Application of

Monte Carlo criticality calculations

to the Ames Laboratory Research Reactor

by

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TABLE OF CONTENTS

LIST OF ILLUSTRATIONS

LIST OF TABLES

I. INTRODUCTION

Buffon (1707-1788) (1), is considered by some people to have introduced the first Monte Carlo calculation, the needle problem, which consisted of throwing a needle at random on a surface marked with parallel lines spaced two needle lengths apart. The total throws divided by the number of times the needle hits a line approaches pi as the number of trials is increased. Since that time, man's ingenuity and fast computers have made the Monte Carlo method a useful tool in neutron transport problems.

In early attempts to use Monte Carlo methods for reactor calculations, the limited memory capacity of computers was the cause of its demise. It was not practical to handle the large volume of cross section data needed and also, point cross-section data were not readily available. With the development of large memory fast computers and adequate cross-section libraries, the Monte Carlo method has become an important analysis technique. The three dimension capability has made the Monte Carlo calculation one of the most exact at the present time. Computer time appears to be a limiting factor since a Monte Carlo result is exactly correct only when an infinite number of independent estimates of a given result have been obtained.

The majority of the existing diffusion and transport codes are limited by the following three items. First, the

codes are, at best, only two dimensions which means approximations must be made. Secondly, the codes are usually based upon the assumption that an equilibrium distribution of neutrons is present at the start of an analysis, which makes the study of time-dependent situations rather difficult. Thirdly, most codes are capable of handling only few group cross sections. The Monte Carlo procedure is equivalent to obtaining an exact solution of the Boltzman transport equation. In theory, the Monte Carlo method eliminates the deficiencies of other systems mentioned above. In reality, the Monte Carlo system is still limited by computer storage and statistics. As a result of the latter, a balance must be achieved between statistics and computer costs.

This thesis describes how the Ames Laboratory Research Reactor (ALRR) core region was modeled and the input required to be able to utilize the Monte Carlo computer code KENO (2) for criticality calculations. Reactivity calculations in terms of k-effective (k-eff) were made for various reactor configurations and compared to measurements made on the actual reactor.

II. REVIEW OF LITERATURE

In 1957 Kalos and Wilf (3) reporting on the uses of Monte Carlo calculations in solving reactor problems, state that they may eventually be used for complete reactivity calculations. Since that time, considerable work has been done to make the Monte Carlo method feasible for multigroup criticality analysis.

Rief and Kschwendt (4) have shown that detailed Monte Carlo analysis for fast reactor studies can be carried out with sufficient accuracy to be comparable with equivalent S_n and j_n calculations. Mendelson (5) reports using the O5R Monte Carlo computer code (6) to investigate the ability to compute the criticality of thermal reactors by analyzing three simple critical assemblies. The results of these analyses show that a precision of 0.5% to 0.8% in the eigenvalue is obtainable. The majority of Monte Carlo work has been in computing the criticality of fast assemblies, while the application to thermal systems has been somewhat limited. Woodcock, et al. (7), have developed the GEM Code (8) which has been used for Monte Carlo neutronics calculations in reactors. The O5R code and the GEM code are the forefathers of the KENO code used in this analysis.

At the present time, the KENO code is the main code used in industry for performing criticality analyses involving safety questions on fresh fuel storage, spent fuel storage

and safety analyses of batch fuel processes. Its application
to a criticality analysis of a thermal reactor is, perhaps,
stretching its capabilities; but it yields a tool that can be
used to obtain reactivity worths of various core changes with
the control rods included in the calculations. Previous
analyses of the ALRR core by J. C. Crudele (9) using the
diffusion code, EXTERMINATOR-2 (10), was limited to R-Theta
geometry with the control rods fully withdrawn. Many calcu-
lations that can be made are affected by the location of
strong absorbers such as the control rods. The KENO code can
handle strong absorbers which gives it an extreme advantage
over the diffusion code.

III. DESCRIPTION OF ALRR

The ALRR Hazards Report (11) describes the reactor as a
heterogeneous arrangement of highly enriched uranium-aluminum
fuel assemblies using aluminum as a structural material and
heavy water as moderator, reflector and main coolant. Figure
1 shows a cutaway view of the reactor. The area of interest
for this report is the center-most portion of this view, that
is, the region having sides and bottom defined by the thermal
shield vessel and top defined by the bottom of the lower top
shield plug. Major items in this region are the thermal
shield vessel, H_2O reflector, the D_2O vessel, the D_2O
moderator, experimental facilities, control rods, fuel
assemblies and aluminum structural material.

The major vessel is the D_2O vessel. It is a cylindrical
vessel having a wall thickness of approximately 0.5 inches.
It is 6 feet high with a diameter of 5 feet. The reactor
core is located in the center of this vessel and is in the
form of a right circular cylinder approximately 24 inches
high and 32 inches in diameter. This provides a D_2O
reflector region in the vessel of approximately 15 inches on
the sides, 30 inches on the top and 18 inches beneath the
core region. The core region is composed of twenty-four fuel
assemblies and six control rods plus additional D_2O
moderator. The fuel assemblies are arranged in three
concentric circles, six assemblies on a 5.25 inch radius, six
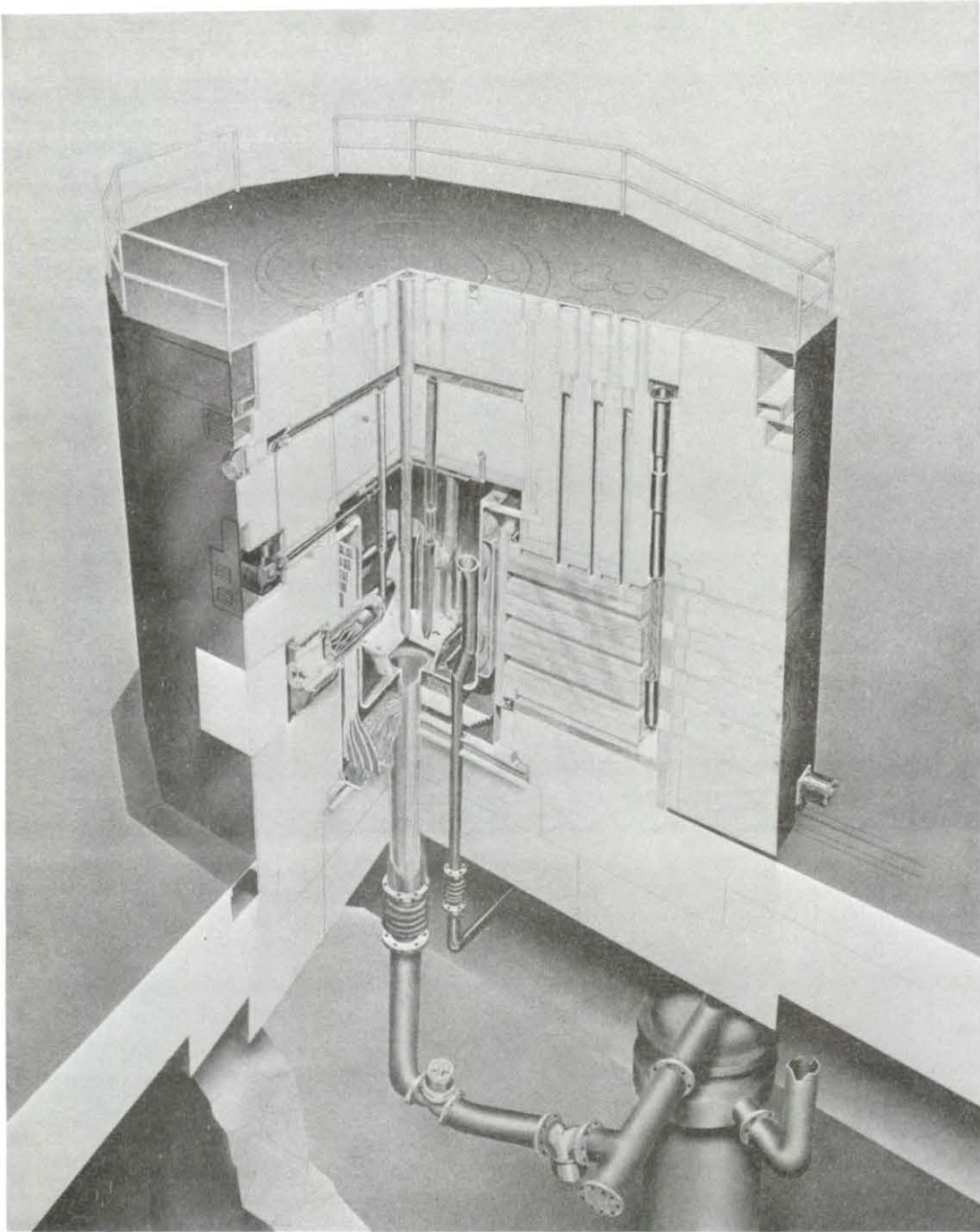
Figure   1.   Cut away view of ALRR

assemblies on a 10.5 inch radius and the remaining twelve
assemblies are located on a 13.89 inch radius. The control
rods also form a circle with their centers on a 9.09 inch ra-
dius. The fuel assembly itself is composed of seventeen
curved plates. Fifteen of these are fuel bearing plates made
up of a layer of uranium-aluminum alloy, clad on each side
with a layer of aluminum, each of the three layers being
0.020 inches thick. The remaining two plates are composed of
aluminum only and serve as side plates. These seventeen
plates are held together by two end plates. This arrangement
forms a 3 inch square box and allows .110 inches between
plates. There are approximately 11.33 grams of U235 per
plate resulting in an average of 170 grams U235 per assembly.
The active fuel length is 23.5 inches. The total length of
the completed fuel assembly, including hold-down extension
bar and transition nozzle is approximately 52.5 inches.
Figure 2 shows a cross-section and a vertical section of a
fuel assembly.

The control rod which is shown in Figure 3 has a 28 inch
length of travel from its full in position to 100% withdrawn.
The poison section is composed of a cadmium cylinder which
has an internal radius of 1.37 inches and a cadmium thickness
of 0.060 inches and a length of 19.87 inches. The cadmium is
encased in stainless steel 20.5 inches long and .065 inches
thick which results in an OR of 1.5 inches and an IR of 1.31

52.45 ± .045 REF

29.25 REF

24.63 P.W/23.5 FUEL ZONE

.875

.110 ± .010

3.010 SQ
2.990
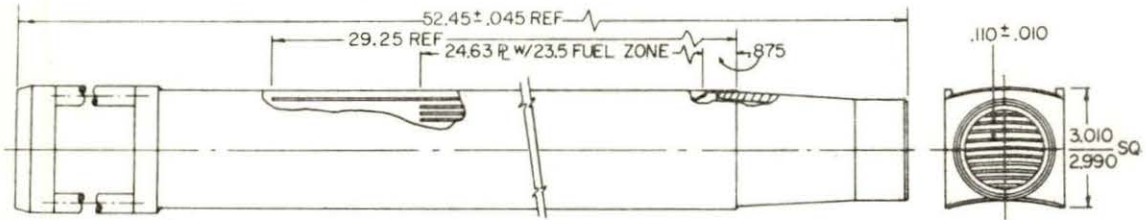
FUEL ELEMENT ASSY

INSCRIBE SERIAL NUMBER HERE
1/8" HIGH MAXIMUM

2.811
CORD
LENGTH

9
16

23.5 ± 1/4 FUEL ZONE

24.63
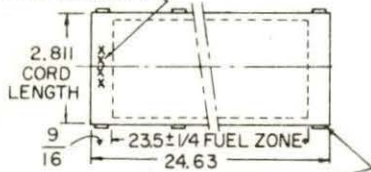
BREAK ALL SHARP
EDGES .015R

.175 MIN. TYP

.060 ± .001

.070 REF

2.40
ARC
LENGTH

29° 30'

5.50R

SEE DETAIL "C"

.020 TYP. CLAD

DETAIL "C"
ENLARGED

.020 FUEL
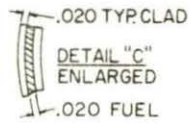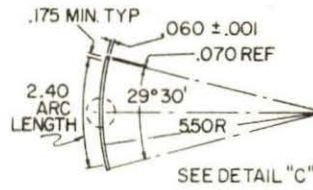
FUEL ELEMENT PLATE DETAIL

Figure   2.   ALRR fuel assembly

A = 1.5
B = 1.435
C = 1.375
D = 1.31
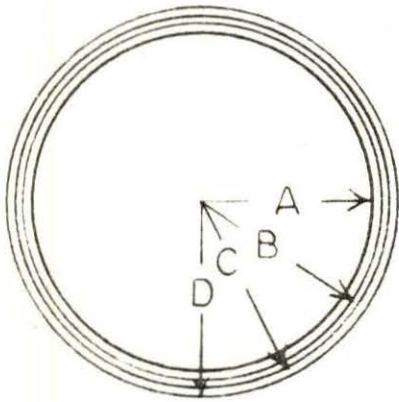
TOP VIEW

DIMENSIONS IN INCHES
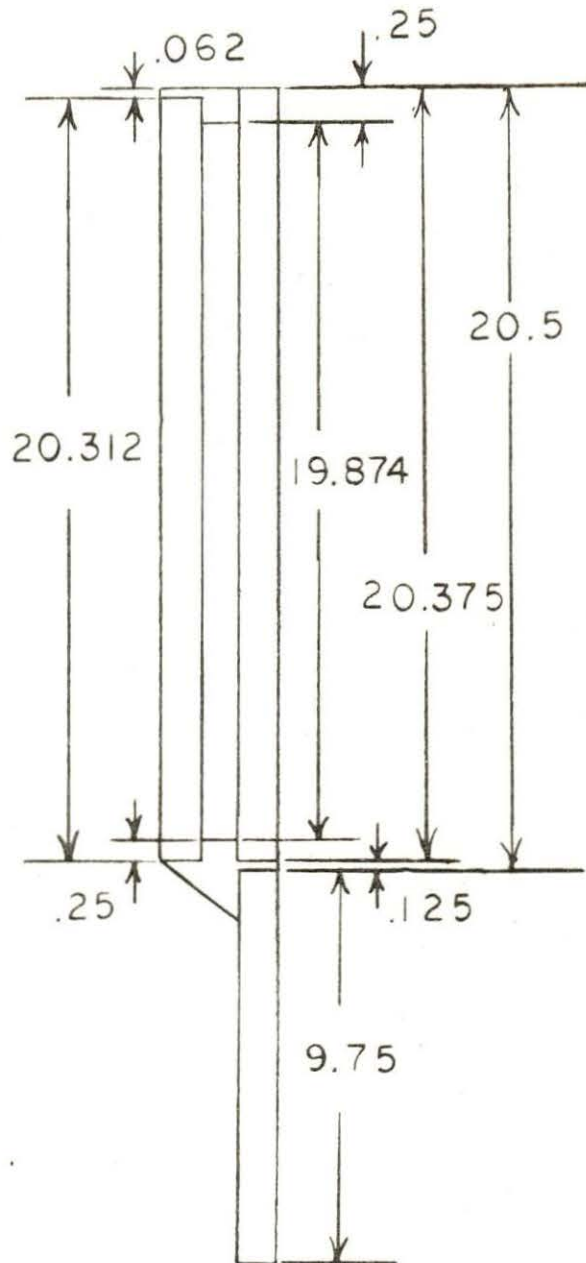
Figure   3.   ALRR control rod poison section

inches. At the bottom of the poison section is a stainless
steel follower which is .065 inches thick, 9.75 inches long
and has an OR of 1.50 inches. These rods have an armature
attached to the poison section and by manipulating a rack and
pinion magnet drive, the magnet can be lowered onto the
armature and by energizing the magnet, the control section
can be withdrawn from the core. By de-energizing the magnet,
the poison section will free fall into the core.

The major structural components located in the D_2O
vessel are the upper and lower grid plate, fuel assembly
guide tube, fuel assembly hold down plug, D_2O return tubes,
D_2O overflow tube, control rod guide tubes, and D_2O dump
tube. Also located in the D_2O vessel are six vertical
irradiation facilities, nine horizontal irradiation facili-
ties and two rabbit tubes along with two grazing tubes that
also pass through the vessel. There are additional facili-
ties but they are not considered large enough to cause sig-
nificant voids in the reflector or moderator.

The D_2O vessel is enclosed by the thermal shield vessel
which is an aluminum tank, 8 feet in diameter. This provides
an 18 inch annulus between vessels, which is composed of H_2O
and six 1 inch stainless steel plates. This system provides
the final protection for the biological shield. The thermal
shield does not encircle the D_2O vessel completely. A small
portion of this outer reflector is penetrated by the thermal

column.   Figure 4 shows a horizontal cross section of the

reactor and the relationship between the major components.
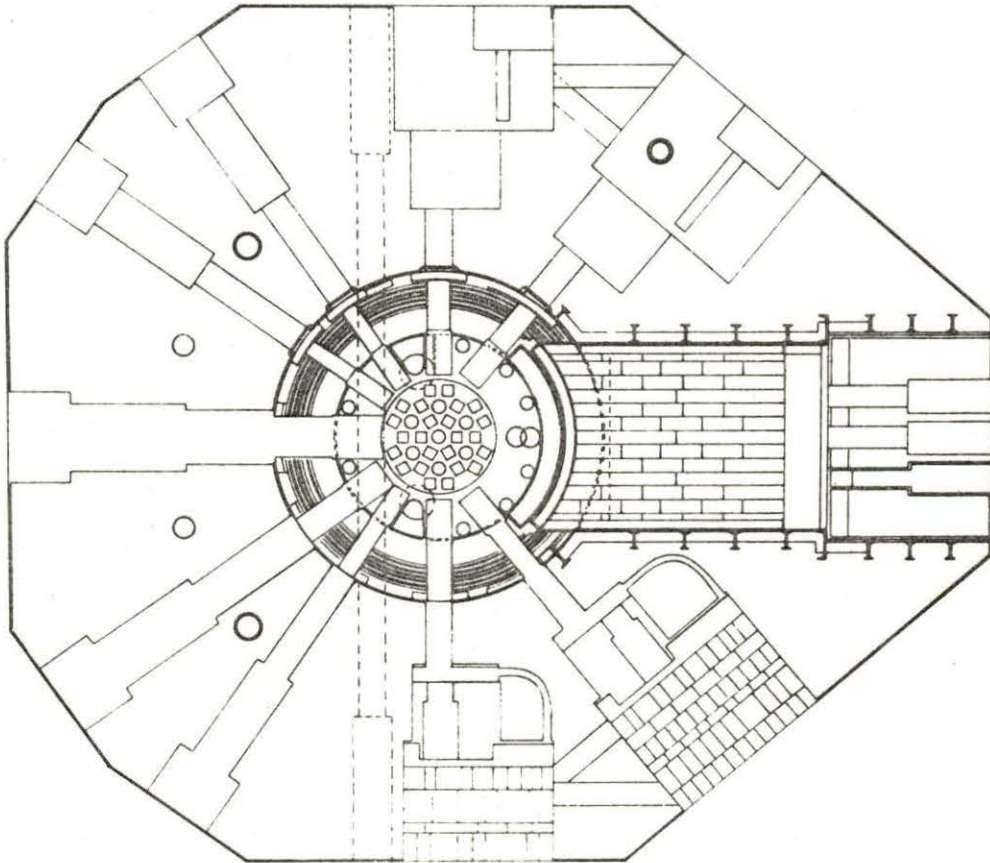
Figure   4.   Horizontal cross section of ALRR

IV. METHOD OF ANALYSIS

A. Introduction to KENO

The development of KENO, a multigroup Monte Carlo criticality program, resulted from the need to calculate the criticality condition of a proposed prompt-burst reactor design of cylindrical geometry. It was not considered realistic to homogenize the system in order to reduce the geometry to two dimensions for calculational purposes. Consequently, a three dimensional criticality code was required. The existing Monte Carlo codes GEM and 05R were considered, but were not deemed adequate for various reasons.

In the case of the 05R program, the lack of adequately checked point-set cross sections for a number of materials was one of the reasons for not using it, but it was noted that at one point in its history, the 05R program had been used with six-energy-group Hansen-Roach (12) neutron cross sections for uranium. This led to modifying the 05R code to use the existing sixteen-energy-group Hansen-Roach (12) cross sections that were available for a number of nuclei. This combination yielded results which were in excellent agreement with experimental data. The 05R code was further modified to allow easier geometry description of complex units and arrays of units. The geometry package developed to achieve this was patterned after the geometry package of the GEM Monte Carlo program. The resulting package, KENO, was a very rapid pro-

gram which could accurately determine the criticality condi-
tion of systems of fissile materials.

In order to determine the critical condition of a
fissile system, KENO determines k-effective where k-eff is
defined by the following expression:

$$k\text{-eff} = \sum_{j=1}^{NPB} \sum_{i=1}^{NCOLL} WT_{ij} \frac{\gamma\Sigma_f}{\Sigma_t} / \sum_{j=1}^{NPB} WT_{oj}$$

NPB is the number of neutrons per batch

NCOLL is the number of collisions for each neutron

WT_{ij} is the statistical weight of the jth neutron
at the ith collision

γ is the average number of neutrons born per
fission

Σ_f is the macroscopic fission cross section

The method used to accomplish this calculation is summarized
in the KENO program manual CTC-5 (2).

B. Modeled Core

The KENO program allows easy description of three-
dimensional systems composed of cylinders, spheres and
cuboids (rectangular parallelpipeds) in any order with only
one restriction: each geometrical region must be described
as completely enclosing all regions interior to it. In

conjunction with this, boundaries of the surfaces of regions may be shared but they must not intersect. This implies that the entire volume between two sequential geometrical surfaces contains only one mixture. If multiple units are combined to form an array, as in the case of describing the complete core, then the outer surface of each unit must be a cube or cuboid. If the total array is surrounded with a reflector region, an initial cube or cuboid must be described which exactly encloses all units in the array. The reflector region is then described relative to this core boundary.

The ALRR core was modeled in such a fashion that the original triangular pitch configuration shown in Figure 5 was converted to the x, y array shown in Figure 6. This was done by rotating sixteen of the twenty-four fuel assemblies, 30 degrees, about their centers. This results in eight columns of fuel assemblies all aligned with the same x, y orientation and three columns of control rods. These columns overlapped some of the fuel assembly columns in the x direction but not in the y direction. The next step was to expand the x, y grid system in the y direction until none of the columns of fuel assemblies or control rods overlapped, since the rules prohibit the intersection of boundaries. The amount of displacement of the columns ranged from .37 inches to 1.94 inches. Due to the angular arrangement of the assemblies prior to their rotation, the displacement of the
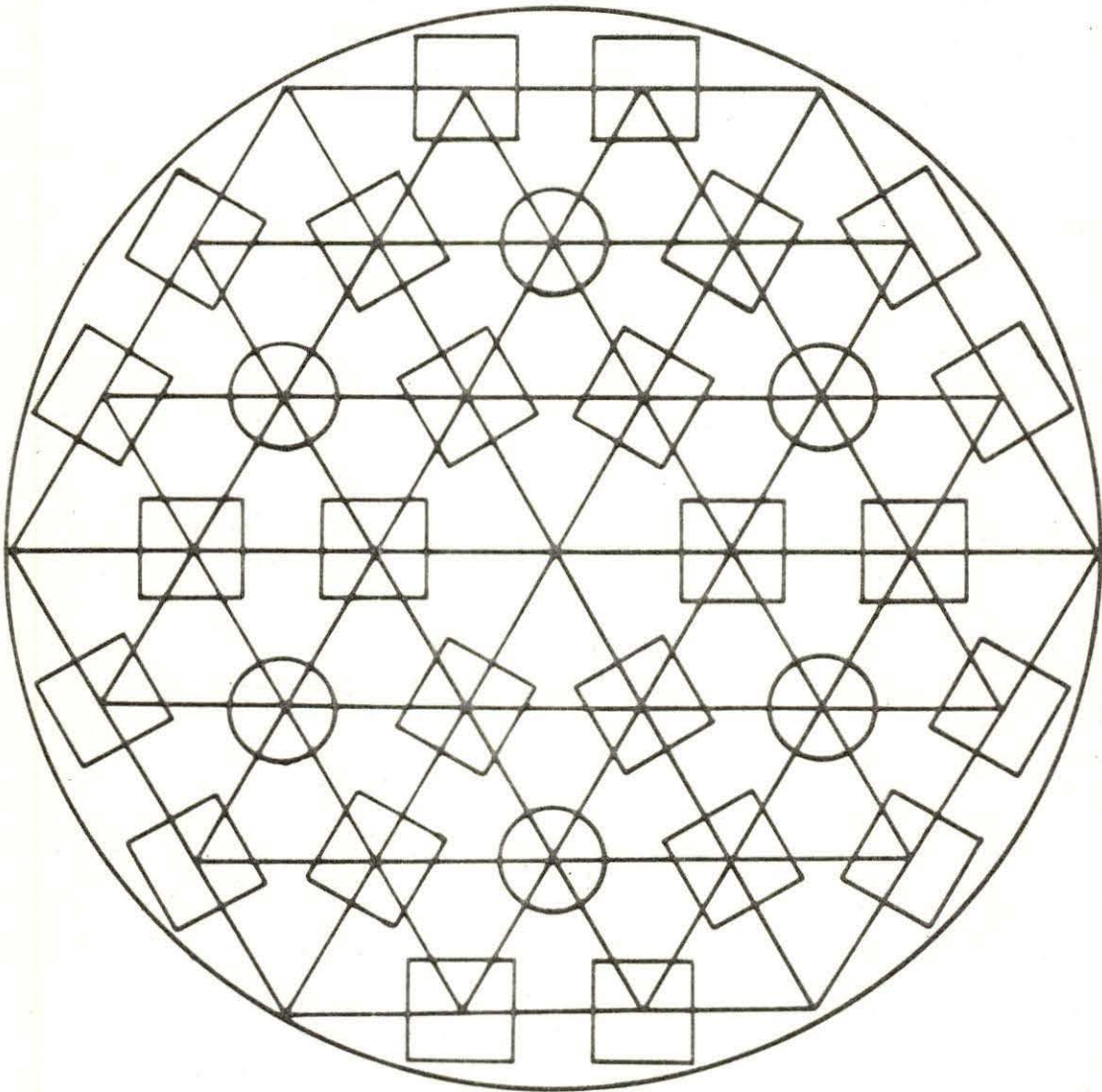
Figure 5. ALRR core configuration - triangular pitch
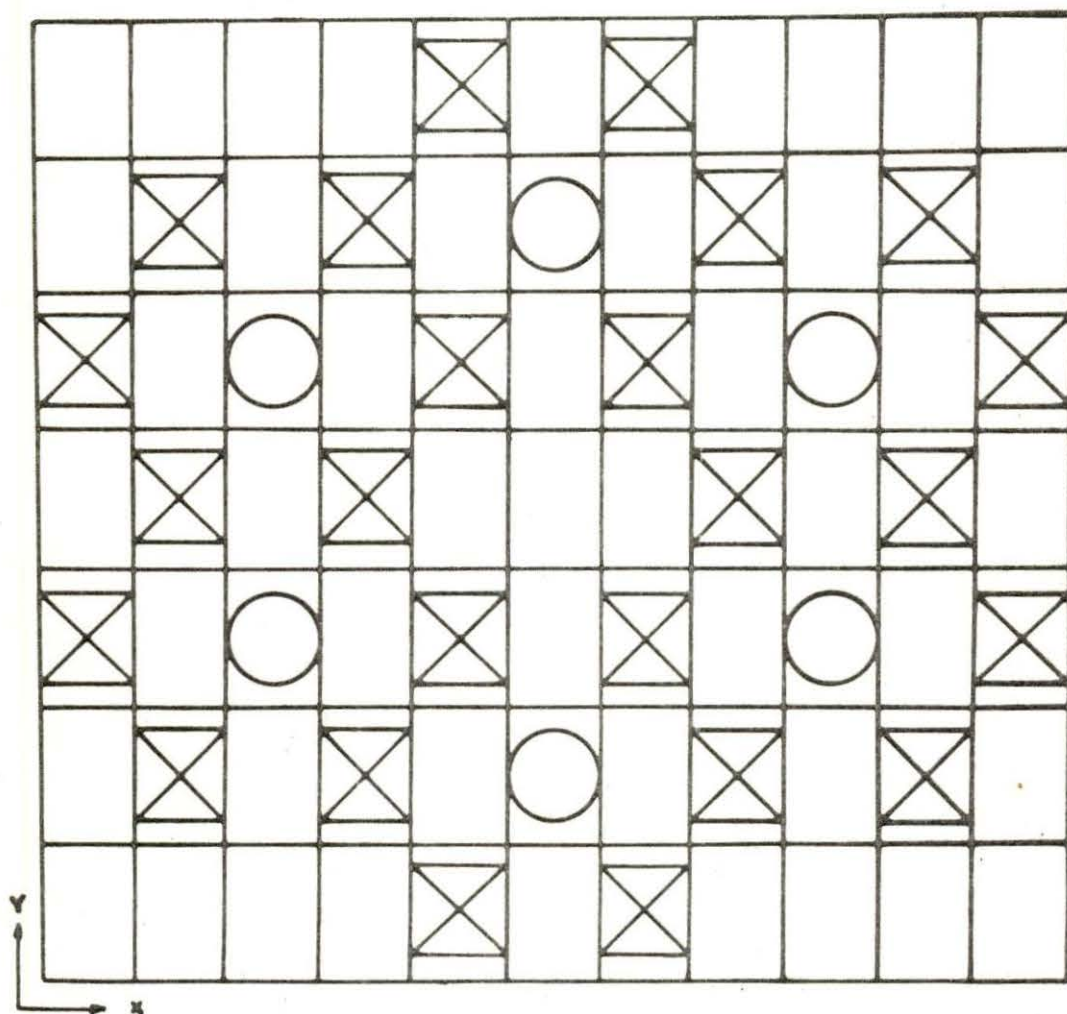
Figure   6.   Modeled core configuration

columns resulted in a core boundary of 33 inches by 31.5
inches instead of a 32 inch diameter circle. The x, y grid
is formed by boxes 3 inches by 4.5 inches in the form of an
11 by 7 array as shown in Figure 6. The height of this x, y
array is approximately 62 inches and is divided into six
zones. The height of the individual zones is a variable but
all box heights are equal within a particular zone. The
zones are used to terminate a particular box so that the geo-
metric arrangement is constant in the z direction. For exam-
ple: the control rod is composed of a poison section and a
dashpot section, the normal transition point being the inter-
section of these pieces. It is not permissible to describe
the complete control rod in a single box due to the change in
material in the z direction.

For the case where the control rods are 40% withdrawn,
the six zones are divided as follows and are shown in Figure
7. Starting at the top of the plenum, the first zone is up
to the base of the meat in the fuel plate of a fuel assembly.
This level is composed of boxes 3 x 4.5 x 6.38 inches high
and the mixture included is homogenized D_2O and aluminum.
The second zone is composed of boxes containing moderator
only and boxes containing a portion of a fuel assembly plus
moderator. These boxes have a height of 8.2 inches. The
third zone contains boxes which describe a fuel assembly sec-
tion, control rod follower and moderator. The height of this

TOP OF CORE TANK

ZONE 6

16.80

CONTROL ROD POISON

5

14.95

20.5

4

5.55

3

FUEL ASSEMBLY

CONTROL ROD FOLLOWER

23.5

9.75

2

8.20

1

TOP OF GRID PLATE

6.38

DIMENSIONS IN INCHES

33.0

MIXTURE 8 IN ZONES 1,5,6
MIXTURE 10 IN ZONES 2,3,4
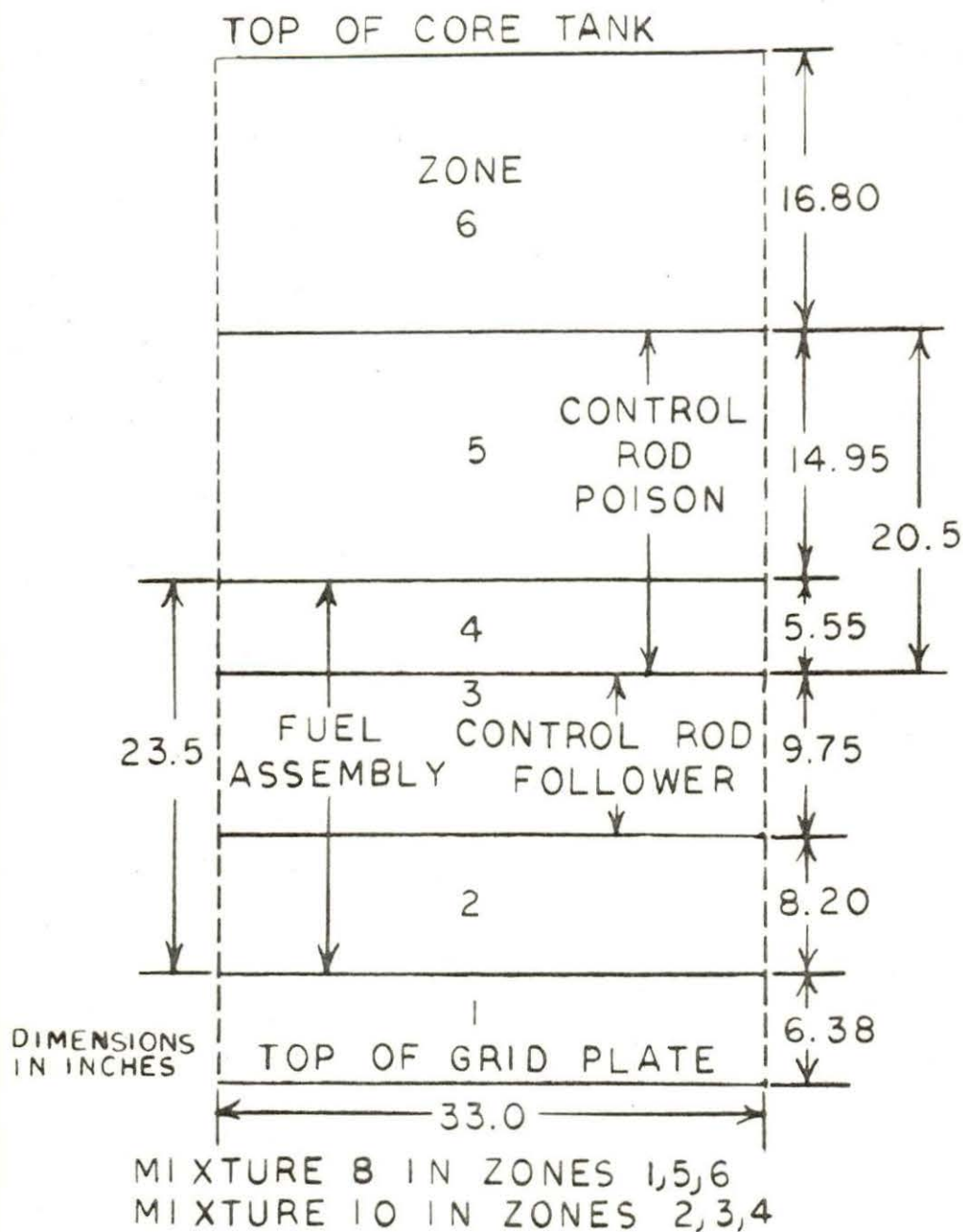
Figure   7.   Six zones of modeled core region

zone is based on the length of the follower which is 9.75 inches. The fourth zone is based on the remaining section of the fuel assembly which is 5.55 inches. The other boxes in this zone contain a section of control rod or moderator only. The fifth zone contains two box types, one containing the remaining section of control rod and the other being just moderator. This zone is 14.95 inches high. The last zone is composed of boxes of moderator only and is used to fill the remaining core, with moderator, to the top of the D_2O vessel. The twelve box types do not imply twelve different core materials to be described but rather indicates the need for multiple boxes to completely describe a particular item. For example, due to the number of zones, it required three box types to describe the fuel assembly with the only difference between boxes being the height.

At this point, an array 11 x 7 x 6 has been described made of twelve box types all 3 x 4.5 inches in the x, y field and of six different heights in the z field. These twelve box types can be divided into four groups: fuel assembly, control rod and two groups of moderator.

Since a complete three-dimensional description of the reactor would require a great deal of computer storage, a compromise was reached where the major components were described in rather close detail while the structural material was accounted for by homogenizing it with the moderator. Of

the four groups of box types, the fuel assembly and control
rod fall into the major component class and the following
paragraphs are used to describe their geometric layout in the
x, y field, while in the case of the moderator box types, the
geometry is completely described by the 3 x 4.5 inch dimen-
sions. The only thing remaining is to define the mixture
contained in the different types.

The initial step in describing the fuel assembly was to
reduce its complexity by only taking into consideration the
fuel zone. Secondly, the slightly curved plates were
straightened so that the assembly could be described in terms
of a series of cuboids. Figure 8 shows the resulting box
whereby starting with the middle fuel plate and adding
cuboids as shown in Table 1, the fuel assembly is described
in the x, y plane. In this case, the fuel and the aluminum
clad were homogenized to form the fuel plate thereby reducing
the number of cuboids needed to describe the assembly.

Figure 9 shows the box type describing the poison sec-
tion of the control rod with Table 2 indicating the dimen-
sions, geometry and material arrangement. As with the fuel
plate, the cadmium and stainless steel clad were homogenized.
One section of the control rod differs from the other two in
that it describes only the follower which is made of
stainless steel and has an inner radius of 1.435 inches while
the outer radius is 1.5 inches.
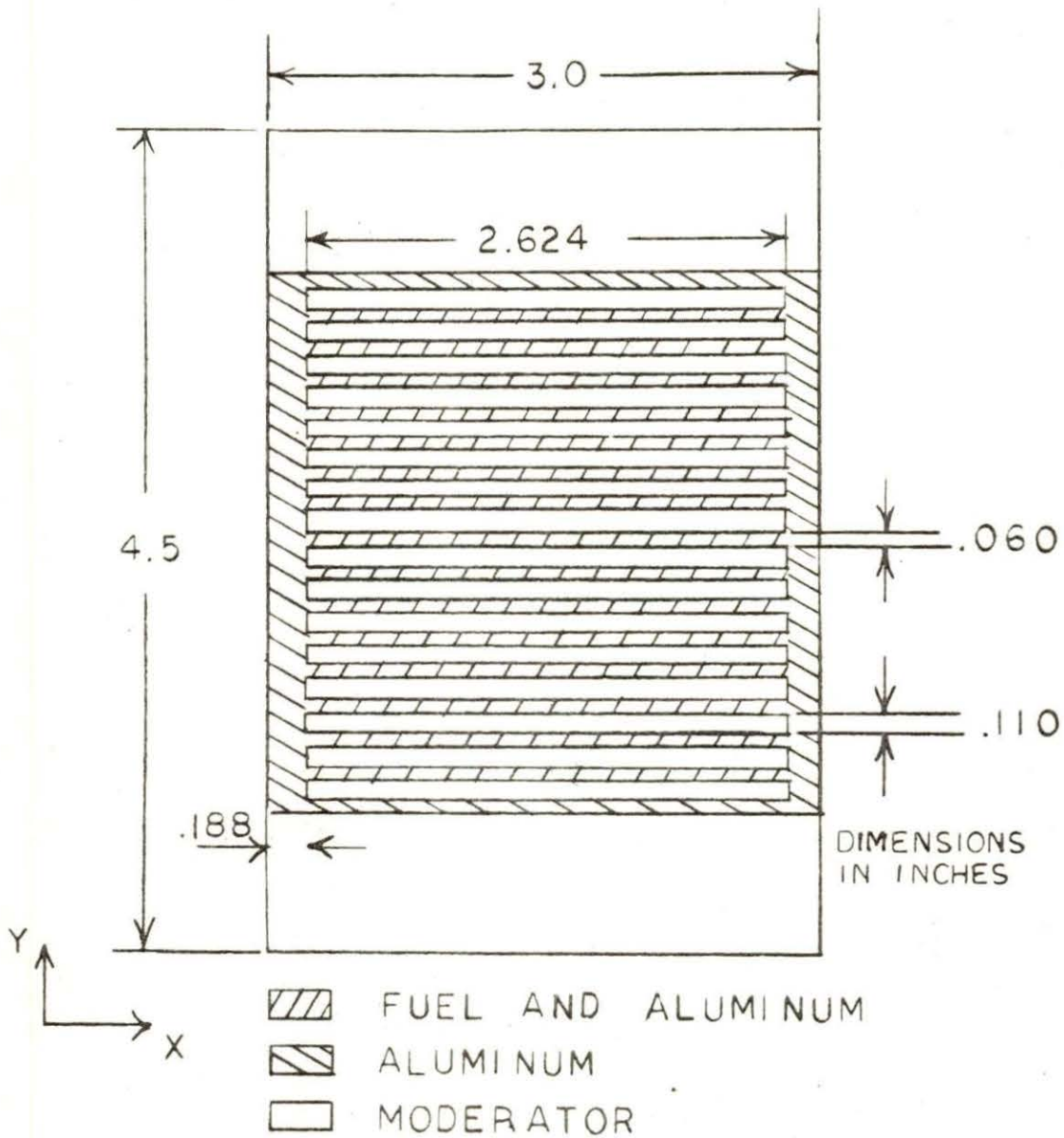
Figure 8. Modeled fuel assembly

Table 1. Cuboid arrangement of modeled fuel assembly box

Cuboid Number	Material	y-dimension (inches)	x-dimension (inches)
1	fuel + aluminum	0.06	2.624
2	moderator	0.28	2.624
3	fuel + aluminum	0.40	2.624
4	moderator	0.62	2.624
5	fuel + aluminum	0.74	2.624
6	moderator	0.96	2.624
7	fuel + aluminum	1.08	2.624
8	moderator	1.30	2.624
9	fuel + aluminum	1.42	2.624
10	moderator	1.64	2.624
11	fuel + aluminum	1.76	2.624
12	moderator	1.98	2.624
13	fuel + alumunum	2.10	2.624
14	moderator	2.32	2.624
15	fuel + aluminum	2.44	2.624
16	moderator	2.56	2.624
17	aluminum	2.78	3.000
18	moderator	4.50	3.000
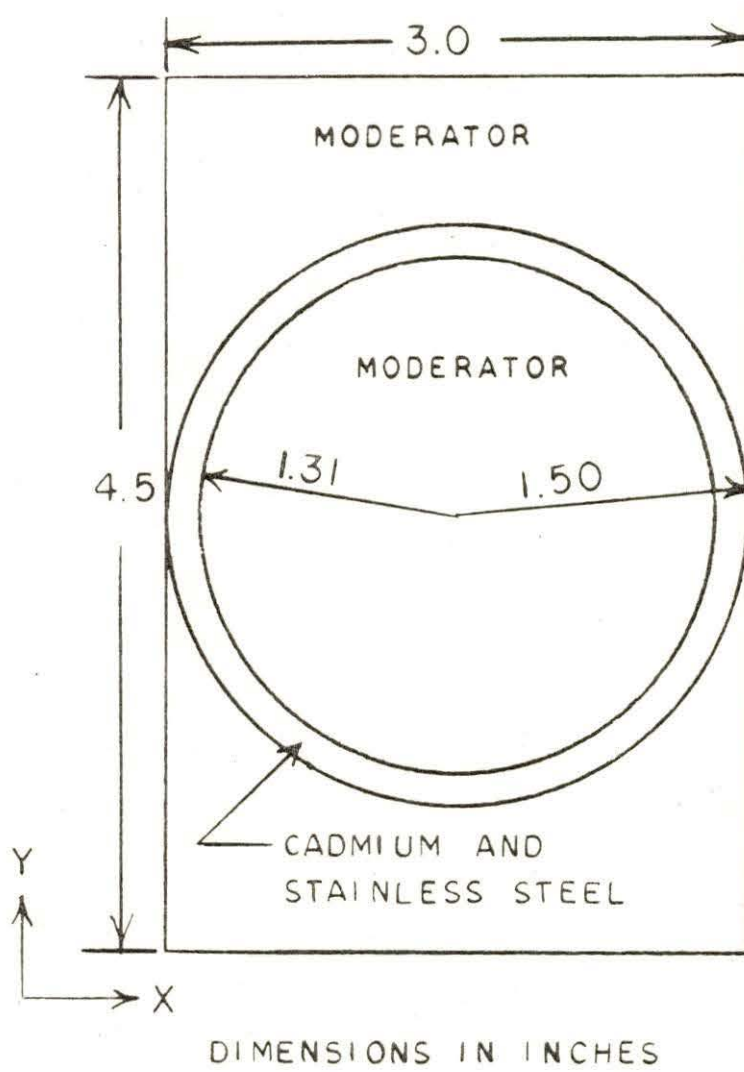
Figure 9. Modeled control rod

Table 2. Box description of modeled control rod

Item Number	Geometry	Material	x-dimension or Radius (inches)	y-dimension (inches)
1	Cylinder	Moderator	1.31	--
2	Cylinder	Stainless Steel and Cadmium	1.50	--
3	Cuboid	Moderator	3.00	4.50

The moderator boxes are all 3 x 4.5 inch boxes, the difference between them being due to the amount of structual material located in a particular zone. In this case, for zones 2, 3 and 4, the moderator is pure D_2O and in this section of the core, the control rods and fuel assemblies are completely described. In zones 1, 5 and 6, the moderator is homogenized with the total volume of structural material located in these regions. Figure 10 shows the regions the core was broken into in determining the D_2O and and structural material inventory. Table 3 gives the volume of moderator and structural material in the various regions.

Now that each box type has been described in terms of a geometric arrangement, it is necessary to instruct the computer what material or mixture to place in each respective box and how to arrange the boxes so that they represent the core region.

In order to accomplish the first item, the user must establish a mixing table. This table can be made up of items listed in Appendix A, Section A, which lists the description of albedo functions available. Section B lists the mixtures whose cross sectional data are available, such as stainless steel, water, etc. Section C lists the elements whose cross-sectional data are available.

In order to form the mixing table, each mixture is numbered sequentially starting with one. Each numbered entry
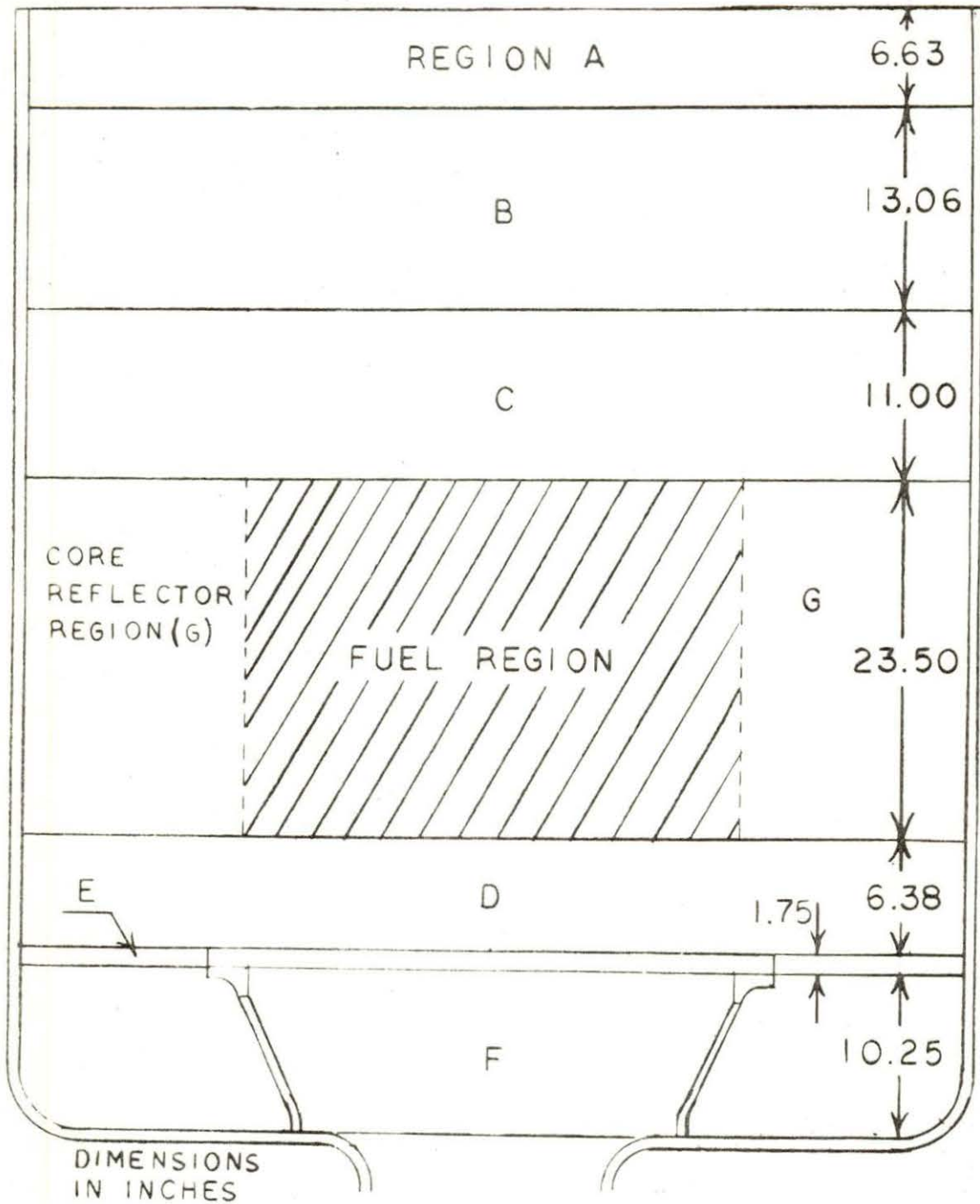
Figure 10. Regions used in homogenization process

Table 3. Volume inventory of reactor materials

| Region | Volume (cubic inches) | | |
	Aluminum	Moderator	Void*
A + B	1380.14	54272.02	--
C	2384.61	28717.16	--
D	1126.08	16911.65	--
E	1643.29	3304.71	--
F	1824.04	26772.99	384.14
G	2658.06	27956.31	11402.16**

----

* Voids due to irradiation facilities.

** Total vertical thimble volume included in this region.

may be composed of an individual element, a group of elements, a single mixture from Section B, Appendix A, or finally any combination of the previous. The input nuclide number obtained from Appendix A is entered along with the volume fraction (if the entry is from Section B) or the atomic density (if the entry is from Section C) for each item entered. This is repeated for each numbered mixture until the table includes all the materials described in the core. Table 4 shows an example of a mixing table.

The arrangement of the different box types in each zone is done by considering them as consisting of a three-dimensional matrix of box type numbers, with the box position increasing in the positive x and y directions. To enter boxes into this matrix, a method similar to a Fortran do loop is used, where three sets of three fields are needed. The first entry in each set is the starting point, the second is the ending point and the third entry of each set is the number of boxes by which increases are made. Figure 11 shows the mixed boxed formation of zone three of the core. Table 5 shows the do loop formation of this matrix. It should be noted that the last box type that locates a specific spot is the one that is retained.

Once the core region has been established, the core boundary is entered. The core boundary is a set of dimensions which completely encloses the core matrix. The mixture

Table 4. Example of mixture table

Mixture	Nuclide ID Number	Atomic Density or Volume Fraction

Mixture	Nuclide ID Number	Atomic Density or Volume Fraction
1	1201	6.4934 E -02
1	8100	3.2467 E -02
1	501	2.3000 E -02
2	13100	5.9600 E -02
2	-92504*	4.7908 E -04
2	92845	3.5592 E -05
3	200	1.0000 E -00

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* A negative Nuclide ID number indicates that the fission
  spectrum for that nuclide will be used.
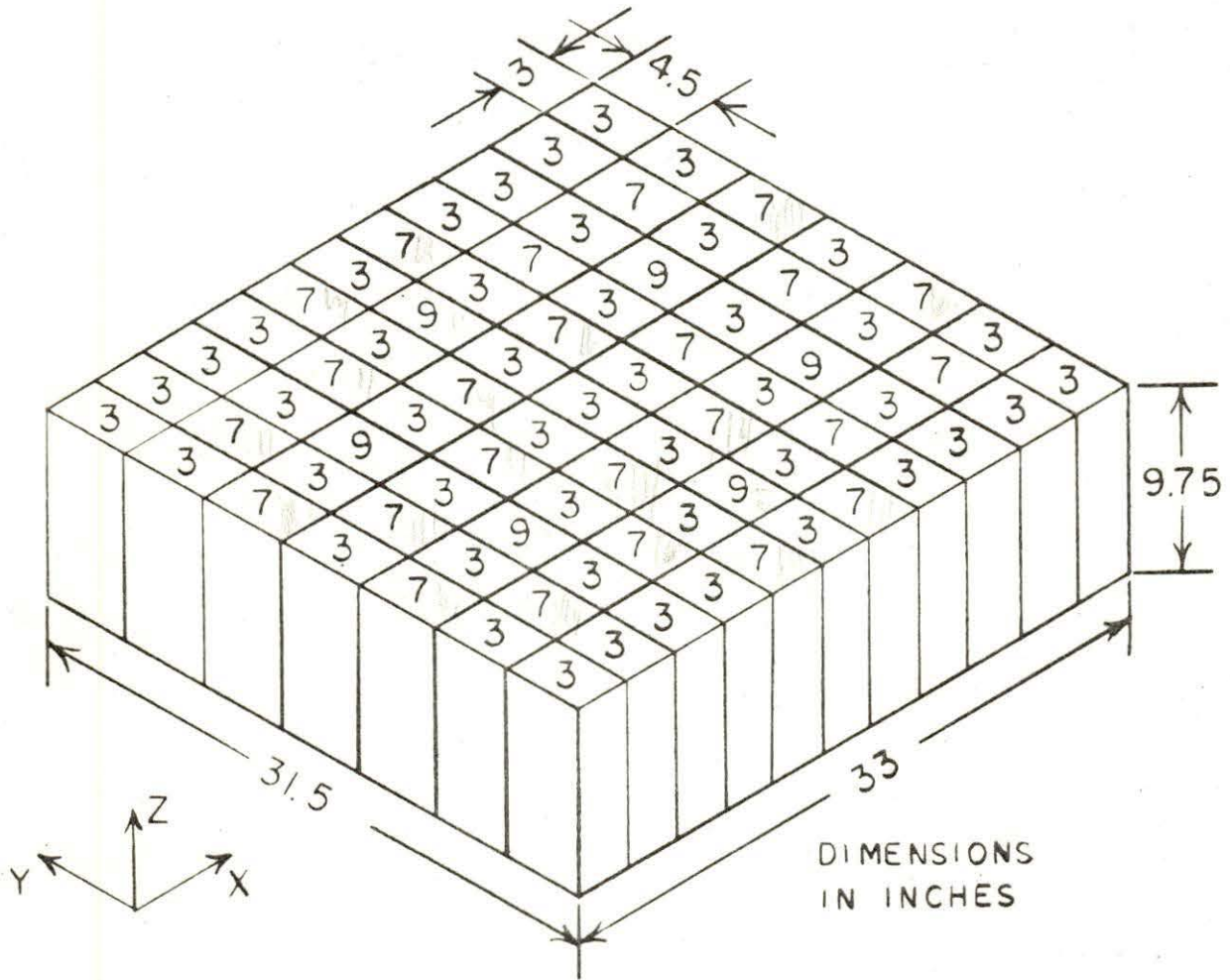
Figure 11. Mixed box orientation - zone 3

Table 5. Mixed box formation of zone 3

Box Type	X	Y	Z
3	1,11,1	1,7,1	3,3,1
7	5,7,2	1,7,2	3,3,1
7	2,4,2	2,6,2	3,3,1
7	1,11,10	3,5,2	3,3,1
9	6,6,1	2,6,4	3,3,1
9	3,9,6	3,5,2	3,3,1

----

input is represented by a zero which implies a void. All
reflector regions are referenced to the core boundary. The
reflector was added on in three sections. This allowed the
moderator mixture in each of the regions to be different.
The first region added was that above the grid plate and out-
side the core matrix. The next region was that region that
contained the grid plate. The last moderator region was the
remaining moderator below the grid plate.

For the region above the grid plate, the aluminum struc-
tural volume, voids due to experimental facilities, the D_2O
in regions A, B, C, D and the core reflector region shown in
Figure 10 were homogenized. The fuel region in Figure 10 is
equivalent to zones 2, 3 and 4 of Figure 7. In regions E and
F, the D_2O and structural aluminum were also homogenized.
Regions E and F were not combined to prevent dilution of the
high aluminum concentration in region E with the low aluminum
concentration of region F. This completed the description of
the core and moderator. The next item added was the aluminum
D_2O vessel. The remaining item left to describe is the
thermal shield.

In order to save computer time, it was decided to use
one of the albedos included in the KENO program. The closest
approximation was the 12 inch H_2O differential albedo; but to
apply it, the core vessel must be surrounded by a cube or
cuboid. Therefore, a cuboid was added with the appropriate

dimensions that allowed it to be tangent at the diameter of
the vessel. The mixture added to the corners was light
water. The albedo was then added referenced to this outer
cuboid. Since the thermal shield surrounds just the sides
and bottom of the core, the computer was instructed to apply
the albedo to these areas only. This then, completed the
model of the reactor. Section D describes in more detail the
proper arrangement of these data on computer cards for input
to the program KENO.

C. Selection of Cross Sections

The KENO cross-section library is divided into two
parts: the first is a table containing nine items that are
mixtures. When using materials from this section, volume
fractions are used instead of number density for the value of
RHOA on card 5 of the input. This implies that the first
table is composed of macroscopic cross sections rather than
microscopic, as is the second part of the cross-section li-
brary. In both tables, some of the cross sections are either
lethargy weighted or fission spectrum weighted. The choice
between using lethargy weighted or fission spectrum weighted
cross sections was one of trial and error with the final se-
lection based on the combinations that yielded a k-effective
closest to one for the case where the control rods were at
40% withdrawn.

In the second section of cross sections, some elements, namely the fuels, have a number of different listings based on the potential scattering cross section of the medium per atom of the reacting element. Once the potential scattering cross section has been calculated, the proper cross section can be chosen from the list. This calculation for the ALRR fuel assemblies is shown in Appendix B.

If neither table has the cross section desired, it is possible to enter the appropriate sixteen-group cross section by cards as demonstrated in Section D on input to KENO. The majority of cross sections listed on tape are from the Hansen-Roach (12) sixteen-group cross section set.

D. Input Format

The following is the data guide from the KENO manual for the proper input of data. The information is in the order in which the computer reads the data. The Fortran format required is given along with the nomenclature of each item as it is used in the computer program. Data cards not used in this particular application but listed in the manual, have been omitted here.

Card 1   Time Card   Format (2I10.5)   maximum computer
                                             time (in minutes)
                                             to be allowed for
                                             problem

Card 2   Title Card   Format (18A4)   contains title
only

Card 3   Parameter Card   Format (13I5)

cols				
cols 1-5	NBA	Number of generations		
cols 6-10	NPB	Number per generation		
cols 11-15	NSKIP	Number of generations to be skipped		
cols 16-20	NGP	Number of energy groups		
cols 21-25	NDS	Number of downscatters		
cols 26-30	NMAT	Number of input nuclides		
cols 31-35	MATT	Number of mixtures		
cols 36-40	NMIX	Number of mixing table entries		
cols 41-45	KREFM	Total number of geometry cards. This includes the Core Boundary Card, but not the Box Type cards.		
cols 46-50	NBOX	The number of box types		
cols 51-55	NBXMAX	# of units in the x direction		
cols 56-60	NBYMAX	# of units in the y direction		
cols 61-65	NBZMAX	# of units in the z direction		

Card 4   More Parameters   Format (14I5)

cols 1-5   NTAPE   The number of input nuclides to be read from tape. If NTAPE > 0, read a KENO cross-section tape. If NTAPE < 0, read a XSDRN cross-section tape.

```
cols   6-10    NXX        specifies albedo options

               NXX =      Albedo ID number

cols  11-15    NSCH       Search type = 0 if no search

cols  16-20    LIST       Applies only to cross-sections
                          read from tape.

               LIST = 0   Do not print input cross-sections

cols  21-25    NOXS       If NOXS = 0, read in new cross-
                          sections

cols  26-30    NTYPST     The type of starting distribution
                          NTYPST = 1 Cosine over array, in
                          fissile material only

cols  31-35    NFLX       NFLX = 1 Fluxes not calculated

cols  36-40    NFDEN      NFDEN = 1 Fission densities
                          will not be calculated
```

Card 5   Reflector constants   Format (6E10.3)

Note: use negative number for diff. albedo

```
cols   1-10    REFCST(1)  Reflector const. for +x direction

cols  11-20    REFCST(2)  Reflector const. for -x direction

cols  21-30    REFCST(3)  Reflector const. for +y direction

cols  31-40    REFCST(4)  Reflector const. for -y direction

cols  41-50    REFCST(5)  Reflector const. for +z direction

cols  51-60    REFCST(6)  Reflector const. for -z direction
```

Card(s) 6 Mixing Table Format (2I10, E10.4) Enter only if

                                              NOXS = 0

```
cols   1-10    KKA        Mixture number
```

cols 11-20   NMA   Nuclide ID number

A negative ID indicates that the
fission spectrum for that nuclide
will be used. Nuclides read from
cards are assigned sequential ID
numbers starting with 1

cols 21-30   RHOA   Number density (atoms/barn-cm)

there must be NMIX cards 6

Cards(s) 7   Cross Sections From Cards   Enter only if

NOXS = 0 and

NTAPE < NMAT

Card(s) 7a   Title Card   Format (17A4,A3,I1)

cols 1-71   XST   Nuclide identification

cols 72   IORDER   Enter 0 if P_0 component only

Card(s) 7b P_0 cross-section set   (two cards per group)

cols   1-12   13-24   25-36   37-48   49-60   61-72

GP1 σ_a^1 $\gamma\sigma_f^1$ σ_t^1 $\sigma_{1\to1}$ $\sigma_{1\to2}$ $\sigma_{1\to3}$

GP1 $\sigma_{1\to4}$ $\sigma_{1\to5}$ $\sigma_{1\to6}$

Repeat sequence for groups 2 thru 16

Card(s) 8   Geometry Card and Weights

Card(s) 8a   Box Type Card   Format (2A4,A2,I6)

cols 1-8   "BOX TYPE" (left adjusted)

cols 11-16   The box number (between 1 & NBOX)

(right adjusted)

Card(s) 8b   Geometry Cards   Format (2A4,A2,I6,5E8.0)

cols   1-10   FGEOM   FGEOM may be one of the following

and must be left adjusted: CUBE

CUBOID, SPHERE, CYLINDER, XCYLIN-

DER, YCYLINDER, HEMISPHERE.

cols 11-16   MAT   Mixture number

cols 17-24   XX(1)   Radius for sphere, cylinders,

hemisphere +x dimension for cube,

or cuboid

cols 25-32   XX(2)   -x dimension for cube or cuboid,

+z for cylinder, +x for xcylinder,

+y for ycylinder

cols 33-40   XX(3)   +y dimension for cuboid

-z for cylinder, -x for xcylinder,

-y for ycylinder

cols 41-48   XX(4)   -y dimension for cuboid

cols 49-56   XX(5)   +z dimension for cuboid

cols 57-64   XX(6)   -z dimension for cuboid

Card(s) 8c   Weight Cards   Use blank card for default

values.

Note: repeat 8a,8b,8c, sequence until NBOX box

types have been described

Card(s) 8d Core Boundary Card Format (2A4,A2,I6,6E8.0)

cols 1-8   FGEOM   "CORE BDY" (left adjusted)

cols 9-16 MAT   Zero usually (right adjusted)

cols 17-24 XX(1)   +x dimension of cube or cuboid

```
  cols 25-32   XX(2)        -x dimension of cube or cuboid
  cols 33-40   XX(3)        +y dimension for cuboid
  cols 41-48   XX(4)        -y dimension for cuboid
  cols 49-56   XX(5)        +z dimension for cuboid
  cols 57-64   XX(6)        -z dimension of cuboid
```

Card(s) 8e Weight Card   Use blank card for default

values.

Card(s) 8f Reflector Geometry Cards   See cards 8b.

Card(s) 8g Weight Cards   See cards 8c.

Note: repeat 8f,8g until reflector region has

been completely described.

Card(s) 9 Mixed Box Orientation Cards

Format [I2,3(3X,I4,1X,I4,1X,I4),1X,A1]

Note: last data card uses nonblank character in column

55.

V. EXPERIMENTAL MEASUREMENTS AND RESULTS

Once the reactor core was modeled, KENO was run on the
Iowa State University IBM computer, Model 360/65, for a num-
ber of different conditions. Initially, runs were made to
establish the effect of using lethargy or fission spectrum
weighted cross sections. Runs were also made to establish
the effect of homogenizing various sections of the core. The
only criteria used to judge the effect of these runs was
based upon the fact that the actual reactor critical condi-
tion for a twenty-four fuel assembly core was obtained with a
control rod bank position of 40% withdrawn. Therefore, runs
that yielded a k-effective closest to one were judged to be
the proper selection. The final selection of input data re-
sulted in a k-eff of 1.04107 ± .00556 for 22275 neutron
histories with 275 neutrons per generation. This final ar-
rangement consisted of using the fission spectrum weighted
light water cross section in the fuel region and the lethargy
weighted cross section in the moderator regions shown in
Figure 10. The value obtained implies that with the control
rods 40% withdrawn, the reactor is super-critical. In
criticality safety calculations (13) using KENO, a value
within the range of $-3\%\Delta k/k$ of a k-eff of 1.0 is considered
to be critical. Taking this into consideration along with
the fact that there is no temperature compensation for the
cross-section data used, it was felt that the value of (+3.95

± .53)%Δk/k was a reasonable value to establish as a base run
for future critical measurements.

The next question that was considered was should the
computer run be one long run or should a number of shorter
runs be made, varying the number of neutrons per generation
for each run and then summing the data from all runs. The
reason behind this question was due to the fact that the
final answer of one long run would be based upon one
continuous random sequence and only one initial source dis-
tribution. The data obtained from multiple runs, varying the
neutrons per generation for each run, would reflect different
random number sequences and, consequently, different initial
source distributions. Statistically, the results should be
equal, assuming infinite computer time. Since it was
relatively easy to vary the random number generation se-
quence, which is accomplished by varying the number of
neutrons tracked per generation, an attempt was made to
answer the question, by making three short runs and comparing
the results with the one long run. Table 6 shows the data
used where set #1 is the one long run and set #2 is three
separate short runs. Applying equation one to the data of
set #2 yields

$$\text{EQ. 1} \quad \text{k-eff} = \frac{\sum \text{k-eff}}{3} \pm \sqrt{\frac{\sigma_1^2 + \sigma_2^2 + \sigma_3^2}{3}}$$

Table 6. Data used for determining length of run

Set	k-eff	Sigma	Neutrons per Generation	Run Time (Hours)	Total Histories
1	1.04107	.00556	275	1.5	22275
2	1.03658	.01463	300	0.5	6600
	1.02573	.00831	325	0.5	6500
	1.04147	.01010	360	0.5	6480

----

a k-eff of 1.03459 ± .00654. If the data of the second set
are further broken down and analyzed by finding the average
k-eff for the 63 generations which composed the 19,580
histories and the standard deviation of the average is calcu-
lated using equation two, the results obtained are an avg. k-
eff = 1.03443 ± .00670

$$\text{EQ. 2.} \quad \sigma = \frac{\sum (k\text{-eff}_i - \overline{k\text{-eff}})^2}{\text{number of generations}}$$

k-eff$_i$ being the individual k-effective of each generation
and $\overline{k\text{-eff}}$ is the mean. It is observed that both methods of
analyzing the data of the second set are in close agreement.

Upon comparing the data of the two methods, it was ob-
served that the magnitude of the value of reactivity worth
obtained by subtracting the two sets of data was the same
relative magnitude as the deviation of each set. Therefore,
it was concluded that either method was suitable and for
convenience, all runs would be single runs rather than the
multiple runs.

During the execution of the program, absorbtion of
neutrons is not allowed. Rather than absorbtion, at each
collision point of a neutron tracking history the weight of
the neutron is reduced by the absorbtion probability. When
the neutron weight has been reduced below a specified point

for the region in which the collision occurs, Russian
roulette is played to determine if the neutron's history is
to be terminated at that point or if the neutron is to
survive with an increased weight. There are three specified
points which are entered into the program; these being WTLOW,
WTAVG and WTHIGH. If a neutron's weight increases above the
WTHIGH value, it is split into two neutrons, each with one-
half the weight. The probability of survival when Russian
roulette is played depends upon the values chosen for WTLOW
and WTAVG. The justification for the values used for these
weights is based upon the number of neutrons tracked during a
fixed amount of computer time. It is possible to enter user
supplied weights or use those suggested in the code.
Therefore, a short test was run to see if the default values
were suitable for this core configuration. Table 7 shows the
results of these tests and illustrates that the default
values were a proper selection. WTAVG is related to WTLOW
and WTHIGH by WTAVG times three or divided by three; hence,
only WTAVG is listed in the table. Also, the weights were
varied in the two main regions of concern, the fuel region
and the moderator region.

Since a differential albedo was used to approximate the
thermal shield, a computer run was made to determine the
reactivity effect of this model and compare the reactivity
worth obtained with that obtained from actual reactor meas-

Table 7. Effect of varying WTAVG on total histories obtained

Case	WTAVG	Region	Histories
1	0.5* 0.5*	fuel moderator	5100
2	0.3 0.5	fuel moderator	3600
3	0.3 0.7	fuel moderator	3600
4	0.25 0.3	fuel moderator	3000

----

* Default values.

urements. Since the base run was available, a run was made
without the albedo present and the cuboid surrounding the
core tank, which is normally filled with light water, de-
clared a void. This run resulted in a k-eff of 1.01993 ±
.00592. Using this value and the base run information, the
reactivity worth due to the addition of the albedo is (1.99 ±
.79)%$\Delta k/k$. The actual measured value obtained at the time of
the initial criticality testing was 1.48%$\Delta k/k$. Therefore,
the albedo package was considered an adequate representation
of the thermal shield.

After these initial runs were completed, another series
of computer runs were made so that the code could be further
checked out by comparing values determined by the code with
values of measurements obtained from actual reactor experi-
ments. These measurements consisted of control rod worths,
fuel assembly worth, converter assembly worth and H_2O filled
fuel assembly worth. The following paragraphs will discuss
each of the above experiments.

Control rod worths are measured after every refueling at
ALRR. The method used is the "rod drop" technique. This is
a derivation of the integrated count method of control rod
calibration and utilizes one-group, space-independent, zero-
power kinetic theory to calculate the behavior of a reactor
following a step change in reactivity. This method is appli-
cable to changes in reactivity up to 10%$\Delta k/k$. The worth of

each of the six rods is measured individually and then summed, applying a rod shadow factor, in order to obtain the total worth of all rods. The results of the June, 1973, measurements gave a total control worth of 27.69%$\Delta k/k$ and a reactor shutdown margin of 14.86%$\Delta k/k$. Utilizing the KENO code, runs were made for the case with the control rods 100% withdrawn and for the control rods fully inserted. The values of k-eff are as follows: for the rods full in, k-eff = .87034 ± .00669 and for the rods full out, k-eff = 1.14864 ±.00762. These values result in a total rod bank worth of (27.84 ± 1.03)%$\Delta k/k$ with a shutdown margin of (14.90 ± 0.78) %$\Delta k/k$. These values were based on a minimum of 13500 neutron histories.

The reactor measurements of the reactivity worth of a fuel assembly, converter assembly and H_2O filled fuel assembly were done using a cold, clean core and zero power. The procedure used to obtain the reactivity worth of an item will be described for the fuel assembly. The procedure is essentially the same for the other items.

Starting with a new core of twenty-four fuel assemblies, the reactor was taken just critical with the control rods in a six rod bank. The rod bank position was recorded along with core temperature and other data. The control rod configuration was then changed to a five rod bank with the regulating rod at 75% withdrawn, maintaining the reactor just

critical. Pertinent data was recorded and the reactor shut down. The fuel assembly selected to have its reactivity worth measured, was removed from the core using the appropriate procedures. Upon its removal, another zero power run was made, utilizing a six rod bank and then the five rod bank as determined previously, adjusting for criticality with the regulating rod, recording the rod positions and other data. Utilizing the control rod positions obtained for all four runs and the previously obtained control rod worth calibration curves, the fuel assembly worth can be determined. Using the data from the two six-rod bank runs, the worth of the single fuel assembly is just the difference in reactivity worth of the two six-rod banks correcting for temperature differences between runs. Utilizing the data from the remaining two runs, the worth of the single fuel element is just the reactivity worth represented by the difference in the regulating rod position for the two runs since the five-rod bank is the same for both runs. A correction for temperature is then made if needed. The measured reactivity values obtained for the fuel assembly, converter assembly and the H_2O filled assembly were 2.41%$\Delta k/k$, 2.24%$\Delta k/k$ and 2.88%$\Delta k/k$ respectively.

The procedure used to calculate the reactivity worth of a fuel assembly was to first make a computer run using twenty-four assemblies and then eliminate one assembly from

the proper geometric location, replacing it with moderator, re-running the program for the twenty-three assemblies. The difference in reactivity obtained from the two runs is the calculated reactivity worth of one assembly. The value obtained was $(1.74 \pm .83)\% \Delta k/k$.

For the case of the converter assembly, an additional box type had to be added describing the converter and then added to the array in its proper location. The KENO result of this measurement was $(1.84 \pm 0.75)\% \Delta k/k$.

The remaining measurement is the H_2O filled element. This is a fuel assembly modified by welding so that it could be filled with light water without fear of contaminating the heavy water. The reactivity worth of an H_2O filled element was calculated for two different cases by KENO. In the first case, the worth of an element filled with light water was represented by a lethargy weighted cross section and in the second case, the light water was represented by the fission spectrum weighted cross section. The results of these KENO runs are as follows: for the lethargy case the worth was $(1.99 \pm 0.86)\% \Delta k/k$ and for the fission spectrum weighted case, $(2.08 \pm 0.86)\% \Delta k/k$.

VI. SUMMARY AND CONCLUSIONS

The advantage of the three-dimensional aspect of the Monte Carlo method was decreased somewhat by the need to limit the input, thereby reducing the storage space required, and the need to find ways to reduce the running time. As was shown, this was accomplished by various methods such as homogenization of material, the use of albedo functions and the proper statistical weighting. Even with these disadvantages, the ability to describe portions of the reactor in a three-dimensional arrangement along with the fact that the core could be analyzed with the control rods included provide a significantly different approach to criticality calculations involving the ALRR.

Once the reactor was described in sufficient detail, it was found that a number of runs had to be made in order to verify the proper use of cross sections, albedos, etc. Once this had been done, it was then possible to make a series of runs to verify the accuracy of the program by comparing reactivity values obtained from the program to reactivity values obtained from reactor measurements. Table 8. summarizes the results of these runs. The first of these runs, the control rod worths and shutdown margin were found to give very good results.

Although the results were extremely close, a degree of caution should be exercised since the actual control rod

Table 8. Summary of KENO results and reactor measurements

Run	Reactor Measurement %Δk/k	KENO Calculation %Δk/k
control rod worth	27.69	27.84 ± 1.03
reactor shutdown margin	14.86	14.90 ± 0.78
thermal shield	1.48	1.99 ± 0.79
ALRR fuel assembly	2.41	1.74 ± 0.83
CP-5 converter assembly	2.24	1.84 ± 0.75
ALRR H_2O filled assembly	2.88	--
501 cross-section	--	2.08 ± 0.86
502 cross-section	--	1.99 ± 0.86

----

measurements may deviate ±5%.

It is well to note, even with the core modeled in a slightly super critical condition, the reactivity determined from the difference between runs gave fairly accurate answers. It was also observed from these data that the accuracy increased as the magnitude of the reactivity change increased. That is, the deviation of the control rod worths was about 5% of the total worth while the deviation of the fuel assembly worth was about 30% even though the fuel measurement was based upon a third more neutron histories. This correlates with what G. E. Whitesides has said in an article on the Monte Carlo method (14), in which he implies that for the calculation of a Δk between two cases to be meaningful, the Δk would have to be large with respect to the estimated standard deviation associated with the calculation.

The converter measurement represents the ability for the KENO program to handle reactivity worth measurements in locations other than a fuel assembly or control rod location. The converter was measured in the center experimental facility location, which is located in the center of the core. The reactivity worth of this converter, as calculated by KENO, was less than the measured value; but, again, the measured value fell within the limits of deviation with the statistics based upon a minimum of 22,240 neutron histories.

As shown in the case of the fuel assembly, the value of reactivity associated with the standard deviation is about a third of the mean value for k-effective. Even though there is a large deviation in the case of the smaller reactivity measurements, the consistency of the measured value being within the deviation allows the reactor physicist to include the deviation and predict whether or not an experiment will violate the operating limit concerning excess reactivity loading with a high reliability even though the exact value of the experiment can not be predicted to the same accuracy.

The reactivity calculation for the H_2O filled assembly was the only case where the results of KENO did not span the measured reactivity value when the deviation was considered. This calculation was made for two cases. The first case used the fission spectrum weighted cross section for the light water and its result did include the measured value when the deviation was considered. The second case used the lethargy weighted cross section for light water. The results from that calculation were slightly less than the first case and when the deviation was included, the measured value was not spanned. Neither calculated value was in close agreement with the measured value and upon further investigation into the matter, it was found that other users of KENO (15) had found similar problems when trying to calculate cases where abrupt changes in cross section occurred in small quantities,

such as the small volume of H_2O in the D_2O moderated core.
It was also indicated that the authors of KENO were working
on a tracking system that would relieve the problem.

The difference obtained between the two cases of the
light water element is significant since it shows the effect
of the different cross sections, even though only a small
fraction of the core was involved. The volume of moderator
in one element is less than 2500 cubic centimeters which is
very small compared to the D_2O inventory of approximately
2,600,000 cubic centimeters in the reflector region.

In a program such as KENO, there is always room for
continual improvement. Up-dating cross section libraries,
adding changes such as mentioned in the previous paragraph,
modifying routines in order to decrease the amount of comput-
er time; but in the mean time, KENO appears to be a useful
tool at ALRR for predicting reactivity changes above $2\%\Delta k/k$.

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IX. APPENDIX A: CROSS SECTIONS ON TAPE

A. Available Albedos

DIFFERENTIAL ALBEDO, 4 INCIDENT ANGLES

ID NUMBER	DESCRIPTION
1012	12 INCH WATER
2012	12 INCH PARAFIN
3080	78.74 INCH CARBON
4012	12 INCH POLYETHYLENE
5004	4 INCH CONCRETE
5008	8 INCH CONCRETE
5012	12 INCH CONCRETE
5016	16 INCH CONCRETE
5024	24 INCH CONCRETE

ALBEDOS AND TRANSMISSIONS, 4 ANGLES

-5004	4 INCH CONCRETE
-5008	8 INCH CONCRETE
-5012	12 INCH CONCRETE
-5016	16 INCH CONCRETE

B. Mixtures

MIXTURE	DENSITY	NUMBER DENSITY	ID NUMBER
Carbon Steel	7.82g/cc	C=.003921, Fe=.083491	00100
304 Stainless Steel	7.9g/cc	C=3.1691-4, Cr=1.6471-2	00200
		Mn=1.7321-3, Fe=6.036-2	
		Ni=6.4834-3, Si=1.694-3	
Oak Ridge Concrete	2.3g/cc	H=.0085 C=.0202	00300
		O=.0355, Ca=.0111	
		Si=.0017, Mg=.00186	
		Fe=1.93-4, Al=5.56-4	
		K=4.03-5, Na=1.63-5	
X(E) Polyethylene	0.92g/cc	H=.079433, C=.039716	00401
dE/E Polyethylene			00402
X(E) Water	.9982g/cc	H=.066743, O=.033372	00501
dE/E Water			00502
X(E) Plexiglas	1.182g/cc	H=.056884, C=.035552	00601
dE/E Plexiglas		O=.014221	00602

C.   Elements

ID NUMBER	ELEMENT
1101	HYDROGEN X(E)
1102	HYDROGEN DE/E
1201	DEUTERIUM X(E)
3100	LITHIUM-6
3200	LITHIUM-7
4100	BERYLLIUM
5100	BORON
6100	CARBON
7100	NITROGEN
8100	OXYGEN
9100	FLUORINE
11100	SODIUM
12100	MAGNESIUM
13100	ALUMINUM
14100	SILICON
16100	SULFUR
17100	CHLORINE
19100	POTASSIUM
20100	CALCIUM
22100	TITANIUM
23100	VANADIUM
24100	CHROMIUM
25100	MANGANESE
26100	IRON
27100	COBALT
28100	NICKEL
29100	COPPER
30100	ZINC
40100	ZIRCONIUM
41100	NIOBIUM
42100	MOLYBDENUM
48100	CADMIUM
49100	INDIUM
58100	CERIUM
62100	SAMARIUM
63100	EUROPIUM
64100	GADOLINIUM
73100	TANTALUM
74100	TUNGSTEN
82100	LEAD
90104	TH-232 SIG P # 50
90108	TH-232 SIG P # 1000
90109	TH-232 SIG P # 1250
90110	TH-232 SIG P # 1500
90111	TH-232 SIG P # 1750

ID_NUMBER	ELEMENT
90112	TH-232 SIG P # 2000
90113	TH-232 SIG P # 2500
90114	TH-232 SIG P # 3000
90115	TH-232 SIG P # 3500
92300	U-233
92301	U-233-1 SIG P # 20
92302	U-233-2 SIG P # 40
92303	U-233-3 SIG P # 60
92304	U-233-4 SIG P # 100
92305	U-233-5 SIG P # 200
92306	U-233-6 SIG P # 400
92307	U-233-7 SIG P # 600
92308	U-233-8 SIG P # 1000
92309	U-233-9 SIG P # 2000
92310	U-233-10 SIG P # 4000
92311	U-233-11 SIG P # 6000
92312	U-233-12 SIG P # 10000
92400	U-234
92500	U-235 YR
92501	U-235-1R SIG P # 20
92502	U-235-2R SIG P # 40
92503	U-235-3R SIG P # 60
92504	U-235-4R SIG P # 100
92505	U-235-5R SIG P # 200
92506	U-235-6R SIG P # 400
92507	U-235-7R SIG P # 600
92508	U-235-8R SIG P # 1000
92509	U-235-9R SIG P # 2000
92510	U-235-10R SIG P # 4000
92511	U-235-11R SIG P # 6000
92511	U-235-12R SIG P # 10000
92600	U-236
92800	U-238-Y
92801	U-238 SIG P # 12
92802	U-238 SIG P # 15
92803	U-238 SIG P # 20
92804	U-238 SIG P # 25
92805	U-238 SIG P # 30
92806	U-238 SIG P # 35
92807	U-238 SIG P # 40
92808	U-238 SIG P # 45
92809	U-238 SIG P # 50
92810	U-238 SIG P # 55
92811	U-238 SIG P # 60
92812	U-238 SIG P # 65
92813	U-238 SIG P # 70
92814	U-238 SIG P # 75
92815	U-238 SIG P # 80

ID NUMBER	ELEMENT
92816	U-238 SIG P # 85
92817	U-238 SIG P # 90
92818	U-238 SIG P # 95
92819	U-238 SIG P # 100
92820	U-238 SIG P # 110
92821	U-238 SIG P # 120
92822	U-238 SIG P # 130
92823	U-238 SIG P # 140
92824	U-238 SIG P # 160
92825	U-238 SIG P # 180
92826	U-238 SIG P # 200
92827	U-238 SIG P # 220
92828	U-238 SIG P # 240
92829	U-238 SIG P # 260
92830	U-238 SIG P # 280
92831	U-238 SIG P # 300
92832	U-238 SIG P # 330
92833	U-238 SIG P # 360
92834	U-238 SIG P # 400
92835	U-238 SIG P # 450
92836	U-238 SIG P # 500
92837	U-238 SIG P # 550
92838	U-238 SIG P # 600
92839	U-238 SIG P # 650
92840	U-238 SIG P # 700
92841	U-238 SIG P # 800
92842	U-238 SIG P # 900
92843	U-238 SIG P # 1000
92844	U-238 SIG P # 1500
92845	U-238 SIG P # 2000
92846	U-238 SIG P # 3000
92847	U-238 SIG P # 4000
92848	U-238 SIG P # 5000
92849	U-238 SIG P # 6000
92850	U-238 SIG P # 8000
92851	U-238 SIG P # 10000
92852	U-238 SIG P # 20000
92853	U-238 SIG P # 40000
92854	U-238 SIG P # 60000
92855	U-238 SIG P # 100000
92856	U-238-1R SIG P # 20
92857	U-238-2R SIG P # 40
92858	U-238-3R SIG P # 60
92859	U-238-4R SIG P # 100
92860	U-238-5R SIG P # 200
92861	U-238-6R SIG P # 400
92862	U-238-7R SIG P # 600
94000	PU-240

ID NUMBER	ELEMENT				
94001	PU-240-1	SIG	P	#	50
94002	PU-240-2	SIG	P	#	100
94003	PU-240-3	SIG	P	#	200
94004	PU-240-4	SIG	P	#	400
94005	PU-240-5	SIG	P	#	600
94006	PU-240-6	SIG	P	#	1000
94007	PU-240-7	SIG	P	#	2000
94008	PU-240-8	SIG	P	#	4000
94009	PU-240-9	SIG	P	#	6000
94010	PU-240-10	SIG	P	#	10000
94011	PU-240-11	SIG	P	#	20000
94012	PU-240-12	SIG	P	#	40000
94013	PU-240-13	SIG	P	#	60000
94014	PU-240-14	SIG	P	#	100000
94015	PU-240-15	SIG	P	#	200000
94016	PU-240-16	SIG	P	#	400000
94017	PU-240-17	SIG	P	#	600000
94018	PU-240-18	SIG	P	#	1000000
94100	PU-241				
94200	PU-242				
94800	PU-238				
94801	PU-238-1	SIG	P	#	100
94802	PU-238-2	SIG	P	#	1000
94803	PU-238-3	SIG	P	#	10000
98804	PU-238 Y				
94900	PU-239				
94901	PU-239-1	SIG	P	#	20
94902	PU-239-2	SIG	P	#	40
94903	PU-239-3	SIG	P	#	60
94904	PU-239-4	SIG	P	#	100
94905	PU-239-5	SIG	P	#	200
94906	PU-239-6	SIG	P	#	400
94907	PU-239-7	SIG	P	#	600
94908	PU-239-8	SIG	P	#	1000
94909	PU-239-9	SIG	P	#	2000
94910	PU-239-10	SIG	P	#	4000
94911	PU-239-11	SIG	P	#	6000
94912	PU-239-12	SIG	P	#	10000
94913	PU-239-13	SIG	P	#	20000
94914	PU-239-14	SIG	P	#	40000
94915	PU-239-15	SIG	P	#	60000
94916	PU-239-16	SIG	P	#	100000

X.   APPENDIX B: CALCULATION OF THE POTENTIAL
SCATTERING CROSS SECTION OF THE FUEL MIXTURE

In order to select the proper cross section for U235 and U238 from the list supplied in the previous section, σ_p (SIG P) for the fuel must be calculated. SIG P is calculated as follows:

$$SIG\ P = \sum \sigma_{si}\ N_i/N_f$$

σ_{si} is the scattering cross section at the applicable energy for each nuclide

N_i is the nuclei density for each nuclide

N_f is the nuclei density for the fuel in question

For the ALRR fuel assembly, the fuel is composed of U238, U235 and aluminum. The nuclei densities being 3.459 E-05, 4.755 E-04 and 5.9607 E-02 respectively. The thermal scattering cross-sections (16) are U235 (10b), U238 (8.3b) and Al (1.4b), where b = barns. The resulting SIG P for U235 is 186b and for U238 it was 2558b. Knowing SIG P, one can then select the proper nuclide from the table.

XI. APPENDIX C: CALCULATION OF REACTIVITY WORTH AND DEVIATION

This calculation consists of converting a value of k-effective and its corresponding deviation into a $\%\Delta k/k$ value with its deviation and then, in some cases, finding the difference between two reactivity worths in $\%\Delta k/k$ and its corresponding deviation. The relationship between $\Delta k/k$ and k-effective is as usual: $\Delta k/k = (k\text{-eff} - 1.0)/k\text{-eff}$. To find the deviation, it is necessary to first consider the numerator alone which is in the form of $y \pm x$ where the deviation is $p_{num} = \pm\sqrt{(p_x^2 + p_y^2)}$.

Since the deviation of the critical condition (1.0) is zero, then obviously the deviation of the numerator is just the deviation of k-effective. The form of the equation then becomes x/y where $p = \pm\sqrt{(y^2 p_x^2 + x^2 p_y^2)}/y^2$ but from above $p_x = p_y$ so $p = \pm p_x\sqrt{(y^2 + x^2)}/y^2$ where $y = k\text{-eff}$ and $x = k\text{eff}-1$ and p_x is the standard deviation of k-eff. At this point, k-effective can be converted to a $\Delta k/k$ value along with its deviation. If two values of $\Delta k/k$ are subtracted, then the first form $(x \pm y)$ applies and the new deviation can be calculated.