4                                     | 3.5061(2) | 5.5532(2)                                | 59.12(1)         |
| 2-10   | 1.5                                     | 3.5071(2) | 5.5544(2)                                | 59.17(1)         |
| 1-84   | 3.1                                     | 3.5081(2) | 5.5589(4)                                | 59.25(1)         |
| 2-5    | 6.5                                     | 3.5114(2) | 5.5685(4)                                | 59.46(1)         |
| 1-98   | 12.4                                    | 3.5153(1) | 5.5805(3)                                | 59.72(1)         |
| 2-4    | 18.2                                    | 3.5209(2) | 5.5940(2)                                | 60.06(1)         |

<sup>a</sup>From vacuum fusion analysis.

<sup>b</sup>Figure in parentheses represents uncertainty in the last digit (1).

and 1 mm length, the needles were electropolished to 0.2 mm diameter to remove the cold worked surface. The needles were exposed to nickel filtered copper radiation for six to eight hours in a 114.6 mm Debye-Scherrer camera. The films were developed and read and this information was analyzed by an IBM 360 computer using a Nelson-Reilley extrapolation procedure to obtain reliable  $a_0$  and  $c_0$  lattice parameters. The results are given in Table 4 and are plotted along with Beaudry's data in Figure 3. Good agreement with Beaudry's results was found for all samples.

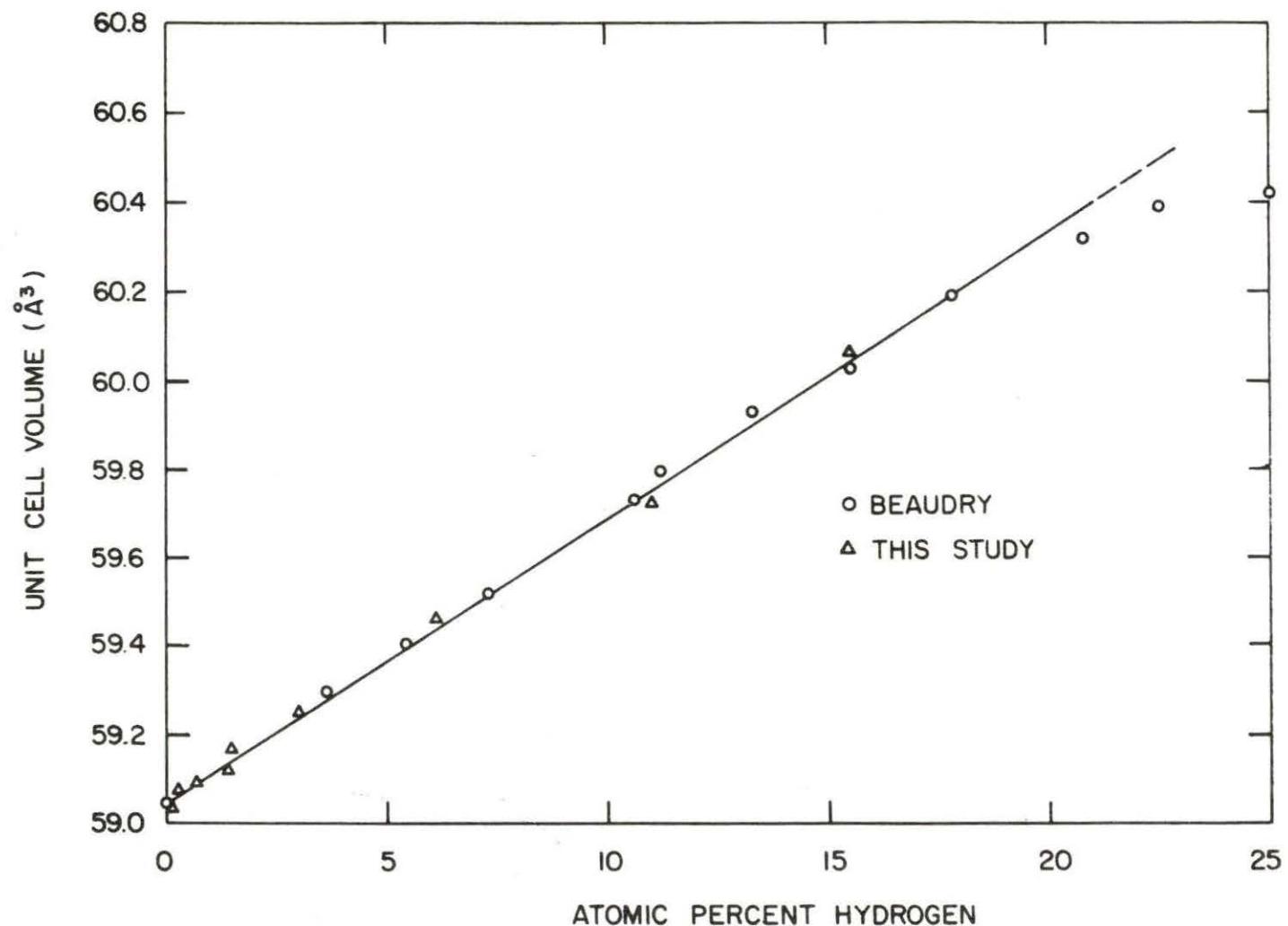


Figure 3. Atomic volume versus hydrogen content in lutetium

## RESULTS AND DISCUSSION

The heat capacity of the sample holder of the calorimeter was determined in a separate experiment and was checked using the 1965 Calorimetry Conference Standard Copper Sample. Figure 4 shows the measured heat capacity together with a plot of the copper reference equation of Osborne, Flotow, and Schreiner.<sup>12</sup> The measured data agree to within about two percent of the copper reference equation. The scatter in the data is due to the small size of the sample (about five grams).

The measured heat capacity of electrotransport purified lutetium, Lu-II, is shown in Figure 5 together with the line determined by the least squares fit of the data. This line is also plotted as a reference to pure lutetium for the lutetium hydrogen alloys in Figures 6 and 7. The  $\gamma$  and  $\theta_D$  values determined from Lu-II and Lu-III agree well. The values of  $\theta_D$  are also in good agreement with  $\theta_D$  determined from elastic constant measurements on lutetium single crystals by Tonries *et al.*<sup>13</sup> He reports a value of 184.5 K as compared to 183.2 K for Lu-II and 182.3 for Lu-III. The difference is probably less than the sum of errors in both experiments.

The heat capacity of the lutetium starting material for this study was measured (sample Lu-IA) and the data showed, in a C/T versus  $T^2$  plot, a slight rise below about 2.5 K from the straight line established at higher temperature. See Figure 6. Since there is no evidence for this behavior in the electrotransport purified lutetium samples it was suspected that this anomaly might be due to hydrogen. Vacuum fusion analysis showed that there were about 1050 atomic parts per million (ppm)

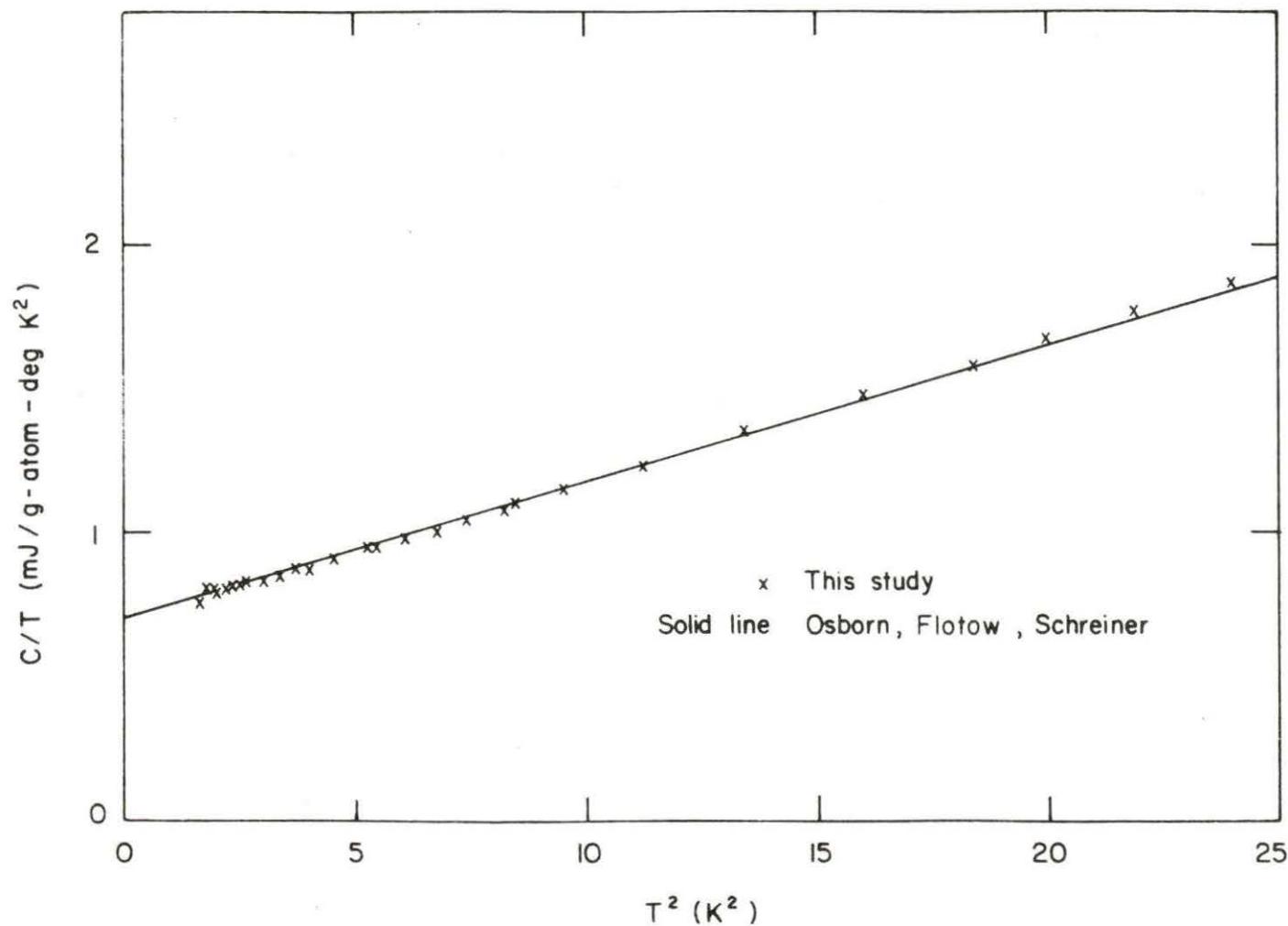


Figure 4. Heat capacity of the copper standard sample

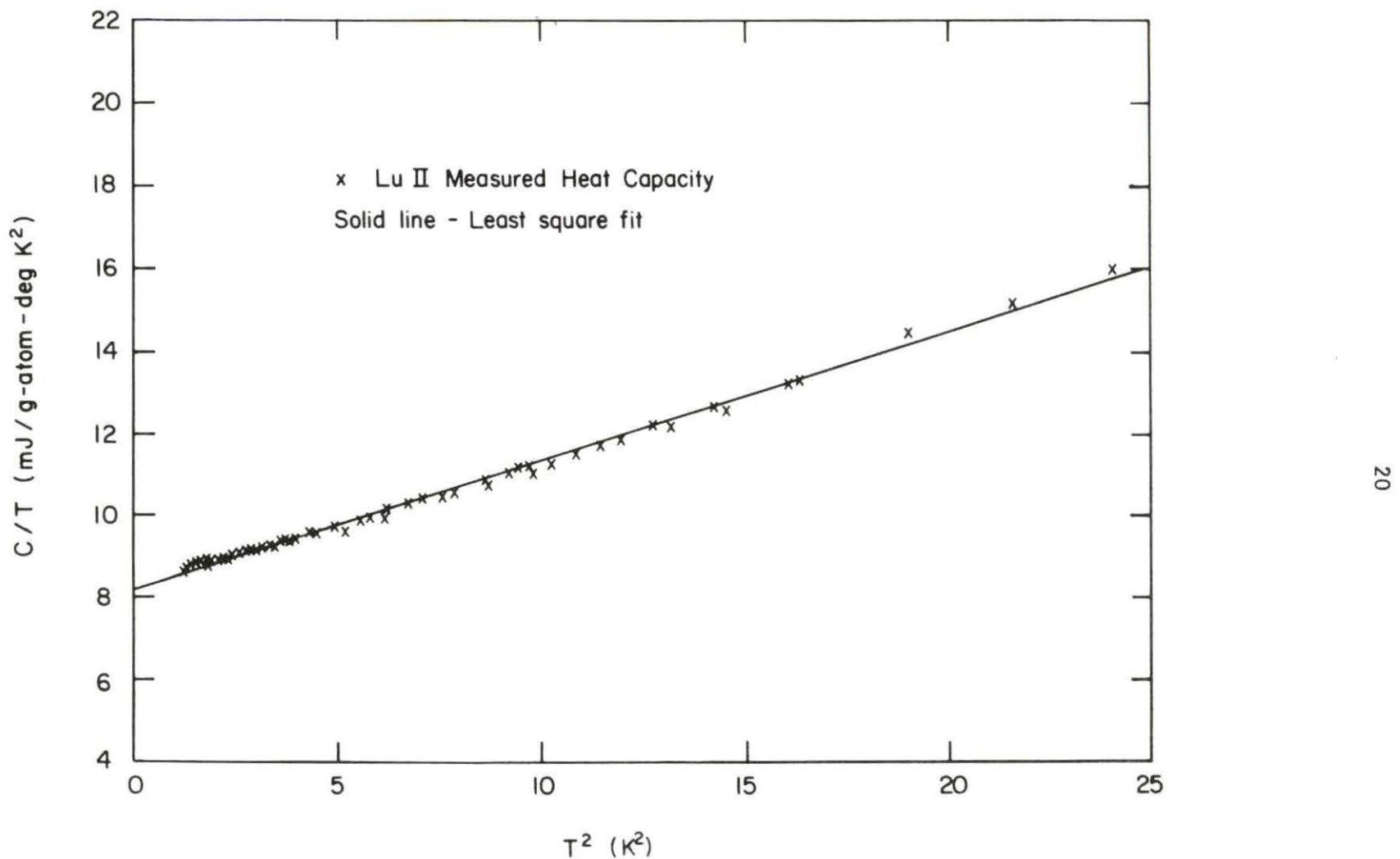


Figure 5. Heat capacity of electrotransport purified lutetium

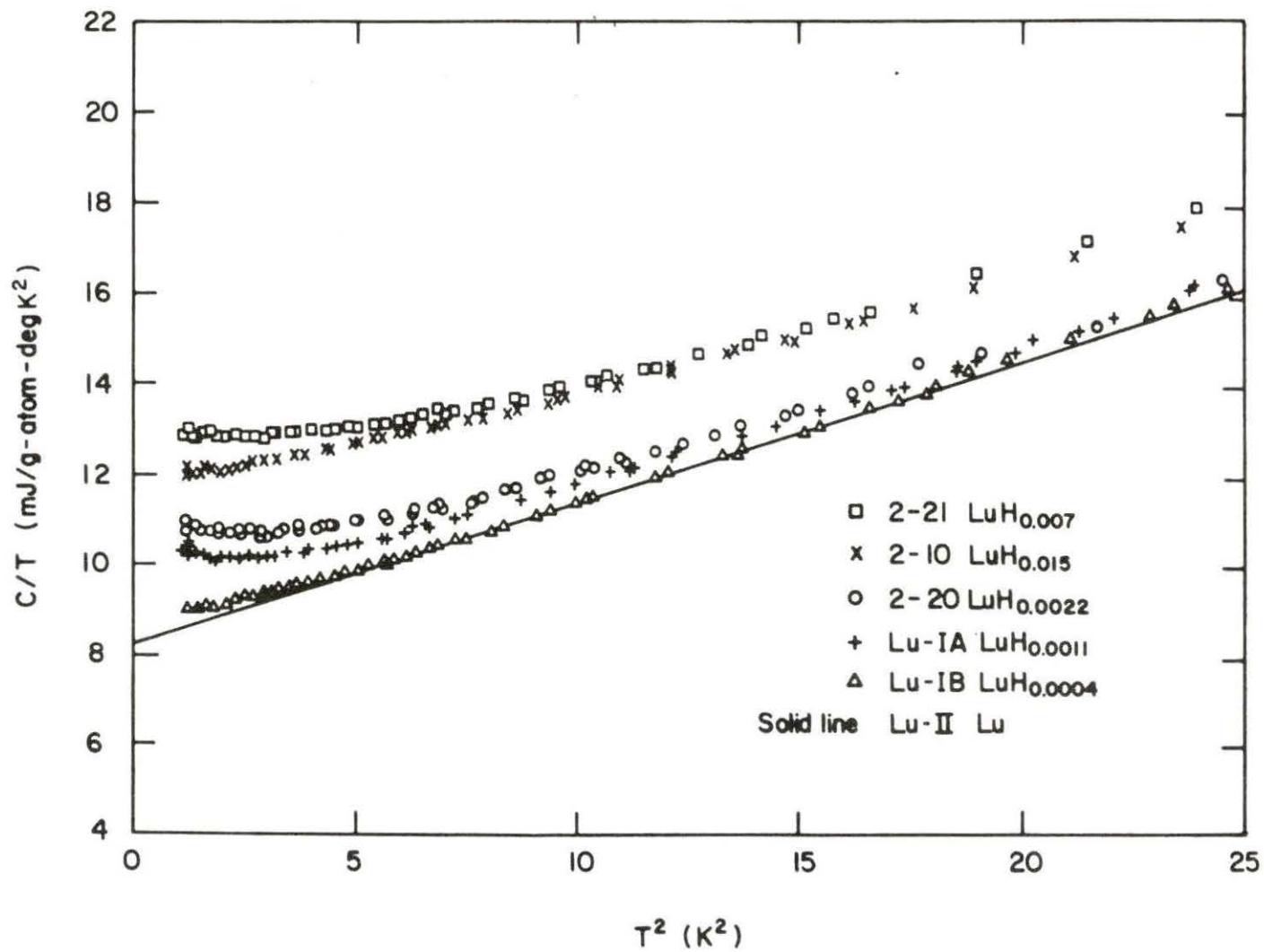


Figure 6. Heat capacity of lutetium-hydrogen alloys

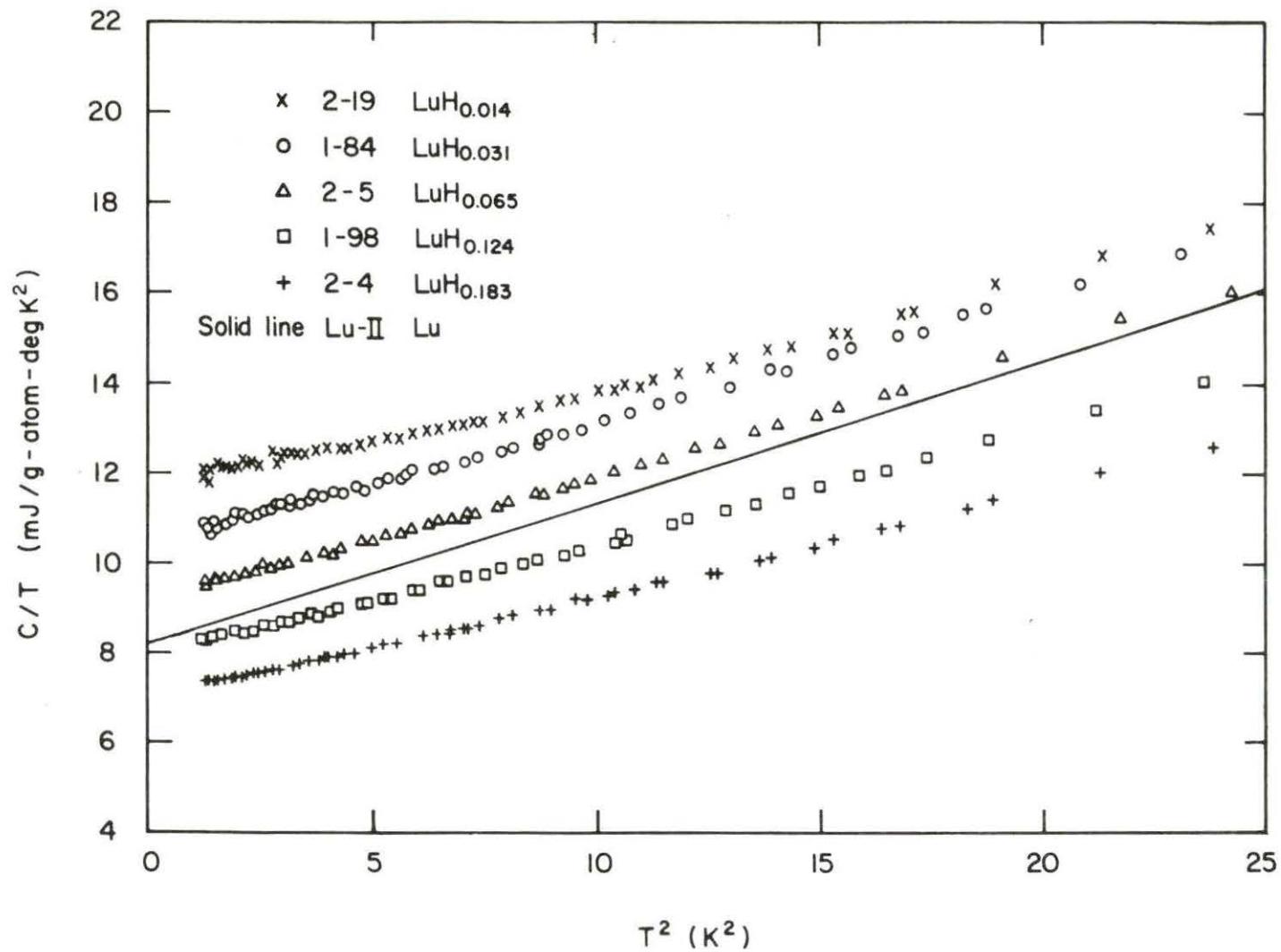


Figure 7. Heat capacity of lutetium-hydrogen alloys

of hydrogen in this material. A piece of Lu-I was then annealed at 1000°C for six hours in a vacuum of  $1 \times 10^{-8}$  Torr to remove the hydrogen. The analysis for this sample, Lu-IB, showed about 350 atomic ppm of hydrogen and the heat capacity data were in much better agreement with Lu-II and Lu-III. The  $\gamma$  and  $\theta_D$  values with their statistical error together with the analysis for hydrogen, nitrogen, and oxygen are listed in Table 5 for all samples measured. The heat capacity data for Lu-IA and Lu-IB are shown in Figure 6. The heat capacity of the starting material was remeasured (sample Lu-IC) and the results agreed with sample Lu-IA indicating that as little as 0.1 atomic percent hydrogen has an effect on the heat capacity of lutetium. It was found that other lutetium samples with concentrations between 0.1 and about 1.5 atomic percent hydrogen also showed a rise in C/T with decreasing temperature below about 2.5 K. The heat capacity data are shown in Figure 6 for these alloys. The increase in C/T with decreasing temperature is similar to that reported for the superconducting palladium-hydrogen system<sup>14</sup> except it appears that the peak in C/T versus  $T^2$  for lutetium-hydrogen alloys would occur below 1 K which is below the limit of the calorimeter used in this study. The values for  $\theta_D$  and  $\gamma$  for the low concentration lutetium hydrogen alloys (< 1.5 atomic percent hydrogen) were determined from data between the start of the increase in C/T versus  $T^2$  and about 4.5 K. In some cases this meant only the points between 4 and 4.5 K which caused a large scatter in  $\theta_D$  for these alloys as well as increased statistical error for  $\gamma$ . The  $\theta_D$  versus hydrogen content values are

Table 5.  $\theta_D$ ,  $\gamma$ , and composition of lutetium hydrogen alloys

| Sample | hydrogen <sup>a</sup> | nitrogen <sup>a</sup> | oxygen <sup>a</sup> | $\gamma$<br>(mJ/g-atom K <sup>2</sup> ) | $\theta_D$<br>(K) |
|--------|-----------------------|-----------------------|---------------------|---|-------------------|
| Lu-II  | < 0.018               | < 0.0013              | 0.008               | 8.194±0.016                             | 183.2±0.3         |
| Lu-III | 0.035                 | 0.0130                | 0.063               | 8.209±0.020                             | 182.3±0.3         |
| Lu-IB  | 0.035                 | 0.0013                | 0.060               | 8.351±0.019                             | 184.0±0.3         |
| Lu-IA  | 0.105                 | 0.0013                | 0.061               | 8.680±0.035                             | 185.1±0.4         |
| Lu-IC  | 0.105                 | 0.0013                | 0.061               | 8.650±0.042                             | 184.7±0.6         |
| 2-20   | 0.22                  | 0.0013                | 0.064               | 9.234±0.044                             | 190.5±0.7         |
| 2-21   | 0.57                  | 0.0054                | 0.103               | 9.769±0.111                             | 187.2±1.3         |
| 2-19   | 1.4                   | none                  | 0.078               | 11.126±0.035                            | 194.6±0.6         |
| 2-10   | 1.5                   | 0.0008                | 0.074               | 10.707±0.088                            | 189.3±1.0         |
| 1-84   | 3.0                   | 0.0031                | 0.15                | 10.354±0.008                            | 191.0±0.2         |
| 2-5    | 6.1                   | 0.0021                | 0.14                | 9.102±0.005                             | 190.8±0.1         |
| 1-98   | 11.0                  | 0.0100                | 0.19                | 7.861±0.007                             | 196.8±0.2         |
| 2-4    | 15.5                  | 0.0150                | 0.20                | 6.964±0.005                             | 204.9±0.2         |
| 2-8    | 67.0                  | -                     | -                   | 0.724±0.002                             | 361.4±0.3         |

<sup>a</sup>Atomic percent.

plotted in Figure 8 and with an expanded concentration scale in Figure 9. The  $\gamma$  versus hydrogen content values are plotted in Figure 10 with an expanded concentration scale in Figure 11. The  $\gamma$  values show an increase of about 40 percent with the hydrogen content increasing from zero to about 1.2 atomic percent and then a gradual decrease with further increase in hydrogen content. These results could give an indication of the band structure of lutetium however it is not possible to conclude this from heat capacity measurements alone.

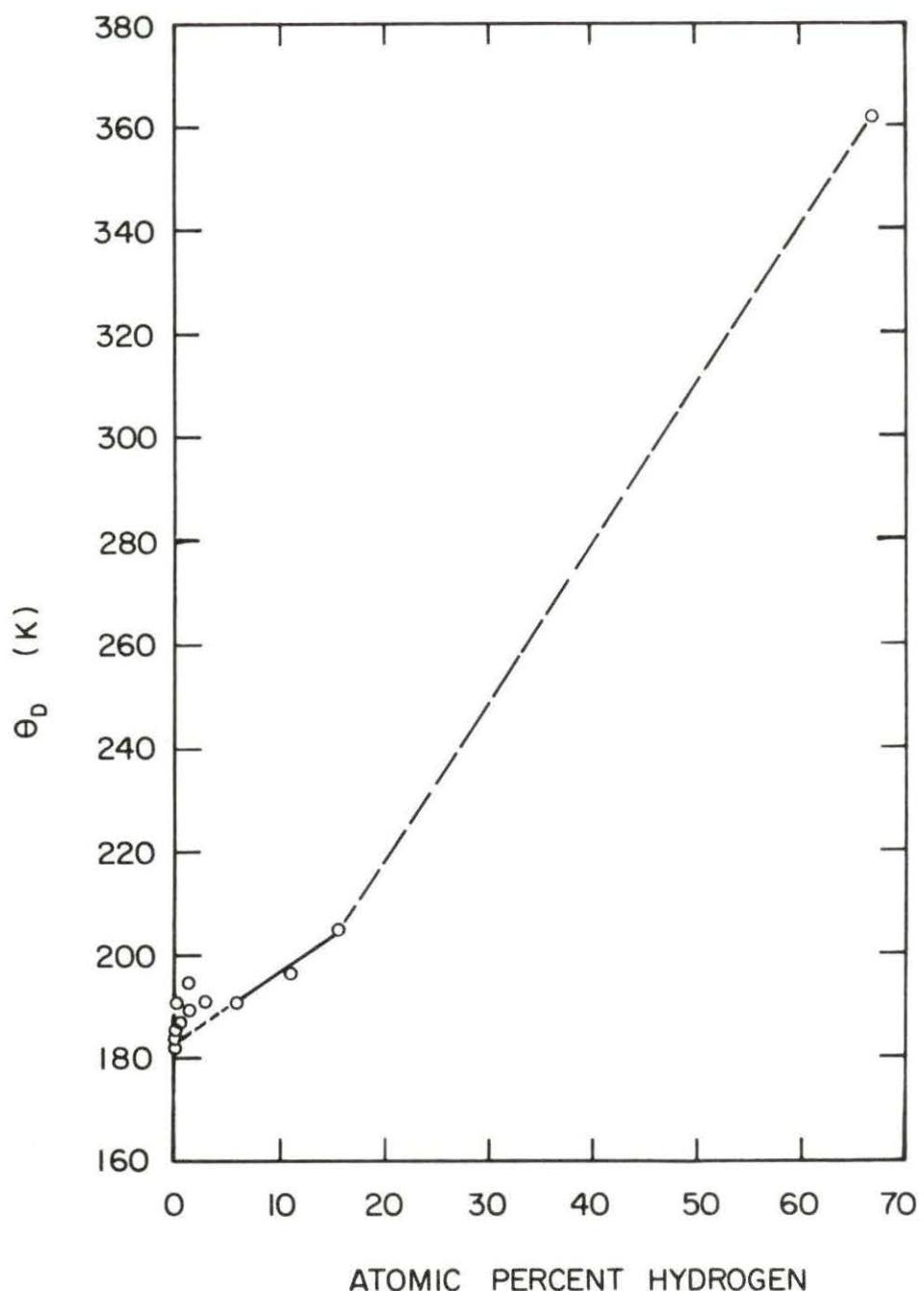


Figure 8.  $\theta_D$  versus hydrogen content in lutetium

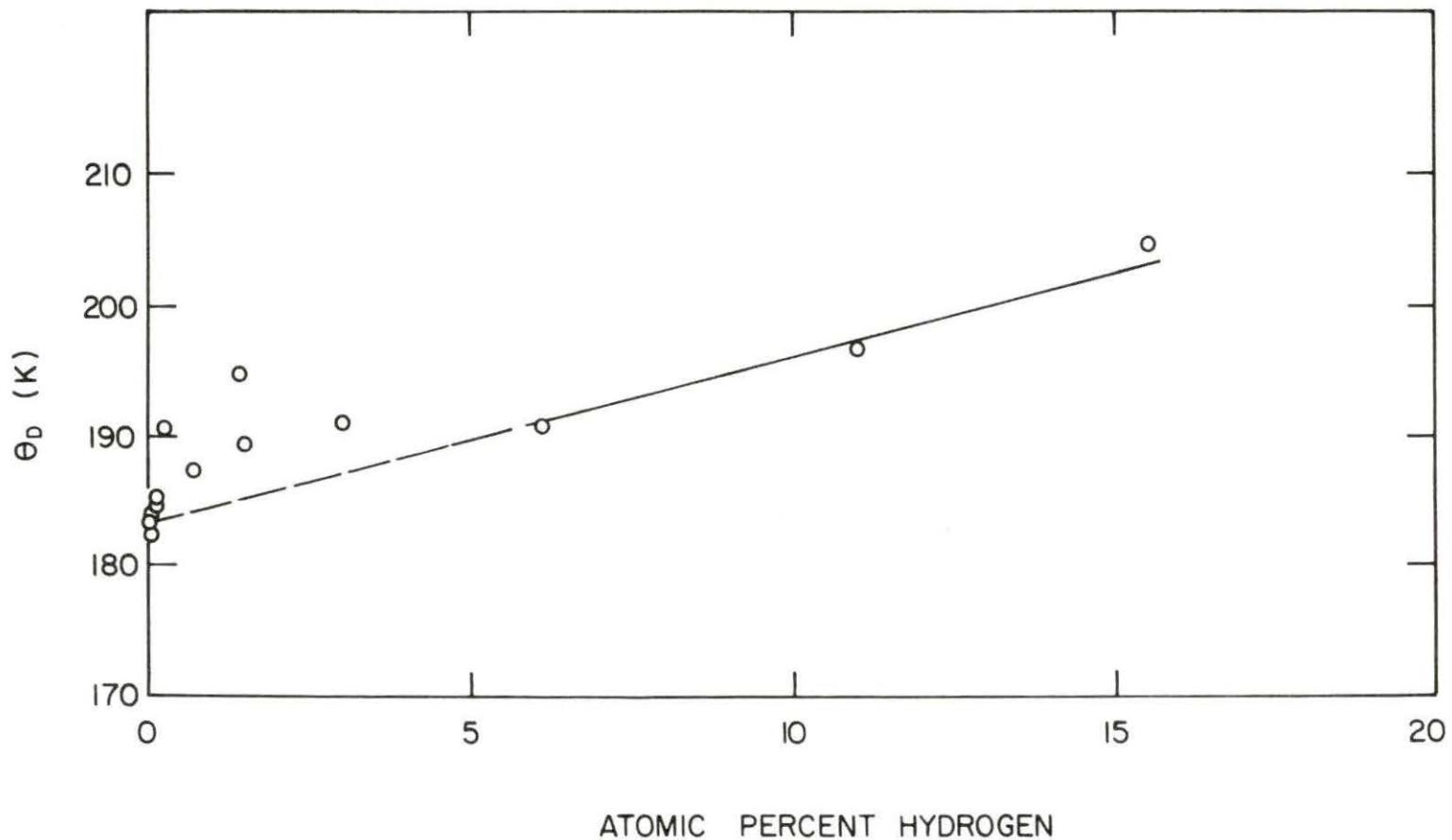


Figure 9.  $\theta_D$  versus hydrogen content in lutetium

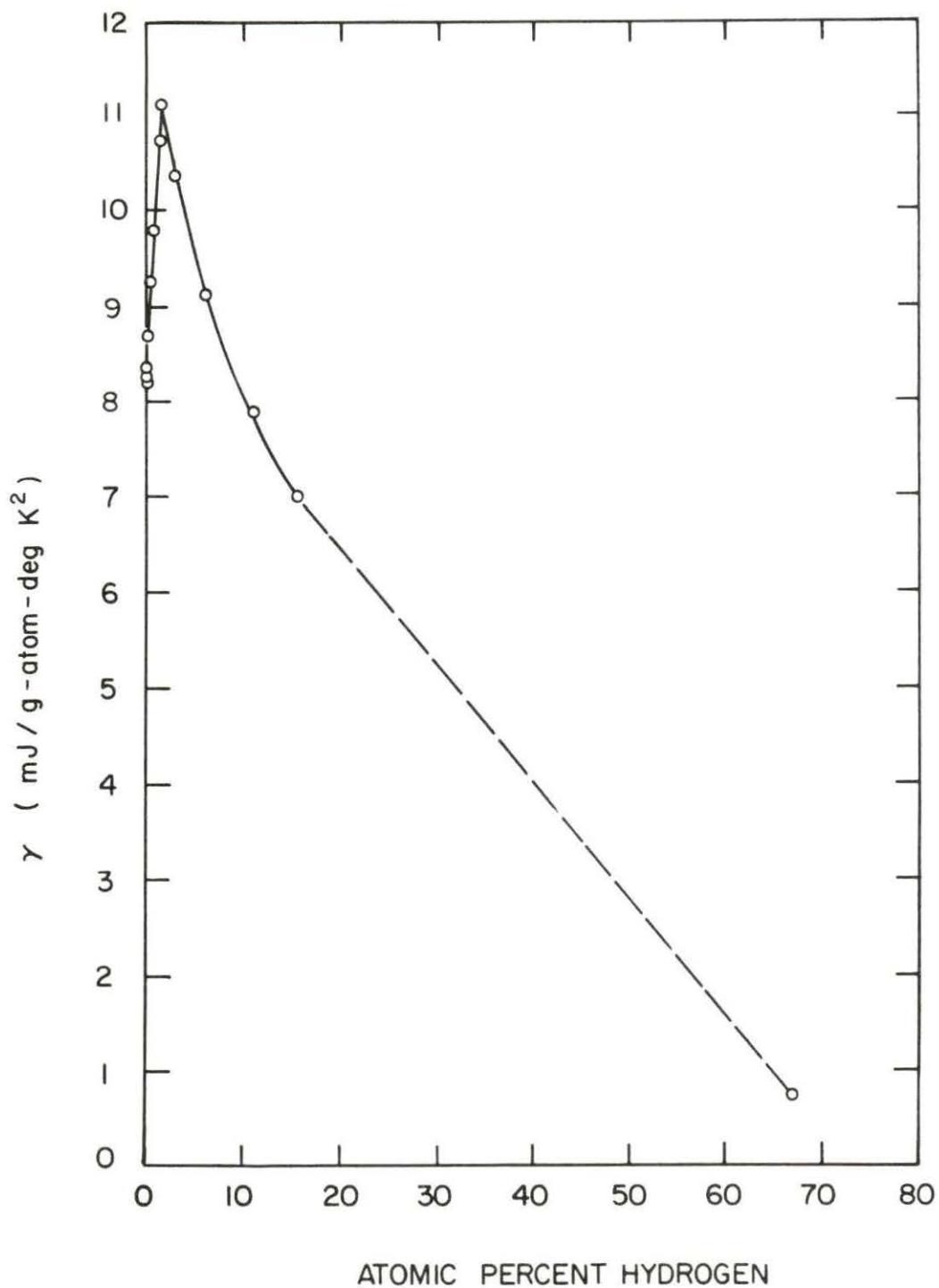


Figure 10.  $\gamma$  versus hydrogen content in lutetium

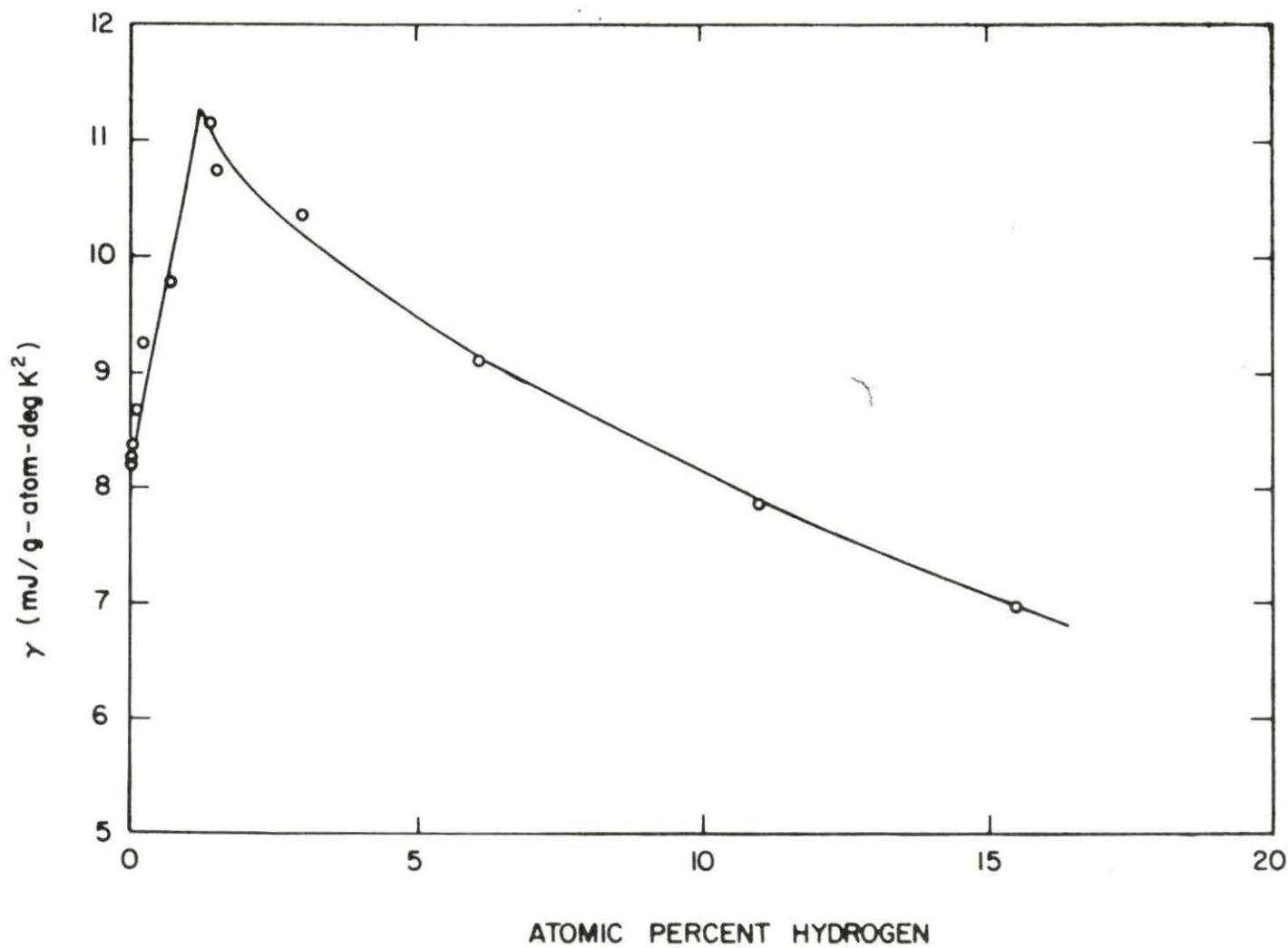


Figure 11.  $\gamma$  versus hydrogen content in lutetium

Sellers, Anderson, and Birnbaum have studied the effects of hydrogen and deuterium on the heat capacity of niobium between 0.06 and 2 K and find an isotope dependent anomaly.<sup>15</sup> They suggest that the anomaly is caused by lattice effects rather than electronic effects. They further suggest that the lattice effects are due to quantum mechanical tunneling of the hydrogen or deuterium interstitials. It may be possible that tunneling of hydrogen occurs in the lutetium-hydrogen system as well. It is difficult to compare the lutetium-hydrogen system to the niobium-hydrogen and deuterium systems for a number of reasons: (1) niobium is a superconductor in the temperature range studied and the heat capacity was measured in the superconducting state; (2) the niobium-hydrogen alloys were two-phase while evidence shows lutetium-hydrogen alloys up to 15.5 atomic percent hydrogen are single phase as is discussed later; (3) the calorimeter in this study could only attain a minimum temperature of 1.1 K so that any peak in heat capacity below this could not be characterized; and (4) the heat capacity of lutetium plus deuterium was not measured.

If tunneling does give rise to a linear term in the heat capacity of lutetium, then it is consistent with the peak in  $\gamma$  versus hydrogen content. As hydrogen is added to pure lutetium tunneling would occur increasing the heat capacity. As the hydrogen content increases neighboring sites for hydrogen become occupied and the probability for tunneling decreases because of the unavailability of unoccupied sites. This would be consistent with the decrease in  $\gamma$  with hydrogen increasing above about 1.2 atomic percent in lutetium. To confirm this, measurements

of the effects of deuterium on lutetium need to be measured (preferably to below 1 K) to determine if the anomaly observed is isotope dependent. Magnetic susceptibility measurements could also shed light on the lutetium-hydrogen system by determining if the anomaly is due to magnetic effects, such as itinerant ferromagnetism, or superconductivity.

Daou et al.<sup>16</sup>, in measuring resistivity of lutetium-hydrogen alloys found no evidence for precipitation of second phase from a solid solution of 12.8 atomic percent hydrogen on cooling to 4.2 K and gives several arguments against it. The fact that  $\theta_D$  in this study does not extrapolate to values determined for lutetium dihydride (as shown in Figure 12) is strong evidence that lutetium with 15.5 atomic percent hydrogen is still a solid solution even at 1 K. A linear increase in  $\theta_D$  with increasing hydrogen to the lutetium dihydride value would be expected from a two phase system. Observation of the 15.5 atomic percent hydrogen sample with an optical microscope while cooling to 77 K did not show any evidence of precipitation of second phase.

The heat capacity of the lutetium dihydride sample referred to above was measured and the results are shown in Figure 12. The  $\gamma$  and  $\theta_D$  values for lanthanum dihydride<sup>17</sup> compare with those determined for lutetium dihydride. Bieganski et al. report their value for  $\theta_D$  on a per mole basis which is incorrect;  $\theta_D$  should be calculated on a per gram-atom basis. Their corrected values are 349 K for  $\theta_D$  and  $2.6 \text{ mJ/g-atom-K}^2$  for  $\gamma$  for lanthanum dihydride. These values compare with 361 K for  $\theta_D$  and  $0.72 \text{ mJ/g-atom-K}^2$  for  $\gamma$  for lutetium dihydride as is listed in Table 5.

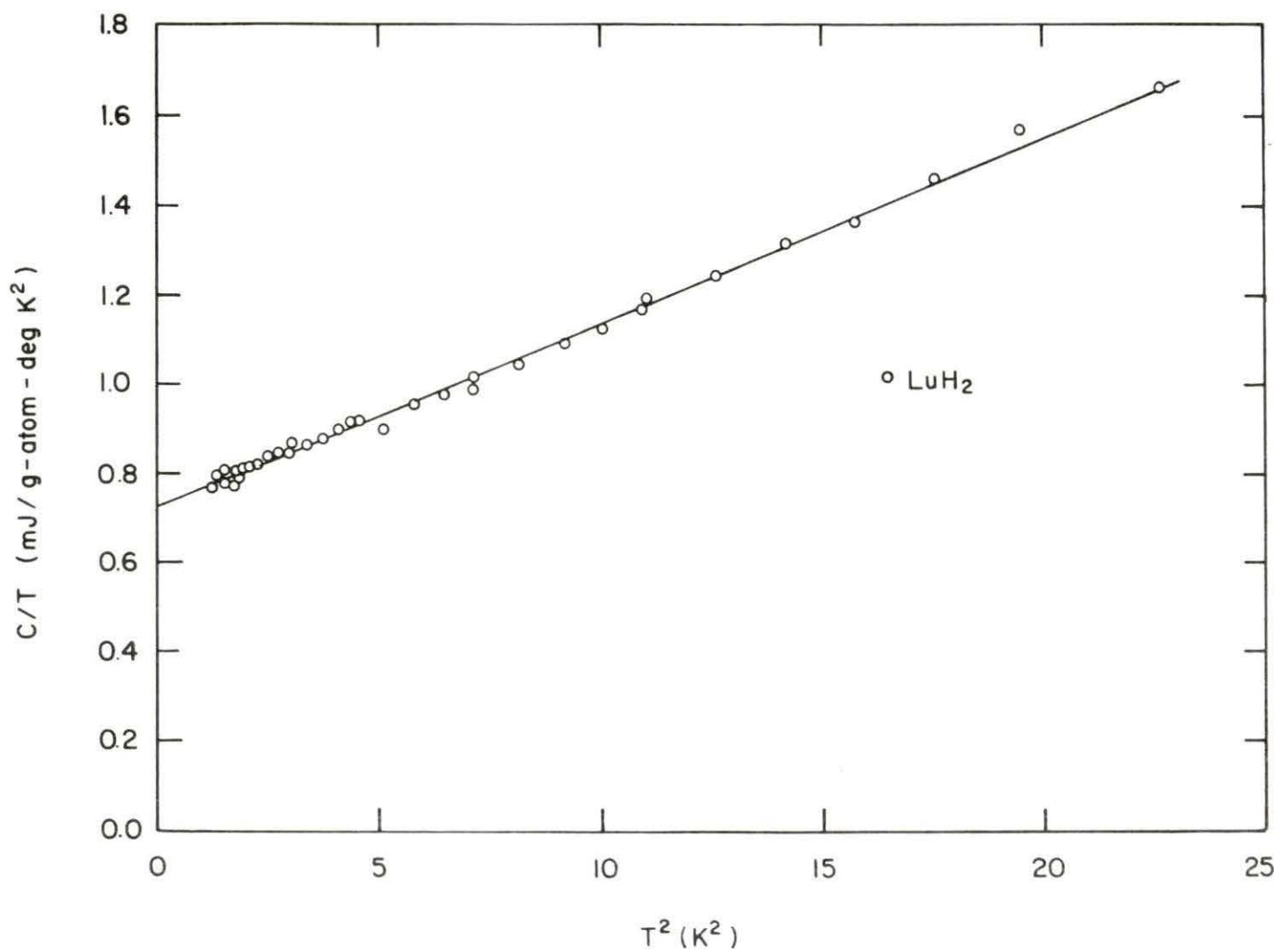


Figure 12. Measured heat capacity of lutetium dihydride

## SUMMARY

The heat capacity of high purity electrotransport refined lutetium was measured between 1 and 20 K. Results for  $\theta_D$  were in excellent agreement with  $\theta$  values determined from elastic constant measurements.

The heat capacity of a series of lutetium-hydrogen solid solution alloys was determined and results showed an increase in  $\gamma$  from 8.2 to about 11.3 mJ/g-atom-K<sup>2</sup> for hydrogen content increasing from zero to about one atomic percent. Above one percent hydrogen  $\gamma$  decreased with increasing hydrogen contents. The C/T data showed an increase with temperature decreasing below about 2.5 K for samples with 0.1 to 1.5 atomic percent hydrogen. This accounts for a large amount of scatter in  $\theta_D$  versus hydrogen content in this range.

The heat capacity of a bulk sample of lutetium dihydride was measured between 1 and 20 K and showed a large increase in  $\theta_D$  and a large decrease in  $\gamma$  compared to pure lutetium.

## REFERENCES

1. P. Wells, P. C. Lanchester, D. W. Jones, and R. G. Jordan, J. Phys. F, 6(1), 11 (1976).
2. L. D. Jennings, R. E. Miller, and F. H. Spedding, J. Chem. Phys., 33(6), 1849 (1960).
3. O. U. Lounasmaa, Phys. Rev., 133(1A), A219 (1964).
4. H. U. Culbert, Phys. Rev., 156(3), 701 (1967).
5. B. C. Gerstein, W. A. Taylor, W. D. Shickell, and F. H. Spedding, J. Chem. Phys., 51(7), 2924 (1969).
6. O. N. Carlson, F. A. Schmidt, and D. T. Peterson, J. Less-Common Metals, 39, 277 (1975).
7. E. S. R. Gopal, "Specific Heats at Low Temperatures," Plenum Press, New York, N.Y., 1966.
8. B. J. Beaudry and F. H. Spedding, Met. Trans., 6B, 419 (1975).
9. T.-W. E. Tsang, K. A. Gschneidner, Jr., and F. A. Schmidt, Solid State Commun., 20, 737 (1976).
10. A. Pebler and W. E. Wallace, J. Phys. Chem., 66, 148 (1962).
11. D. T. Peterson and E. N. Hopkins, AEC Report IS-1036, Iowa State University, October 1964.
12. D. W. Osborne, H. E. Flotow, and F. Schreiner, Rev. Sci. Inst., 38(2), 159 (1967).
13. J. J. Tonnes, K. A. Gschneidner, Jr., and F. H. Spedding, J. Appl. Phys., 42(9), 3275 (1971).
14. M. Zimmermann, G. Wolf, and K. Bohmhammel, Phys. Stat. Sol. (a), 31, 511 (1975).
15. G. J. Sellers, C. A. Anderson, and H. K. Birnbaum, Phys. Rev. B, 10(7), 2771 (1974).

16. J. N. Daou, A. Lucasson, and P. Lucasson, Solid State Commun., 19, 895 (1976).
17. Z. Bieganski, D. Gonzalez Alvarez, and F. W. Klaaijsen, Physica, 37, 153 (1967).
18. F. R. Kroeger and W. A. Rhinehart, Rev. Sci. Inst., 42(10), 1532 (1971).

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## APPENDIX A.

## DESCRIPTION OF CALORIMETER AND ELECTRONIC SYSTEM

### Calorimeter

The calorimeter used in this study is designed to measure small samples in the range of 1 K to 20 K. It operates on the heat pulse principle; a known amount of energy is applied to the sample and the temperature rise is measured. The ratio of the energy input to the change in temperature determines the heat capacity.

A diagram of the calorimeter is shown in Figure A1, and an enlarged view of the sample chamber shown in Figure A2 indicating the important features.

The sample holder was fabricated from 0.013 cm thick copper foil into the shape of a pan 1.6 cm in diameter with side walls 0.3 cm high. Six eyelets were silver soldered to the pan to support it in the calorimeter. A copper foil tab to hold a germanium resistance thermometer (GRT) and a copper wire thermal link to the helium pot were also silver soldered into place.

The GRT was a Cryocal, No. 3979, and was calibrated by Dr. C. A. Swenson's research group against two standard GRT's. The estimated accuracy is  $\pm 0.5$  mK from 1 K to 5 K and  $\pm 3.0$  mK above 5 K.

The heater is made of a length of 92 percent platinum, 8 percent tungsten wire wound noninductively around the side walls of the sample holder pan and secured with G.E. 7031 insulating varnish. This heater material was chosen for high strength and stability, low coefficient of resistance change with temperature and small heat capacity below 20 K.

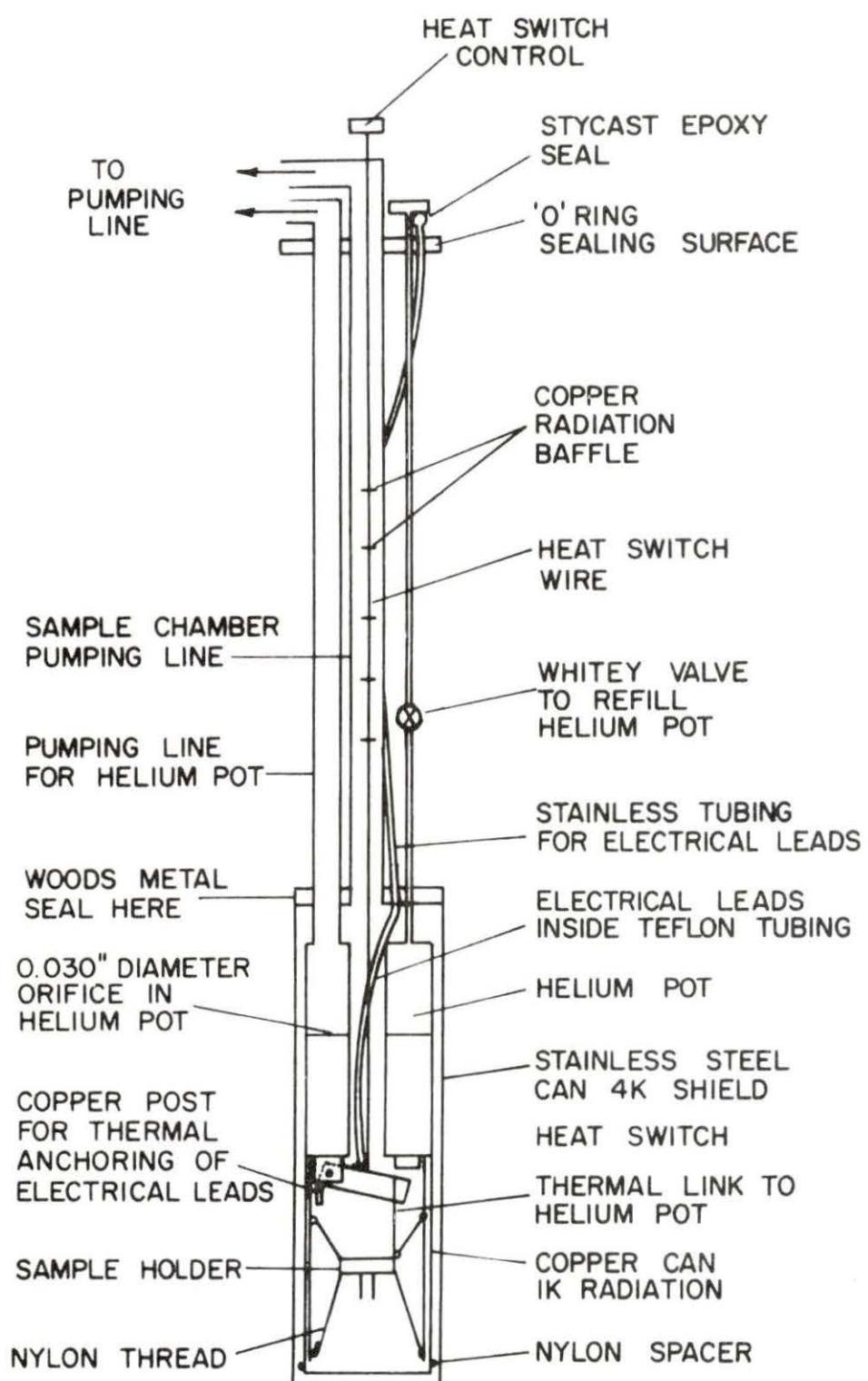


Figure A1. The low temperature calorimeter used in this study

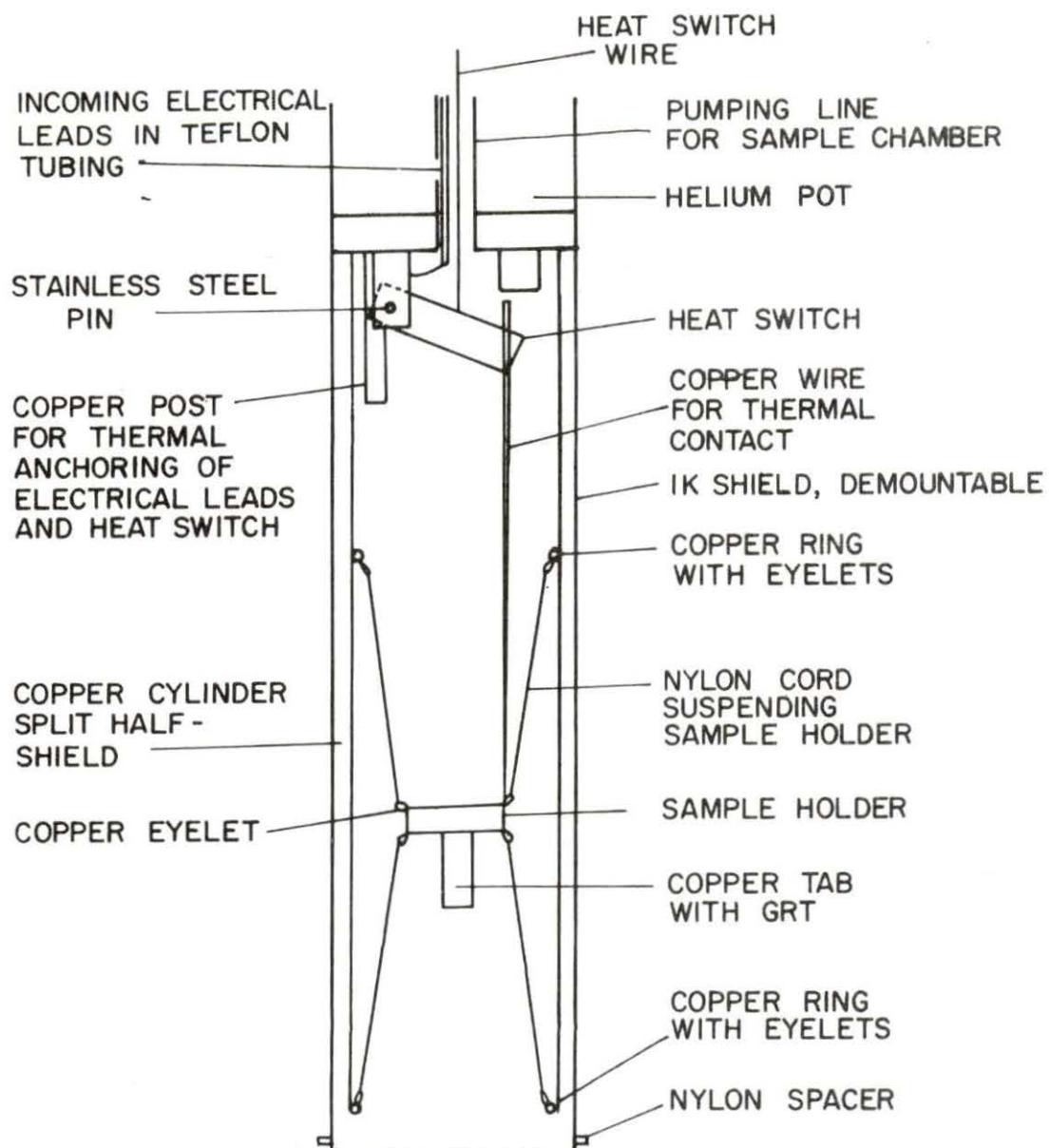


Figure A2. The sample chamber of the calorimeter

A copper half shield was mounted to the helium pot. This shield had two copper rings soldered to it with three eyelets on each ring to support the sample holder. The helium pot is a copper cylinder with a volume of about 100 cm<sup>3</sup>. Half way between the top and bottom is a plate with an orifice 0.08 cm in diameter. The orifice is necessary to control the evaporation of liquid helium below the lambda point when it becomes a superfluid. The pot is isolated from the reservoir by stainless steel tubes. Liquid helium from the reservoir enters the pot through a small stainless steel tube. A valve can be opened to allow helium to enter the pot and closed to maintain a vacuum on the pot to cool to 1 K.

A copper tube mounts directly onto the helium pot to provide a 1 K radiation shield. Outside this shield is the sample chamber vacuum can which is maintained at 4.2 K in the helium reservoir. This can is sealed to the system with Wood's metal to provide a good vacuum.

#### Electronic System

The electronic system for the calorimeter is most easily described in sections below.

##### The germanium resistance thermometer current circuit

The current to the GRT is supplied by 20 mercury cells in series with a large adjustable resistance. Mercury cells were chosen since they provide a stable voltage at low current drain and are isolated from A-C line voltage. This helps to eliminate grounding loops or A-C

line noise. By adjusting the series resistance, currents of 1, 2, 4, 6, 10, 20, or 50 microamperes can be supplied through shielded leads to the GRT.

#### The germanium resistance thermometer voltage circuit

The voltage drop across the GRT is measured with a Leeds and Northrup type K-5 potentiometer in series with a Keithley model 150B microvoltmeter. The potentiometer is used to "buck" most of the voltage signal of the GRT and the voltmeter measures the difference. The voltmeter provides an adjustable output to drive a Texas Instruments two pen strip chart recorder. The temperature drift is displayed and can be extrapolated to the midpoint of a heat pulse determined by the second pen of the recorder which indicates when the heater is on. The 100 or 30 microvolt full scale range is generally used below 4 K while the 10 microvolt full scale range is used above 4 K.

The potentiometer is used in a nonconventional way. Its power comes from a constant current supply<sup>18</sup> which was temperature compensated to drift less than 0.2 parts per million per degree centigrade. The potentiometer is standardized against a standard resistor rather than a standard voltage cell. Thermal emfs are taken into account. Although the accuracy of this method is not as good, the difference in voltage measured before and after the heat pulse is most important and this depends on the linearity and resolution of the potentiometer and not absolute value of the voltage measured. In any case, the voltage will be within about 0.02 percent of the true value. It should be mentioned

that extrapolation of the temperature to the midpoint of the heat pulse probably produces the largest error. The GRT electrical circuit is shown in Figure A3.

#### The heater circuit

The heater current is provided by an adjustable constant current supply.<sup>18</sup> The value of the current is determined by reading the voltage across one of two standard resistors with a Leeds and Northrup type K-5 potentiometer with a Keithley model 153 microvoltmeter used as a null detector. This circuit is shown in Figure A4. The duration of the heat pulse is measured with a Monsanto digital timer. The current to the heater, the timer, and the marker pen of the strip chart recorder are all triggered with a relay. The contacts were measured to close within two milliseconds of each other. The relay is well shielded from the GRT because it is possible for the GRT to detect any radio frequency interference produced on opening and closing the contacts.

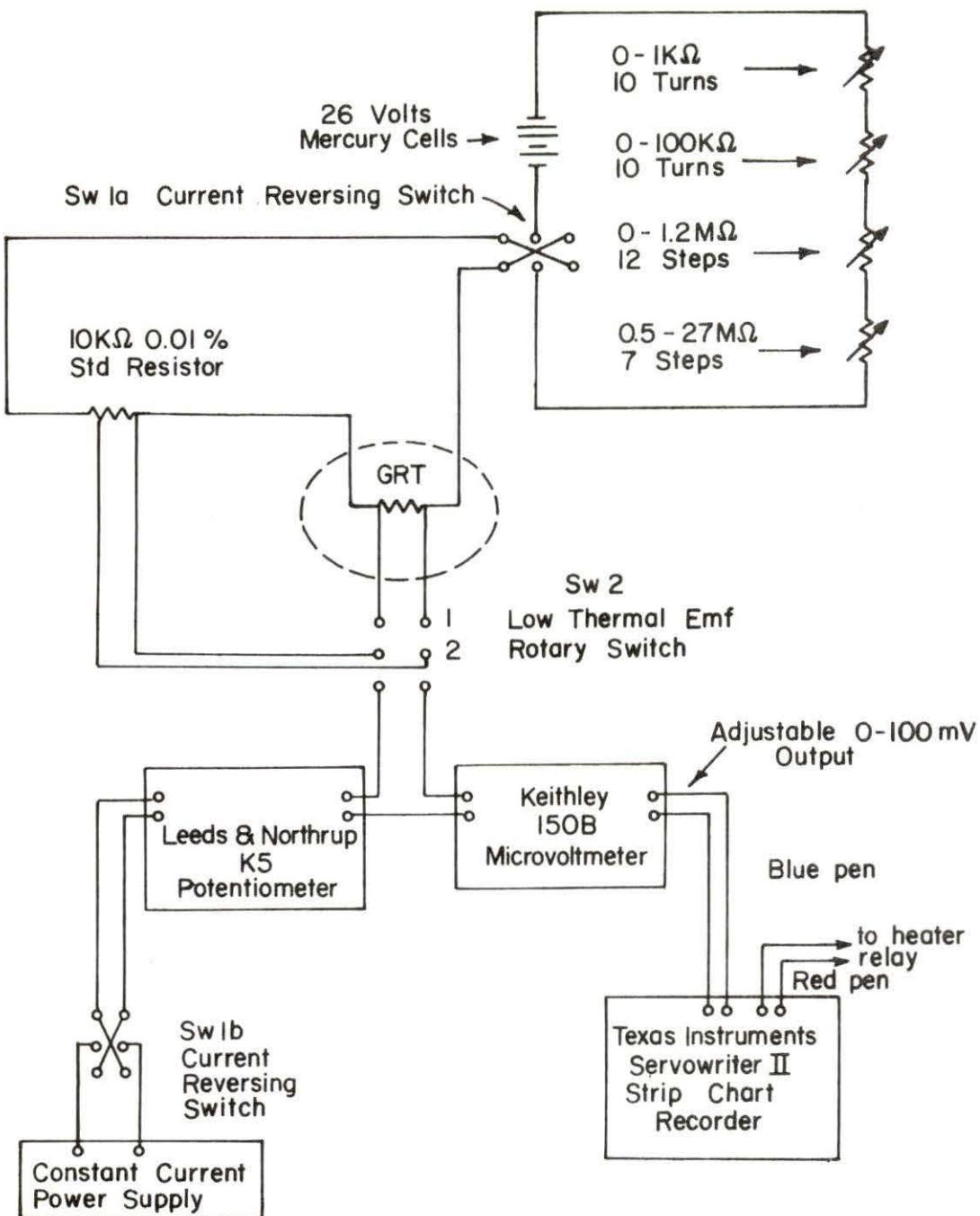


Figure A3. The GRT electrical circuit

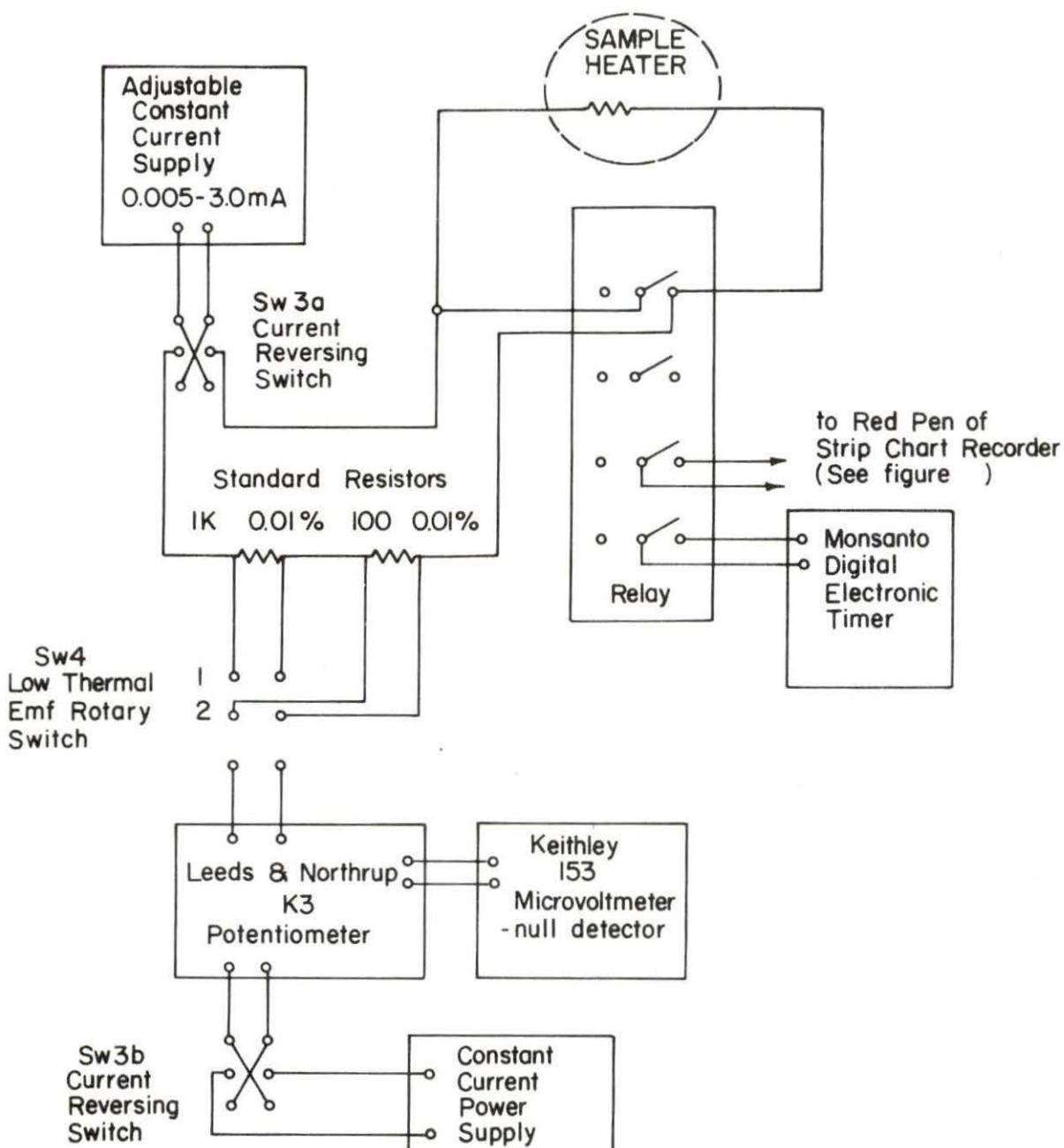


Figure A4. The heater electrical circuit

APPENDIX B.  
MEASURED HEAT CAPACITY DATA

Measured Heat Capacity  
Electrotransport Purified Lutetium Lu-II

| T<br>(K) | C<br>(mJ/g-atom K) | T<br>(K) | C<br>(mJ/g-atom K) |
|----------|--------------------|----------|--------------------|
| 1.1002   | 9.4759             | 2.7950   | 29.4524            |
| 1.1140   | 9.6992             | 2.9377   | 31.7668            |
| 1.1521   | 10.1331            | 2.9413   | 31.6561            |
| 1.1813   | 10.3619            | 3.0379   | 33.6610            |
| 1.2133   | 10.7558            | 3.0658   | 34.2634            |
| 1.2449   | 10.9547            | 3.1113   | 34.8535            |
| 1.2699   | 11.2166            | 3.1306   | 34.6380            |
| 1.2946   | 11.3528            | 3.2080   | 36.0852            |
| 1.3086   | 11.6300            | 3.2998   | 37.9786            |
| 1.3412   | 11.9930            | 3.3799   | 39.5973            |
| 1.3467   | 11.8061            | 3.4570   | 40.9215            |
| 1.3980   | 12.4260            | 3.5703   | 43.6896            |
| 1.4005   | 12.4423            | 3.6321   | 44.3400            |
| 1.4491   | 12.9056            | 3.7764   | 47.9411            |
| 1.4576   | 12.8979            | 3.8091   | 47.8538            |
| 1.4973   | 13.2308            | 4.0052   | 52.9783            |
| 1.5017   | 13.3949            | 4.0393   | 53.6913            |
| 1.5171   | 13.5950            | 4.3619   | 63.1144            |
| 1.5535   | 13.8952            | 4.6466   | 70.3057            |
| 1.5613   | 14.0971            | 4.9036   | 78.5177            |
| 1.6115   | 14.6202            | 5.1358   | 85.7013            |
| 1.6529   | 15.0761            | 5.3684   | 93.5235            |
| 1.6943   | 15.4537            | 5.5392   | 99.9378            |
| 1.7380   | 15.9338            | 5.7845   | 110.6941           |
| 1.7766   | 16.2827            | 6.0217   | 121.9334           |
| 1.8161   | 16.8168            | 6.2511   | 132.8087           |
| 1.8487   | 16.9757            | 6.4805   | 146.3423           |
| 1.8617   | 17.2269            | 6.6187   | 152.3252           |
| 1.8931   | 17.7401            | 6.9337   | 171.5012           |
| 1.9345   | 18.1559            | 7.2735   | 193.4307           |
| 1.9605   | 18.3410            | 7.6360   | 222.3626           |
| 1.9809   | 18.6312            | 7.9895   | 250.6632           |
| 2.0761   | 19.8174            | 8.2432   | 272.1692           |
| 2.1195   | 20.2670            | 8.6407   | 313.7038           |
| 2.2193   | 21.5718            | 9.0587   | 360.2911           |
| 2.2698   | 21.9689            | 9.4895   | 415.8232           |
| 2.3642   | 23.3512            | 9.9166   | 476.4196           |
| 2.3952   | 23.7958            | 10.2184  | 522.6489           |
| 2.3968   | 23.7852            | 10.6709  | 606.2042           |
| 2.4868   | 25.2139            | 11.1132  | 686.4376           |
| 2.4877   | 24.7173            | 11.5495  | 767.8185           |
| 2.5907   | 26.6378            | 11.9984  | 878.4180           |
| 2.6572   | 27.6377            | 12.3589  | 965.6098           |
| 2.7639   | 28.8256            | 12.8456  | 1089.4806          |

Measured Heat Capacity  
Electrotransport Purified Lutetium Lu-II  
 (continued)

| T<br>(K) | C<br>(mJ/g-atom K) | T<br>(K) | C<br>(mJ/g-atom K) |
|----------|--------------------|----------|--------------------|
| 13.3472  | 1216.8488          | 16.3071  | 2209.5882          |
| 13.8601  | 1379.5632          | 17.0255  | 2483.5787          |
| 14.3704  | 1530.9248          | 17.7582  | 2781.2714          |
| 14.9103  | 1711.1504          | 18.3406  | 3050.7342          |
| 15.6564  | 1965.5492          | 19.1055  | 3378.5711          |

Measured Heat Capacity  
Electrotransport Purified Lutetium Lu-III

| T<br>(K) | C<br>(mJ/g-atom K) | T<br>(K) | C<br>(mJ/g-atom K) |
|----------|--------------------|----------|--------------------|
| 1.1085   | 7.3976             | 1.9477   | 18.3047            |
| 1.1953   | 10.3512            | 1.9633   | 18.4969            |
| 1.2043   | 10.6969            | 2.0197   | 18.6497            |
| 1.2333   | 10.7555            | 2.0552   | 19.6313            |
| 1.2604   | 11.1818            | 2.1504   | 20.7295            |
| 1.2782   | 11.2225            | 2.1820   | 21.2058            |
| 1.3031   | 11.6550            | 2.2383   | 21.8254            |
| 1.3154   | 11.7268            | 2.3158   | 22.8195            |
| 1.3188   | 11.7402            | 2.4348   | 24.3876            |
| 1.3715   | 12.4538            | 2.4468   | 24.3004            |
| 1.3760   | 12.4372            | 2.4941   | 25.1183            |
| 1.4309   | 12.8205            | 2.5205   | 26.1830            |
| 1.4329   | 13.1164            | 2.6094   | 26.8799            |
| 1.4330   | 12.9097            | 2.6041   | 26.9635            |
| 1.4858   | 13.1193            | 2.6460   | 27.5867            |
| 1.4971   | 13.4633            | 2.6959   | 27.7038            |
| 1.5051   | 13.6440            | 2.7441   | 28.7537            |
| 1.5497   | 14.7248            | 2.7936   | 29.3324            |
| 1.5707   | 14.2213            | 2.8187   | 30.0170            |
| 1.6069   | 14.8409            | 2.8877   | 30.9694            |
| 1.6340   | 14.8077            | 2.9540   | 32.0563            |
| 1.6622   | 15.2416            | 2.9911   | 32.6408            |
| 1.7001   | 15.6030            | 3.0505   | 33.6517            |
| 1.7097   | 15.5765            | 3.0639   | 34.2505            |
| 1.7289   | 15.9764            | 3.0741   | 34.2138            |
| 1.7547   | 16.1306            | 3.1454   | 35.4723            |
| 1.8124   | 16.6910            | 3.1584   | 35.7206            |
| 1.8462   | 17.0698            | 3.2269   | 36.8447            |
| 1.8939   | 17.7675            | 3.2399   | 37.3538            |
| 1.9381   | 18.2223            | 3.3378   | 55.6962            |

Measured Heat Capacity  
Electrotransport Purified Lutetium Lu-III  
(continued)

| T<br>(K) | C<br>(mJ/g-atom K) | T<br>(K) | C<br>(mJ/g-atom K) |
|----------|--------------------|----------|--------------------|
| 3.5067   | 42.3757            | 8.9886   | 355.9257           |
| 3.5461   | 43.5320            | 9.3194   | 391.1468           |
| 3.8074   | 49.0397            | 9.3323   | 401.9046           |
| 3.8459   | 50.2536            | 9.6845   | 442.7364           |
| 4.0834   | 54.8166            | 9.7940   | 456.5090           |
| 4.1178   | 56.0110            | 9.9384   | 483.5313           |
| 4.2370   | 59.7831            | 10.1684  | 513.5643           |
| 4.3487   | 62.4770            | 10.3576  | 553.1702           |
| 4.5239   | 68.1006            | 10.5469  | 574.1437           |
| 4.6248   | 71.4257            | 10.7805  | 625.7976           |
| 4.7806   | 76.0923            | 10.9225  | 639.9161           |
| 4.8693   | 77.9267            | 11.2088  | 706.1090           |
| 4.9935   | 82.8055            | 11.3287  | 722.9549           |
| 5.0996   | 84.3419            | 11.6254  | 798.7890           |
| 5.1984   | 86.7892            | 11.7747  | 830.6457           |
| 5.3144   | 92.2274            | 11.9194  | 867.1964           |
| 5.3547   | 93.7047            | 12.1166  | 886.8952           |
| 5.4539   | 97.3005            | 12.3573  | 959.5770           |
| 5.6092   | 103.5144           | 12.6345  | 1020.1940          |
| 5.6914   | 107.6844           | 12.8312  | 1079.2488          |
| 5.8816   | 113.9250           | 13.1608  | 1158.6059          |
| 5.9434   | 119.6003           | 13.3248  | 1216.7911          |
| 6.1752   | 130.4948           | 13.6971  | 1317.8618          |
| 6.2141   | 132.4939           | 13.8289  | 1360.6552          |
| 6.4915   | 146.1845           | 14.1987  | 1476.6976          |
| 6.5270   | 149.5337           | 14.2364  | 1478.7927          |
| 6.7019   | 157.4147           | 14.6211  | 1606.5893          |
| 6.7610   | 162.6281           | 14.7394  | 1648.4248          |
| 7.0051   | 175.1446           | 15.0234  | 1713.7788          |
| 7.1123   | 183.4913           | 15.2526  | 1850.9116          |
| 7.3144   | 194.9061           | 15.7509  | 2007.0235          |
| 7.4410   | 206.2609           | 15.7828  | 2016.0227          |
| 7.6025   | 216.6403           | 16.4309  | 2259.3654          |
| 7.7681   | 230.9869           | 16.6136  | 2310.5378          |
| 7.9249   | 247.2211           | 16.9958  | 2501.9633          |
| 8.0930   | 260.2474           | 17.2966  | 2597.2951          |
| 8.1846   | 269.0172           | 17.7317  | 2798.5570          |
| 8.3154   | 282.2106           | 18.0047  | 2841.5835          |
| 8.5455   | 304.6897           | 19.2351  | 3443.9809          |
| 8.6571   | 314.5982           | 19.2351  | 3443.9809          |
| 8.9137   | 344.8518           | 19.9894  | 3772.1252          |

| Measured Heat Capacity                     |                    |          |                    |
|--|--------------------|----------|--------------------|
| Lutetium Starting Material                 |                    | Lu-IB    |                    |
| Annealed in High Vacuum to Remove Hydrogen |                    |          |                    |
| T<br>(K)                                   | C<br>(mJ/g-atom K) | T<br>(K) | C<br>(mJ/g-atom K) |
| 1.0505                                     | 9.0631             | 2.5817   | 26.7023            |
| 1.0710                                     | 9.6160             | 2.6163   | 27.2636            |
| 1.1049                                     | 9.9960             | 2.6931   | 28.3111            |
| 1.1237                                     | 10.1405            | 2.7374   | 28.8426            |
| 1.1590                                     | 10.4130            | 2.8500   | 30.5457            |
| 1.1769                                     | 10.6548            | 2.8619   | 30.6943            |
| 1.2100                                     | 10.8950            | 2.8755   | 30.9231            |
| 1.2285                                     | 11.0393            | 2.8857   | 31.2519            |
| 1.2616                                     | 11.4365            | 3.0175   | 33.3870            |
| 1.2790                                     | 11.4892            | 3.0637   | 34.1007            |
| 1.2958                                     | 11.7494            | 3.1554   | 35.7694            |
| 1.3126                                     | 11.8237            | 3.2017   | 36.5739            |
| 1.3462                                     | 12.2075            | 3.2194   | 36.9464            |
| 1.3601                                     | 12.2468            | 3.3784   | 41.6728            |
| 1.3944                                     | 12.5219            | 3.4330   | 40.8790            |
| 1.4103                                     | 12.7655            | 3.4727   | 41.8308            |
| 1.4490                                     | 13.2219            | 3.6421   | 45.2197            |
| 1.4677                                     | 13.3603            | 3.6912   | 46.0586            |
| 1.5105                                     | 13.8708            | 3.7040   | 46.4822            |
| 1.5225                                     | 14.0318            | 3.8846   | 50.2348            |
| 1.5270                                     | 14.0017            | 3.9264   | 51.2876            |
| 1.5457                                     | 14.1077            | 4.0648   | 54.6921            |
| 1.5867                                     | 14.6782            | 4.1506   | 56.4449            |
| 1.6209                                     | 14.9472            | 4.2239   | 58.2255            |
| 1.6516                                     | 15.3353            | 4.2489   | 59.2496            |
| 1.6946                                     | 15.6581            | 4.3370   | 61.7720            |
| 1.7175                                     | 16.0072            | 4.4337   | 64.4631            |
| 1.7784                                     | 16.6724            | 4.5923   | 68.8294            |
| 1.8137                                     | 17.0638            | 4.6131   | 60.5558            |
| 1.8437                                     | 17.3018            | 4.7862   | 73.8840            |
| 1.8776                                     | 17.8183            | 4.8451   | 76.3241            |
| 1.9127                                     | 18.1966            | 4.9639   | 79.8659            |
| 1.9868                                     | 19.0740            | 5.0796   | 83.7594            |
| 2.0448                                     | 19.6997            | 5.0955   | 84.1803            |
| 2.1249                                     | 20.6745            | 5.2631   | 89.2872            |
| 2.1753                                     | 21.3459            | 5.3372   | 93.1484            |
| 2.2561                                     | 22.3137            | 5.4660   | 97.3166            |
| 2.2935                                     | 22.8397            | 5.5167   | 99.6631            |
| 2.3786                                     | 23.8864            | 5.6694   | 105.3249           |
| 2.3997                                     | 23.8218            | 5.7548   | 109.4985           |
| 2.4088                                     | 24.3092            | 5.8761   | 114.0858           |
| 2.4156                                     | 24.4010            | 5.9824   | 119.8639           |
| 2.4829                                     | 25.2917            | 6.0279   | 120.7354           |
| 2.5160                                     | 25.7447            | 6.2200   | 130.5434           |

Measured Heat Capacity  
Lutetium Starting Material Lu-IB  
 (continued)

| T<br>(K) | C<br>(mJ/g-atom K) | T<br>(K) | C<br>(mJ/g-atom K) |
|----------|--------------------|----------|--------------------|
| 6.2566   | 131.4415           | 11.2127  | 699.9024           |
| 6.4971   | 144.8538           | 11.4928  | 759.4155           |
| 6.5353   | 146.8586           | 11.5348  | 763.4597           |
| 6.7089   | 157.4330           | 11.8926  | 843.6417           |
| 6.8332   | 163.6131           | 12.0514  | 876.4965           |
| 7.0060   | 175.0904           | 12.3152  | 937.7007           |
| 7.1353   | 182.8090           | 12.5495  | 1003.1395          |
| 7.3010   | 195.9489           | 12.7391  | 1044.5113          |
| 7.3022   | 191.0609           | 13.1168  | 1145.6179          |
| 7.5410   | 211.2378           | 13.1604  | 1159.2817          |
| 7.5896   | 215.8600           | 13.5044  | 1263.3887          |
| 7.8114   | 232.2938           | 13.6862  | 1308.6165          |
| 7.8714   | 239.0965           | 13.9428  | 1387.8648          |
| 8.0725   | 256.3312           | 14.3369  | 1492.0721          |
| 8.1284   | 260.5662           | 14.4380  | 1532.3568          |
| 8.4220   | 289.1648           | 14.9840  | 1716.7614          |
| 8.4665   | 294.2588           | 14.9889  | 1725.7706          |
| 8.7748   | 325.3528           | 15.5613  | 1926.7307          |
| 8.7883   | 327.4636           | 15.6387  | 1959.3108          |
| 9.1603   | 371.5006           | 16.0551  | 2101.7685          |
| 9.2163   | 376.8634           | 16.2844  | 2188.0255          |
| 9.5326   | 420.7375           | 16.6615  | 2339.8897          |
| 9.6595   | 435.5667           | 16.8397  | 2395.0597          |
| 9.7479   | 452.1601           | 17.2641  | 2581.1618          |
| 10.096   | 500.0269           | 17.4518  | 2656.7325          |
| 10.1356  | 508.1984           | 17.8923  | 2842.5141          |
| 10.5160  | 571.1835           | 18.0613  | 2894.7508          |
| 10.5887  | 580.6920           | 18.5861  | 3142.6422          |
| 10.8687  | 634.7414           | 18.7358  | 3174.0549          |
| 11.0188  | 658.5830           | 19.5009  | 3561.9654          |

Measured Heat Capacity  
Lutetium Starting Material Lu-IIA

| T<br>(K) | C<br>(mJ/g-atom K) | T<br>(K) | C<br>(mJ/g-atom K) |
|----------|--------------------|----------|--------------------|
| 1.0614   | 10.9127            | 1.1744   | 11.9663            |
| 1.0950   | 11.2562            | 1.2144   | 12.4443            |
| 1.0997   | 11.2274            | 1.2156   | 12.4857            |
| 1.1332   | 11.7131            | 1.2517   | 12.8137            |
| 1.1371   | 11.9152            | 1.2948   | 13.1433            |

Measured Heat Capacity  
Lutetium Starting Material Lu-IIA  
(continued)

| T<br>(K) | C<br>(mJ/g-atom K) | T<br>(K) | C<br>(mJ/g-atom K) |
|----------|--------------------|----------|--------------------|
| 1.3262   | 13.3754            | 3.4836   | 43.2095            |
| 1.3386   | 13.4936            | 3.4925   | 43.5677            |
| 1.3819   | 14.0373            | 3.6975   | 47.4791            |
| 1.3947   | 14.1472            | 3.7974   | 49.6563            |
| 1.4256   | 14.4059            | 3.9282   | 52.6912            |
| 1.4628   | 14.8276            | 4.0288   | 54.8980            |
| 1.4736   | 14.8895            | 4.1326   | 57.2944            |
| 1.4926   | 15.1185            | 4.1624   | 57.9918            |
| 1.5322   | 15.5669            | 4.1626   | 57.9867            |
| 1.5495   | 15.6625            | 4.3063   | 61.6154            |
| 1.6089   | 16.3371            | 4.3109   | 62.1077            |
| 1.6121   | 16.3580            | 4.3587   | 63.1538            |
| 1.6475   | 16.7236            | 4.4586   | 65.4256            |
| 1.6705   | 16.9518            | 4.4570   | 65.3944            |
| 1.6866   | 17.0297            | 4.5014   | 67.4070            |
| 1.7480   | 17.8139            | 4.6088   | 69.6967            |
| 1.7782   | 18.0954            | 4.6937   | 72.5118            |
| 1.8556   | 19.0567            | 4.8759   | 78.3333            |
| 1.8837   | 19.9082            | 4.8832   | 78.8187            |
| 1.9663   | 20.2327            | 5.0269   | 82.7686            |
| 1.9938   | 20.6004            | 5.0731   | 84.4688            |
| 2.0853   | 21.6154            | 5.1821   | 87.6067            |
| 2.0987   | 21.7463            | 5.2120   | 88.7395            |
| 2.1320   | 22.1859            | 5.3540   | 94.0131            |
| 2.1995   | 22.9795            | 5.4098   | 95.9667            |
| 2.2390   | 23.4398            | 5.4876   | 98.9879            |
| 2.2524   | 23.6406            | 5.6059   | 104.0069           |
| 2.3660   | 24.9579            | 5.6791   | 106.4766           |
| 2.3687   | 25.0019            | 5.7900   | 111.6316           |
| 2.4725   | 26.4863            | 5.8712   | 114.5807           |
| 2.4791   | 26.5369            | 5.9678   | 119.6224           |
| 2.5743   | 27.9377            | 6.0682   | 123.7243           |
| 2.5801   | 28.1481            | 6.0823   | 124.5201           |
| 2.5825   | 27.9099            | 6.2656   | 133.3352           |
| 2.7007   | 29.7628            | 6.2933   | 134.5784           |
| 2.7456   | 30.5015            | 6.4353   | 142.5782           |
| 2.7743   | 37.9122            | 6.5110   | 146.1939           |
| 2.9161   | 34.5050            | 6.6366   | 153.7867           |
| 2.9518   | 33.6956            | 6.7846   | 161.6997           |
| 3.0597   | 35.4790            | 6.8505   | 166.0191           |
| 3.1564   | 37.1421            | 6.9914   | 174.8447           |
| 3.2794   | 39.5135            | 7.0711   | 180.4936           |
| 3.3463   | 40.2957            | 7.2331   | 190.4621           |
| 3.3575   | 40.7435            | 7.3455   | 197.9740           |

Measured Heat Capacity  
Lutetium Starting Material Lu-IA  
 (continued)

| T<br>(K) | C<br>(mJ/g-atom K) | T<br>(K) | C<br>(mJ/g-atom K) |
|----------|--------------------|----------|--------------------|
| 7.4842   | 207.4192           | 11.7969  | 819.4511           |
| 7.6371   | 220.5103           | 11.8457  | 829.0468           |
| 7.7386   | 226.7782           | 12.1856  | 909.9584           |
| 7.8068   | 234.7255           | 12.2778  | 928.2906           |
| 7.9807   | 245.8699           | 12.5959  | 1005.3076          |
| 8.0699   | 255.3348           | 12.7143  | 1036.5043          |
| 8.1456   | 263.1248           | 13.0124  | 1120.5435          |
| 8.3578   | 283.0139           | 13.0858  | 1137.6473          |
| 8.3779   | 284.6780           | 13.4591  | 1237.5927          |
| 8.6158   | 308.9873           | 13.5695  | 1269.1684          |
| 8.6703   | 314.2122           | 13.8706  | 1358.9108          |
| 8.8666   | 336.0783           | 14.1242  | 1435.9653          |
| 9.0409   | 381.1837           | 14.4054  | 1527.9997          |
| 9.1071   | 365.2783           | 14.6922  | 1616.8371          |
| 9.2383   | 378.0958           | 14.9937  | 1721.0984          |
| 9.3096   | 390.1960           | 15.2765  | 1826.8735          |
| 9.5041   | 415.5198           | 15.6077  | 1933.3717          |
| 9.6728   | 437.2132           | 15.7774  | 1993.2396          |
| 9.7694   | 450.8247           | 16.2814  | 2183.0034          |
| 10.0274  | 489.4220           | 16.4061  | 2232.3780          |
| 10.0321  | 488.2359           | 17.0112  | 2468.7946          |
| 10.2930  | 532.0964           | 17.0431  | 2477.9542          |
| 10.3907  | 547.0232           | 17.6864  | 2745.2884          |
| 10.4746  | 562.5864           | 17.7182  | 2746.9543          |
| 10.7397  | 607.2995           | 18.2866  | 2987.6072          |
| 10.7412  | 609.5718           | 18.4075  | 3052.5756          |
| 11.0189  | 659.0590           | 18.8824  | 3273.2062          |
| 11.0314  | 661.7195           | 19.1829  | 3401.3260          |
| 11.3016  | 716.8668           | 19.5108  | 3548.0618          |
| 11.4313  | 740.4925           | 20.0330  | 3770.2022          |
| 11.5870  | 778.2833           |          |                    |

Measured Heat Capacity  
Lutetium Starting Material Lu-IC

| T<br>(K) | C<br>(mJ/g-atom K) | T<br>(K) | C<br>(mJ/g-atom K) |
|----------|--------------------|----------|--------------------|
| 1.0912   | 10.3389            | 1.2227   | 11.0049            |
| 1.1044   | 10.8006            | 1.2384   | 12.4648            |
| 1.1570   | 10.8525            | 1.2832   | 12.2524            |
| 1.1741   | 11.8624            | 1.3004   | 13.1003            |

Measured Heat Capacity  
Lutetium Starting Material Lu-IC  
(continued)

| T<br>(K) | C<br>(mJ/g-atom K) | T<br>(K) | C<br>(mJ/g-atom K) |
|----------|--------------------|----------|--------------------|
| 1.3413   | 12.9611            | 3.5377   | 44.1834            |
| 1.3644   | 13.8466            | 3.6135   | 45.7231            |
| 1.3782   | 13.4290            | 3.7106   | 47.7738            |
| 1.4307   | 14.4454            | 3.8030   | 49.6577            |
| 1.4463   | 14.4524            | 3.8950   | 51.4505            |
| 1.4727   | 14.9407            | 3.9960   | 53.9687            |
| 1.5160   | 15.2438            | 4.0790   | 55.8930            |
| 1.5478   | 15.6786            | 4.1791   | 58.3836            |
| 1.5773   | 15.9031            | 4.3496   | 62.8676            |
| 1.6274   | 16.4972            | 4.6264   | 70.7687            |
| 1.6468   | 16.6022            | 4.8987   | 79.0503            |
| 1.6743   | 16.9545            | 5.1671   | 87.5900            |
| 1.7073   | 17.2936            | 5.4224   | 97.4349            |
| 1.7372   | 17.5932            | 5.6144   | 104.6609           |
| 1.7562   | 17.7934            | 5.8704   | 114.8795           |
| 1.8141   | 18.4162            | 6.1489   | 127.8593           |
| 1.8477   | 18.9156            | 6.4584   | 144.1767           |
| 1.9122   | 19.6945            | 6.7743   | 162.4254           |
| 1.9641   | 20.2001            | 7.0292   | 174.7694           |
| 2.0410   | 21.1571            | 7.3575   | 197.8804           |
| 2.0885   | 21.6388            | 7.6740   | 222.3168           |
| 2.1377   | 22.3199            | 7.9872   | 251.8607           |
| 2.1692   | 22.6925            | 8.3028   | 278.9954           |
| 2.2043   | 23.0804            | 8.5829   | 304.2144           |
| 2.2753   | 24.0170            | 8.9669   | 346.2497           |
| 2.3396   | 24.8286            | 9.3572   | 395.1786           |
| 2.4052   | 25.7977            | 9.7479   | 447.3551           |
| 2.4798   | 26.6125            | 10.1441  | 508.1296           |
| 2.5308   | 27.3959            | 10.2794  | 530.9400           |
| 2.5689   | 28.0966            | 10.6880  | 602.4898           |
| 2.5914   | 28.2919            | 11.0752  | 669.9838           |
| 2.6463   | 29.0658            | 11.4543  | 748.9943           |
| 2.7108   | 29.9998            | 11.8474  | 831.8530           |
| 2.7153   | 29.9994            | 12.1730  | 904.0403           |
| 2.7372   | 30.3624            | 12.6151  | 1011.6189          |
| 2.8754   | 32.3676            | 13.0593  | 1126.3221          |
| 2.8964   | 32.8564            | 13.5003  | 1259.7123          |
| 3.0286   | 34.8620            | 13.9895  | 1393.7903          |
| 3.0394   | 35.0201            | 14.4524  | 1539.2630          |
| 3.1970   | 37.7894            | 15.0909  | 1747.4623          |
| 3.2135   | 38.2050            | 15.7505  | 1994.7634          |
| 3.3557   | 40.5983            | 16.3623  | 2217.9393          |
| 3.3750   | 41.3330            | 17.0487  | 2482.0385          |
| 3.4230   | 41.9163            | 17.6609  | 2717.0718          |

Measured Heat Capacity  
Lutetium + 0.22 Atomic Percent Hydrogen  
Sample 2-20

| T<br>(K) | C<br>(mJ/g-atom K) | T<br>(K) | C<br>(mJ/g-atom K) |
|----------|--------------------|----------|--------------------|
| 1.0964   | 12.0087            | 2.9367   | 34.2985            |
| 1.1015   | 11.8769            | 3.0332   | 36.1068            |
| 1.1635   | 12.6692            | 3.0602   | 36.5145            |
| 1.1680   | 12.7146            | 3.1737   | 38.3507            |
| 1.2287   | 13.3263            | 3.1912   | 38.8515            |
| 1.2301   | 13.2808            | 3.2227   | 39.0831            |
| 1.2875   | 13.7381            | 3.3145   | 40.8662            |
| 1.2934   | 13.8941            | 3.3268   | 40.7490            |
| 1.3422   | 14.3554            | 3.4276   | 42.8297            |
| 1.3586   | 14.6533            | 3.5207   | 44.5834            |
| 1.3744   | 14.8619            | 3.6193   | 46.6709            |
| 1.4061   | 15.0868            | 3.6950   | 48.1959            |
| 1.4300   | 15.4794            | 3.8305   | 51.0003            |
| 1.4811   | 15.7998            | 3.8706   | 51.8833            |
| 1.4909   | 15.8488            | 4.0202   | 55.2022            |
| 1.5551   | 16.7090            | 4.0675   | 56.5852            |
| 1.5596   | 16.6653            | 4.2060   | 60.6367            |
| 1.6200   | 17.4824            | 4.3667   | 64.0260            |
| 1.6334   | 17.4520            | 4.6556   | 70.8603            |
| 1.6436   | 17.5206            | 4.9499   | 80.4300            |
| 1.7084   | 18.0978            | 5.2340   | 90.1916            |
| 1.7110   | 18.3142            | 5.4937   | 99.9790            |
| 1.7242   | 18.3165            | 5.6935   | 107.1439           |
| 1.8136   | 19.4015            | 5.9264   | 117.0916           |
| 1.8187   | 19.6117            | 6.1543   | 128.3171           |
| 1.9319   | 20.9351            | 6.4038   | 139.7203           |
| 1.9445   | 20.8737            | 6.7369   | 160.5835           |
| 2.0496   | 22.1371            | 6.9758   | 173.8628           |
| 2.0695   | 22.3802            | 7.2445   | 189.0724           |
| 2.1058   | 22.8031            | 7.5443   | 209.7884           |
| 2.1076   | 22.8493            | 7.8568   | 235.1154           |
| 2.2468   | 24.6084            | 8.1660   | 264.1828           |
| 2.2617   | 24.6907            | 8.3930   | 284.4982           |
| 2.3805   | 26.2949            | 8.7833   | 324.7168           |
| 2.3909   | 26.2775            | 9.1641   | 369.9371           |
| 2.5161   | 28.2272            | 9.5475   | 420.1764           |
| 2.5164   | 27.9328            | 9.9352   | 474.3863           |
| 2.6188   | 29.6207            | 10.2054  | 514.1752           |
| 2.6273   | 29.7119            | 10.6095  | 583.4749           |
| 2.6411   | 29.7072            | 11.0386  | 662.6411           |
| 2.7634   | 31.4369            | 11.4717  | 744.9990           |
| 2.7729   | 31.7451            | 11.8883  | 835.9614           |
| 2.8067   | 32.1216            | 12.2351  | 914.1579           |
| 2.8972   | 33.6632            | 12.6911  | 1022.2498          |

Measured Heat Capacity  
Lutetium + 0.22 Atomic Percent Hydrogen  
 (continued)

| T<br>(K) | C<br>(mJ/g-atom K) | T<br>(K) | C<br>(mJ/g-atom K) |
|----------|--------------------|----------|--------------------|
| 13.1401  | 1143.9450          | 16.4604  | 2243.9163          |
| 13.5736  | 1309.8432          | 17.1242  | 2510.8991          |
| 14.0918  | 1419.9196          | 17.7770  | 2766.9189          |
| 14.6930  | 1607.5669          | 18.3835  | 3031.6097          |
| 15.1683  | 1771.5749          | 18.9942  | 3349.0067          |
| 15.8179  | 2010.0936          |          |                    |

Measured Heat Capacity  
Lutetium + 0.70 Atomic Percent Hydrogen  
 Sample 2-21

| T<br>(K) | C<br>(mJ/g-atom K) | T<br>(K) | C<br>(mJ/g-atom K) |
|----------|--------------------|----------|--------------------|
| 1.0794   | 12.8265            | 2.1382   | 25.6710            |
| 1.0869   | 12.8860            | 2.2140   | 26.7234            |
| 1.1340   | 13.6106            | 2.2538   | 27.2392            |
| 1.1487   | 13.5574            | 2.2562   | 27.1769            |
| 1.1889   | 14.1300            | 2.3379   | 28.3065            |
| 1.2115   | 14.2355            | 2.3873   | 28.9218            |
| 1.2418   | 14.7259            | 2.4493   | 29.8133            |
| 1.2724   | 14.9870            | 2.5085   | 30.7696            |
| 1.2942   | 15.3758            | 2.5529   | 31.4177            |
| 1.3265   | 15.8584            | 2.5656   | 31.6005            |
| 1.3330   | 15.8907            | 2.6266   | 32.7244            |
| 1.3838   | 16.4187            | 2.6539   | 32.7895            |
| 1.3863   | 16.5152            | 2.6933   | 33.4418            |
| 1.4515   | 17.2070            | 2.7878   | 34.7673            |
| 1.4548   | 17.1900            | 2.8321   | 35.5333            |
| 1.5226   | 18.0422            | 2.9336   | 37.2765            |
| 1.5259   | 18.0973            | 2.9647   | 37.5727            |
| 1.5977   | 18.9412            | 3.0653   | 39.4333            |
| 1.5983   | 18.9517            | 3.1008   | 40.0469            |
| 1.6347   | 19.3591            | 3.2103   | 42.0060            |
| 1.6679   | 19.7291            | 3.2289   | 42.2455            |
| 1.6856   | 19.8679            | 3.2289   | 42.2190            |
| 1.7153   | 20.3066            | 3.2664   | 42.9064            |
| 1.7825   | 21.2801            | 3.3918   | 45.2314            |
| 1.8075   | 21.6003            | 3.4235   | 45.7796            |
| 1.8964   | 22.6740            | 3.5642   | 48.7208            |
| 1.9142   | 22.8994            | 3.5758   | 48.8509            |
| 2.0141   | 24.1386            | 3.7221   | 51.6860            |
| 2.0239   | 24.2731            | 3.7635   | 52.9288            |
| 2.0906   | 25.0652            | 3.8870   | 55.2211            |

Measured Heat Capacity  
Lutetium + 0.70 Atomic Percent Hydrogen  
 (continued)

| T<br>(K) | C<br>(mJ/g-atom K) | T<br>(K) | C<br>(mJ/g-atom K) |
|----------|--------------------|----------|--------------------|
| 3.9648   | 57.1980            | 9.7646   | 451.6155           |
| 4.0685   | 59.1737            | 10.1515  | 511.7022           |
| 4.3579   | 67.2187            | 10.4461  | 553.1026           |
| 4.6331   | 74.8358            | 10.8326  | 625.6755           |
| 4.8948   | 82.5808            | 11.2248  | 698.4560           |
| 5.1577   | 90.7525            | 11.6528  | 787.8069           |
| 5.4189   | 100.2875           | 12.0933  | 881.8433           |
| 5.6274   | 107.7838           | 12.4759  | 970.2828           |
| 5.8807   | 117.9019           | 12.9406  | 1090.1020          |
| 6.1585   | 130.6982           | 13.4019  | 1214.5812          |
| 6.4629   | 145.9055           | 14.0336  | 1399.6217          |
| 6.7732   | 163.5820           | 14.7237  | 1615.3874          |
| 7.0359   | 178.4499           | 15.2327  | 1796.6266          |
| 7.3638   | 200.5693           | 15.8501  | 2021.4081          |
| 7.6815   | 225.3473           | 16.4837  | 2224.8685          |
| 7.9951   | 251.0589           | 17.1127  | 2500.0995          |
| 8.3230   | 281.9474           | 17.7497  | 2760.7737          |
| 8.5764   | 303.0375           | 18.2832  | 2978.0827          |
| 8.9707   | 347.5881           | 18.9000  | 3259.0331          |
| 9.3660   | 396.9730           | 19.5911  | 3586.2214          |

Measured Heat Capacity  
Lutetium + 1.40 Atomic Percent Hydrogen  
 Sample 2-19

| T<br>(K) | C<br>(mJ/g-atom K) | T<br>(K) | C<br>(mJ/g-atom K) |
|----------|--------------------|----------|--------------------|
| 1.0901   | 13.0084            | 1.5819   | 19.2799            |
| 1.0952   | 13.2364            | 1.5895   | 19.8874            |
| 1.1573   | 13.9933            | 1.6557   | 20.4992            |
| 1.1686   | 13.8087            | 1.6618   | 20.6434            |
| 1.2229   | 14.9497            | 1.6993   | 20.8313            |
| 1.2410   | 15.0584            | 1.7297   | 21.3150            |
| 1.2840   | 15.5820            | 1.7522   | 21.7450            |
| 1.3065   | 15.8524            | 1.7849   | 22.2247            |
| 1.3431   | 16.2923            | 1.8408   | 22.8528            |
| 1.3712   | 16.5683            | 1.8880   | 23.3918            |
| 1.4069   | 17.0437            | 1.9516   | 24.3878            |
| 1.4214   | 17.3464            | 2.0054   | 25.1793            |
| 1.4517   | 17.8274            | 2.0702   | 26.0189            |
| 1.5020   | 18.3488            | 2.1056   | 26.3957            |
| 1.5224   | 18.6523            | 2.1221   | 27.2931            |

Measured Heat Capacity  
Lutetium + 1.40 Atomic Percent Hydrogen  
 (continued)

| T<br>(K) | C<br>(mJ/g-atom K) | T<br>(K) | C<br>(mJ/g-atom K) |
|----------|--------------------|----------|--------------------|
| 2.1790   | 27.6151            | 5.1221   | 92.5472            |
| 2.2450   | 28.4890            | 5.3774   | 101.9297           |
| 2.3114   | 29.4790            | 5.5775   | 109.2842           |
| 2.3764   | 30.4032            | 5.8323   | 119.8906           |
| 2.4329   | 31.3443            | 6.0787   | 131.0581           |
| 2.5006   | 32.3635            | 6.3498   | 144.1998           |
| 2.5515   | 33.1957            | 6.6491   | 160.3564           |
| 2.6185   | 34.2400            | 6.9129   | 176.5260           |
| 2.6643   | 34.8530            | 7.2426   | 196.6371           |
| 2.7008   | 35.4969            | 7.5521   | 218.9469           |
| 2.7305   | 35.8056            | 7.8586   | 244.0598           |
| 2.7345   | 35.9178            | 8.1743   | 267.2525           |
| 2.8218   | 37.3953            | 8.4148   | 290.5503           |
| 2.8865   | 38.5910            | 8.8027   | 329.8656           |
| 2.9520   | 39.8412            | 9.2074   | 380.0460           |
| 3.0346   | 41.3784            | 9.6027   | 428.5819           |
| 3.0860   | 42.0639            | 10.0110  | 487.2090           |
| 3.1754   | 43.9198            | 10.3329  | 536.0606           |
| 3.2273   | 44.7966            | 10.7429  | 608.2274           |
| 3.2664   | 45.6476            | 11.1444  | 679.5135           |
| 3.3121   | 46.1673            | 11.5531  | 764.2057           |
| 3.3588   | 47.4106            | 11.9845  | 854.7769           |
| 3.4383   | 48.9700            | 12.3638  | 936.2816           |
| 3.5389   | 50.9137            | 12.8342  | 1051.5264          |
| 3.6070   | 52.5617            | 13.3141  | 1187.4770          |
| 3.7206   | 54.8349            | 13.7930  | 1316.8758          |
| 3.7842   | 56.0966            | 14.8822  | 1649.9356          |
| 3.9193   | 59.2722            | 15.5297  | 1894.7723          |
| 3.9530   | 59.8771            | 16.1543  | 2112.8963          |
| 4.1073   | 63.8360            | 16.8381  | 2363.0769          |
| 4.1354   | 64.4634            | 17.5231  | 2639.3879          |
| 4.3532   | 70.5205            | 18.1423  | 2897.1545          |
| 4.6187   | 77.7195            | 18.7795  | 3186.0599          |
| 4.8698   | 84.8682            | 19.4100  | 3431.1448          |

Measured Heat Capacity  
Lutetium + 1.50 Atomic Percent Hydrogen  
Sample 2-10

| T<br>(K) | C<br>(mJ/g-atom K) | T<br>(K) | C<br>(mJ/g-atom K) |
|----------|--------------------|----------|--------------------|
| 1.0961   | 13.1298            | 2.9487   | 39.7872            |
| 1.1154   | 13.5525            | 3.0553   | 41.4720            |
| 1.1392   | 13.6673            | 3.0925   | 42.2686            |
| 1.1673   | 14.1042            | 3.1247   | 42.9193            |
| 1.1816   | 14.1951            | 3.2423   | 45.2315            |
| 1.2191   | 14.7140            | 3.3028   | 46.3131            |
| 1.2276   | 14.7326            | 3.3079   | 46.4737            |
| 1.2689   | 15.4715            | 3.4827   | 49.9666            |
| 1.2806   | 15.4489            | 3.4832   | 49.7837            |
| 1.3198   | 16.0294            | 3.6571   | 53.7909            |
| 1.3260   | 16.0357            | 3.6733   | 54.1512            |
| 1.3574   | 16.4358            | 3.8302   | 57.5661            |
| 1.3917   | 16.8046            | 3.8588   | 57.7791            |
| 1.4574   | 17.6192            | 4.0127   | 61.6120            |
| 1.4878   | 17.9936            | 4.0516   | 62.3153            |
| 1.5262   | 18.5323            | 4.1853   | 65.6206            |
| 1.5523   | 19.0181            | 4.3478   | 70.2446            |
| 1.5935   | 19.3793            | 4.6015   | 77.2047            |
| 1.6190   | 19.7718            | 4.8566   | 84.7572            |
| 1.6191   | 19.9159            | 5.1098   | 92.8905            |
| 1.6417   | 20.1924            | 5.3587   | 101.5633           |
| 1.7031   | 20.9159            | 5.5269   | 107.9654           |
| 1.7146   | 21.0804            | 5.7745   | 117.8465           |
| 1.8060   | 22.3207            | 6.0413   | 129.4854           |
| 1.8067   | 22.3933            | 6.3495   | 144.3879           |
| 1.9112   | 23.7985            | 6.6649   | 160.5496           |
| 1.9115   | 23.8128            | 6.9221   | 176.6505           |
| 1.9647   | 24.5207            | 7.2442   | 195.4909           |
| 1.9712   | 24.5508            | 7.5631   | 218.7160           |
| 2.0978   | 26.4194            | 7.8691   | 243.0012           |
| 2.1063   | 26.4926            | 8.1995   | 271.8059           |
| 2.2238   | 28.2236            | 8.4643   | 295.9962           |
| 2.2465   | 28.5461            | 8.8590   | 336.9183           |
| 2.3368   | 29.9552            | 9.2562   | 384.0213           |
| 2.3661   | 30.3231            | 9.6468   | 436.2392           |
| 2.4451   | 31.6012            | 10.0285  | 492.9541           |
| 2.4795   | 32.0645            | 10.2925  | 529.2455           |
| 2.4888   | 32.3120            | 10.6889  | 592.2818           |
| 2.6044   | 33.9939            | 11.0923  | 668.1601           |
| 2.6190   | 34.3063            | 11.5214  | 749.6642           |
| 2.6564   | 34.8408            | 11.9587  | 847.6547           |
| 2.7621   | 36.6439            | 12.3196  | 927.1016           |
| 2.8076   | 37.2790            | 12.7781  | 1036.6839          |
| 2.9081   | 38.9773            | 13.2478  | 1228.4814          |

Measured Heat Capacity  
Lutetium + 1.50 Atomic Percent Hydrogen  
 (continued)

| T<br>(K) | C<br>(mJ/g-atom K) | T<br>(K) | C<br>(mJ/g-atom K) |
|----------|--------------------|----------|--------------------|
| 13.7483  | 1303.4317          | 16.7864  | 2333.8818          |
| 14.3273  | 1478.1382          | 17.4315  | 2587.8052          |
| 14.8535  | 1639.5836          | 17.9711  | 2813.7917          |
| 15.5045  | 1858.9052          | 18.5886  | 3062.3888          |
| 16.1404  | 2088.0066          | 19.2869  | 3384.0960          |

Measured Heat Capacity  
Lutetium + 3.10 Atomic Percent Hydrogen  
 Sample 1-84

| T<br>(K) | C<br>(mJ/g-atom K) | T<br>(K) | C<br>(mJ/g-atom K) |
|----------|--------------------|----------|--------------------|
| 1.1188   | 12.1453            | 1.9645   | 22.4930            |
| 1.1666   | 12.5579            | 1.9681   | 22.5549            |
| 1.1787   | 12.5087            | 2.0382   | 23.5196            |
| 1.2148   | 13.2229            | 2.0819   | 24.0867            |
| 1.2244   | 13.2118            | 2.1513   | 25.0252            |
| 1.2663   | 13.7220            | 2.1936   | 25.4211            |
| 1.2744   | 13.7977            | 2.2663   | 26.6856            |
| 1.3151   | 14.4263            | 2.3066   | 27.3285            |
| 1.3236   | 14.3371            | 2.3587   | 28.0413            |
| 1.3517   | 14.6043            | 2.3815   | 28.3100            |
| 1.3696   | 14.9898            | 2.4057   | 28.7128            |
| 1.3967   | 15.4960            | 2.4258   | 29.1935            |
| 1.4047   | 16.5812            | 2.5378   | 30.6961            |
| 1.4423   | 15.2952            | 2.5647   | 31.1453            |
| 1.4549   | 16.0721            | 2.6679   | 32.7632            |
| 1.4937   | 16.3573            | 2.7107   | 33.5026            |
| 1.5066   | 16.5488            | 2.8070   | 34.9936            |
| 1.5445   | 17.0892            | 2.8485   | 35.8064            |
| 1.5631   | 17.3119            | 2.9509   | 37.6427            |
| 1.5733   | 17.4235            | 2.9519   | 37.2524            |
| 1.6238   | 18.0466            | 2.9823   | 38.2663            |
| 1.6319   | 18.0523            | 3.0477   | 39.2734            |
| 1.6608   | 18.5057            | 3.1133   | 40.4206            |
| 1.6969   | 19.0544            | 3.1941   | 42.0941            |
| 1.7219   | 19.4279            | 3.2781   | 43.6789            |
| 1.7748   | 20.0243            | 3.3748   | 45.6514            |
| 1.7817   | 20.1776            | 3.4463   | 47.1338            |
| 1.8419   | 20.7774            | 3.5769   | 49.7670            |
| 1.8962   | 21.5446            | 3.6070   | 50.3262            |
| 1.9235   | 22.0157            | 3.7289   | 53.2431            |

Measured Heat Capacity  
Lutetium + 3.10 Atomic Percent Hydrogen  
 (continued)

| T<br>(K) | C<br>(mJ/g-atom K) | T<br>(K) | C<br>(mJ/g-atom K) |
|----------|--------------------|----------|--------------------|
| 3.7728   | 53.8780            | 8.7310   | 316.5806           |
| 3.9140   | 57.2698            | 9.1164   | 358.1778           |
| 3.9581   | 58.5165            | 9.4946   | 403.4283           |
| 4.0932   | 61.5051            | 9.8035   | 446.0583           |
| 4.1607   | 62.9145            | 10.2069  | 502.9326           |
| 4.2669   | 65.7737            | 10.5974  | 565.4762           |
| 4.3273   | 67.6257            | 10.9690  | 628.5894           |
| 4.5646   | 74.0068            | 11.4918  | 731.6470           |
| 4.8058   | 80.9133            | 11.9188  | 814.8343           |
| 5.0428   | 88.2840            | 12.2653  | 891.9608           |
| 5.2845   | 96.6469            | 12.6557  | 984.9854           |
| 5.4602   | 102.7618           | 13.0382  | 1074.0033          |
| 5.7064   | 112.3801           | 13.4048  | 1169.0022          |
| 5.9417   | 122.6702           | 13.7193  | 1265.6868          |
| 6.1900   | 133.7794           | 14.2430  | 1417.5101          |
| 6.4628   | 147.8411           | 14.8363  | 1598.7787          |
| 6.6770   | 159.5502           | 15.3769  | 1778.3280          |
| 6.9740   | 176.4519           | 15.9435  | 1962.5976          |
| 7.2687   | 195.2421           | 16.3312  | 2104.4215          |
| 7.5612   | 216.1570           | 16.9172  | 2326.2456          |
| 7.8531   | 238.5679           | 17.5111  | 2549.6477          |
| 8.0727   | 255.1801           | 18.0966  | 2794.2793          |
| 8.3626   | 281.8929           | 18.7178  | 3057.4564          |

Measured Heat Capacity  
Lutetium + 6.10 Atomic Percent Hydrogen  
 Sample 2-5

| T<br>(K) | C<br>(mJ/g-atom K) | T<br>(K) | C<br>(mJ/g-atom K) |
|----------|--------------------|----------|--------------------|
| 1.1057   | 10.4384            | 1.4589   | 14.1784            |
| 1.1156   | 10.6088            | 1.4818   | 14.4057            |
| 1.1688   | 11.0526            | 1.5325   | 14.9992            |
| 1.1850   | 11.3866            | 1.5578   | 15.2454            |
| 1.2294   | 11.7434            | 1.6022   | 15.9118            |
| 1.2400   | 11.9062            | 1.6358   | 16.0752            |
| 1.2874   | 12.3436            | 1.6729   | 16.5914            |
| 1.2970   | 12.4425            | 1.6779   | 16.5502            |
| 1.3456   | 12.9562            | 1.7118   | 16.9464            |
| 1.3637   | 13.1494            | 1.7522   | 17.4943            |
| 1.3877   | 13.3725            | 1.7716   | 17.6750            |
| 1.4062   | 13.6044            | 1.8689   | 18.8619            |

Measured Heat Capacity  
Lutetium + 6.10 Atomic Percent Hydrogen  
 (continued)

| T<br>(K) | C<br>(mJ/g-atom K) | T<br>(K) | C<br>(mJ/g-atom K) |
|----------|--------------------|----------|--------------------|
| 1.8790   | 18.9395            | 4.6605   | 71.8981            |
| 1.9619   | 19.9816            | 4.9249   | 78.8882            |
| 1.9878   | 20.3083            | 5.1588   | 85.7513            |
| 2.0401   | 20.9155            | 5.4070   | 94.8605            |
| 2.0469   | 20.8686            | 5.6067   | 102.1120           |
| 2.0641   | 21.2421            | 5.8456   | 111.2062           |
| 2.1747   | 22.6684            | 6.1236   | 122.7489           |
| 2.2286   | 23.3079            | 6.4340   | 137.3802           |
| 2.3028   | 24.3362            | 6.7441   | 153.3105           |
| 2.3683   | 25.2249            | 6.9720   | 166.7091           |
| 2.4279   | 26.0469            | 7.2788   | 184.8560           |
| 2.4997   | 27.0354            | 7.5959   | 206.0940           |
| 2.5459   | 27.7698            | 7.9116   | 230.2106           |
| 2.6061   | 28.5331            | 8.2233   | 253.5092           |
| 2.6605   | 29.4704            | 8.4672   | 271.0243           |
| 2.6683   | 29.6357            | 8.8305   | 311.1184           |
| 2.6985   | 29.8909            | 9.2369   | 353.7633           |
| 2.7007   | 29.7914            | 9.6406   | 402.3085           |
| 2.7924   | 31.3799            | 10.0434  | 453.6578           |
| 2.8314   | 32.0410            | 10.3444  | 498.2740           |
| 2.9406   | 33.8778            | 10.7365  | 558.8818           |
| 2.9656   | 34.1834            | 11.1401  | 626.2098           |
| 3.0364   | 35.3652            | 11.5717  | 705.3067           |
| 3.0811   | 36.1977            | 12.0161  | 794.2266           |
| 3.1393   | 37.1945            | 12.3574  | 866.7663           |
| 3.2189   | 38.6583            | 12.8203  | 969.1008           |
| 3.3170   | 40.4473            | 13.2855  | 1086.5594          |
| 3.3879   | 41.6589            | 13.7553  | 1207.7122          |
| 3.4935   | 43.7592            | 14.2967  | 1357.3146          |
| 3.5718   | 45.2654            | 14.8677  | 1526.5920          |
| 3.6766   | 47.4713            | 15.5078  | 1737.4413          |
| 3.7492   | 49.0491            | 16.1563  | 1955.8671          |
| 3.8687   | 51.4723            | 16.8073  | 2181.7168          |
| 3.9248   | 52.7785            | 17.4529  | 2419.6495          |
| 4.0542   | 55.6092            | 17.9559  | 2628.9615          |
| 4.1054   | 56.6494            | 18.5408  | 2837.7215          |
| 4.3707   | 63.7208            | 19.1761  | 3116.7235          |

Measured Heat Capacity  
Lutetium + 11.0 Atomic Percent Hydrogen  
Sample 1-98

| T<br>(K) | C<br>(mJ/g-atom K) | T<br>(K) | C<br>(mJ/g-atom K) |
|----------|--------------------|----------|--------------------|
| 1.0920   | 9.0732             | 2.8883   | 28.7509            |
| 1.1068   | 9.0867             | 2.9448   | 29.6955            |
| 1.1546   | 9.5620             | 3.0424   | 30.9343            |
| 1.2109   | 10.0676            | 3.0840   | 31.5474            |
| 1.2271   | 10.2415            | 3.0868   | 31.6316            |
| 1.2624   | 10.4927            | 3.2263   | 33.7925            |
| 1.2862   | 10.7936            | 3.2495   | 34.2853            |
| 1.2984   | 10.7716            | 3.2616   | 34.2369            |
| 1.3446   | 11.2197            | 3.4161   | 37.0852            |
| 1.3487   | 11.2466            | 3.4640   | 37.8920            |
| 1.3854   | 11.6494            | 3.5898   | 40.0684            |
| 1.3999   | 11.7793            | 3.6770   | 41.5896            |
| 1.4543   | 12.2752            | 3.7816   | 43.6243            |
| 1.4569   | 12.2317            | 3.8689   | 45.2516            |
| 1.5154   | 12.7921            | 3.9810   | 47.4435            |
| 1.5322   | 12.8870            | 4.0530   | 48.8683            |
| 1.5359   | 13.0313            | 4.1723   | 51.5041            |
| 1.6023   | 13.6414            | 4.3338   | 55.3776            |
| 1.6025   | 13.6780            | 4.5972   | 61.6646            |
| 1.6689   | 14.2488            | 4.8584   | 68.2285            |
| 1.6765   | 14.2835            | 5.1164   | 75.2711            |
| 1.6975   | 14.3833            | 5.3610   | 82.4852            |
| 1.7236   | 14.8873            | 5.5574   | 88.9925            |
| 1.7831   | 15.4847            | 5.8038   | 97.7215            |
| 1.7903   | 15.4866            | 6.0719   | 107.6597           |
| 1.8231   | 15.9119            | 6.3779   | 120.4091           |
| 1.9026   | 16.7494            | 6.6918   | 134.5856           |
| 1.9352   | 16.9889            | 6.9504   | 147.6813           |
| 2.0173   | 17.9610            | 7.2731   | 174.7562           |
| 2.0527   | 18.3583            | 7.5995   | 183.9374           |
| 2.0668   | 18.5207            | 7.9121   | 205.0584           |
| 2.1823   | 19.7764            | 8.2408   | 230.0620           |
| 2.1961   | 19.9352            | 8.5061   | 249.8019           |
| 2.2928   | 21.0679            | 8.8911   | 283.5202           |
| 2.3238   | 21.3752            | 9.2829   | 323.2748           |
| 2.3311   | 21.4397            | 9.6775   | 364.4295           |
| 2.4452   | 22.8701            | 10.0681  | 412.3233           |
| 2.4498   | 22.9641            | 10.7575  | 506.6493           |
| 2.5549   | 24.3699            | 11.1621  | 568.9113           |
| 2.5848   | 24.7527            | 11.5653  | 632.8378           |
| 2.6539   | 25.6435            | 11.9937  | 713.8796           |
| 2.6645   | 25.7438            | 12.3544  | 780.7615           |
| 2.7376   | 26.5777            | 12.8146  | 871.1417           |
| 2.7996   | 27.5976            | 13.2754  | 977.3115           |

Measured Heat Capacity  
Lutetium + 11.0 Atomic Percent Hydrogen  
 (continued)

| T<br>(K) | C<br>(mJ/g-atom K) | T<br>(K) | C<br>(mJ/g-atom K) |
|----------|--------------------|----------|--------------------|
| 13.7786  | 1095.2243          | 16.8697  | 2001.5180          |
| 14.3530  | 1245.9496          | 17.5115  | 2215.6814          |
| 14.9251  | 1395.9238          | 18.0998  | 2447.1949          |
| 15.5904  | 1598.5585          | 18.6673  | 2628.7144          |
| 16.2293  | 1796.0810          | 19.2897  | 2888.8237          |

Measured Heat Capacity  
Lutetium + 15.5 Atomic Percent Hydrogen  
 Sample 2-4

| T<br>(K) | C<br>(mJ/g-atom K) | T<br>(K) | C<br>(mJ/g-atom K) |
|----------|--------------------|----------|--------------------|
| 1.0880   | 7.9696             | 2.1458   | 17.1293            |
| 1.1023   | 8.1038             | 2.2289   | 17.9941            |
| 1.1542   | 8.4669             | 2.2847   | 18.6255            |
| 1.1735   | 8.6281             | 2.3558   | 19.2975            |
| 1.2186   | 8.9135             | 2.4114   | 18.7039            |
| 1.2347   | 9.0712             | 2.4736   | 20.6203            |
| 1.2786   | 9.3979             | 2.5351   | 21.3169            |
| 1.2962   | 9.5568             | 2.5884   | 21.9813            |
| 1.3389   | 9.8756             | 2.5889   | 21.9080            |
| 1.3599   | 10.0682            | 2.6518   | 22.6507            |
| 1.3837   | 10.2722            | 2.6633   | 22.7221            |
| 1.4060   | 10.4427            | 2.7085   | 23.2271            |
| 1.4562   | 10.8505            | 2.8044   | 24.5035            |
| 1.4848   | 11.1052            | 2.8415   | 24.9348            |
| 1.5302   | 11.4665            | 2.9535   | 26.3445            |
| 1.5556   | 11.6928            | 2.9890   | 26.8344            |
| 1.6021   | 12.0661            | 3.0866   | 28.2132            |
| 1.6233   | 12.2444            | 3.1331   | 28.7399            |
| 1.6725   | 12.6734            | 3.2022   | 29.6771            |
| 1.6903   | 12.8401            | 3.2197   | 30.0156            |
| 1.6897   | 12.8500            | 3.2889   | 30.9887            |
| 1.7151   | 13.0364            | 3.3712   | 32.3562            |
| 1.7955   | 13.8136            | 3.3780   | 32.3193            |
| 1.8292   | 14.1365            | 3.5420   | 34.6569            |
| 1.9026   | 14.8292            | 3.5552   | 34.8343            |
| 1.9474   | 15.1897            | 3.6923   | 37.1713            |
| 1.9951   | 15.7067            | 3.7213   | 37.6474            |
| 2.0070   | 15.8121            | 3.8541   | 39.9841            |
| 2.0528   | 16.2165            | 3.9164   | 41.2045            |
| 2.0960   | 16.6271            | 4.0458   | 43.4865            |

Measured Heat Capacity  
Lutetium + 15.5 Atomic Percent Hydrogen  
 (continued)

| T<br>(K) | C<br>(mJ/g-atom K) | T<br>(K) | C<br>(mJ/g-atom K) |
|----------|--------------------|----------|--------------------|
| 4.0965   | 44.2958            | 9.7330   | 333.9086           |
| 4.2805   | 47.8522            | 10.1283  | 375.4281           |
| 4.3446   | 49.6138            | 10.4365  | 413.6743           |
| 4.6108   | 55.3756            | 10.8880  | 473.6622           |
| 4.8751   | 61.2794            | 11.3391  | 539.8764           |
| 5.1363   | 67.8177            | 11.7544  | 604.0990           |
| 5.3876   | 74.6162            | 12.1782  | 675.6639           |
| 5.5918   | 80.3315            | 12.5240  | 735.6055           |
| 5.8479   | 88.7944            | 12.9790  | 829.2976           |
| 6.1208   | 98.2335            | 13.4322  | 923.4213           |
| 6.4297   | 109.7796           | 13.9275  | 1038.7161          |
| 6.7508   | 123.0025           | 14.4889  | 1163.0554          |
| 6.9958   | 134.0584           | 15.0184  | 958.8996           |
| 7.3216   | 150.1526           | 15.6328  | 1468.5807          |
| 7.6433   | 167.7903           | 16.2517  | 1651.2611          |
| 7.9604   | 187.2083           | 16.8765  | 1847.1373          |
| 8.2847   | 208.5816           | 17.5171  | 2051.7251          |
| 8.5501   | 228.0126           | 18.1063  | 2247.7220          |
| 8.9412   | 259.2574           | 18.7210  | 2464.4783          |
| 9.3405   | 295.0273           | 19.4160  | 2701.0014          |

Measured Heat Capacity  
Lutetium + 67.0 Atomic Percent Hydrogen  
 Sample 2-8

| T<br>(K) | C<br>(mJ/g-atom K) | T<br>(K) | C<br>(mJ/g-atom K) |
|----------|--------------------|----------|--------------------|
| 1.1153   | 0.8531             | 1.8455   | 1.5954             |
| 1.1480   | 0.9093             | 1.9403   | 1.7003             |
| 1.1827   | 1.0171             | 2.0273   | 1.8191             |
| 1.2290   | 0.9875             | 2.0936   | 1.9154             |
| 1.2508   | 0.9678             | 2.1295   | 1.9464             |
| 1.3066   | 1.0052             | 2.2655   | 2.0387             |
| 1.3518   | 1.0936             | 2.4163   | 2.3196             |
| 1.3645   | 1.0790             | 2.5513   | 2.4974             |
| 1.4175   | 1.1484             | 2.6750   | 2.7222             |
| 1.4330   | 1.1660             | 2.6778   | 2.6469             |
| 1.5026   | 1.2237             | 2.8622   | 2.9847             |
| 1.5790   | 1.3201             | 3.0316   | 3.3132             |
| 1.6669   | 1.4128             | 3.1681   | 3.5669             |
| 1.7372   | 1.4708             | 3.3074   | 3.8680             |
| 1.7533   | 1.5168             | 3.3243   | 3.9602             |

Measured Heat Capacity  
Lutetium + 67.0 Atomic Percent Hydrogen  
 (continued)

| T<br>(K) | C<br>(mJ/g-atom K) | T<br>(K) | C<br>(mJ/g-atom K) |
|----------|--------------------|----------|--------------------|
| 3.5505   | 4.4045             | 8.5907   | 33.7956            |
| 3.7680   | 4.9396             | 8.9015   | 37.1845            |
| 3.9702   | 5.4081             | 9.2268   | 41.1454            |
| 4.1940   | 6.1047             | 9.5878   | 47.3592            |
| 4.4137   | 6.8964             | 9.9862   | 52.6945            |
| 4.7564   | 7.8813             | 10.2607  | 56.9830            |
| 5.0596   | 8.9315             | 10.6836  | 65.7188            |
| 5.3351   | 10.0151            | 11.1038  | 72.3978            |
| 5.5793   | 11.2213            | 11.5269  | 80.5181            |
| 5.7435   | 11.8951            | 11.9306  | 85.5072            |
| 6.0090   | 13.2977            | 12.3090  | 94.2698            |
| 6.2652   | 14.7388            | 12.7821  | 114.5602           |
| 6.5128   | 16.2775            | 13.2338  | 128.0562           |
| 6.7893   | 17.8551            | 13.6713  | 146.0138           |
| 7.0401   | 19.9706            | 14.1705  | 162.6746           |
| 7.3709   | 21.8818            | 14.7449  | 193.8809           |
| 7.7064   | 24.8228            | 16.0081  | 246.0936           |
| 8.0444   | 27.6178            | 16.8010  | 294.2017           |
| 8.3797   | 31.3384            | 17.6074  | 336.3975           |

Measured Heat Capacity  
Calorimetry Conference Standard Copper Sample

| T<br>(K) | C<br>(mJ/g-atom K) | T<br>(K) | C<br>(mJ/g-atom K) |
|----------|--------------------|----------|--------------------|
| 1.2910   | 0.9719             | 2.4671   | 2.4034             |
| 1.3352   | 1.0696             | 2.6041   | 2.6113             |
| 1.3761   | 1.1031             | 2.7199   | 2.8392             |
| 1.3943   | 1.1070             | 2.8734   | 3.0923             |
| 1.4849   | 1.1868             | 2.9047   | 3.1869             |
| 1.5266   | 1.2463             | 3.0831   | 3.5430             |
| 1.5633   | 1.2795             | 3.3443   | 4.1232             |
| 1.6126   | 1.3257             | 3.6597   | 4.9286             |
| 1.7201   | 1.4206             | 4.0004   | 5.8828             |
| 1.8219   | 1.5331             | 4.2905   | 6.7860             |
| 1.9132   | 1.6617             | 4.4738   | 7.5054             |
| 1.9931   | 1.7237             | 4.6764   | 8.2743             |
| 2.1226   | 1.9217             | 4.8947   | 9.1481             |
| 2.2905   | 2.1559             | 5.0974   | 9.9359             |
| 2.3118   | 2.1789             |          |                    |